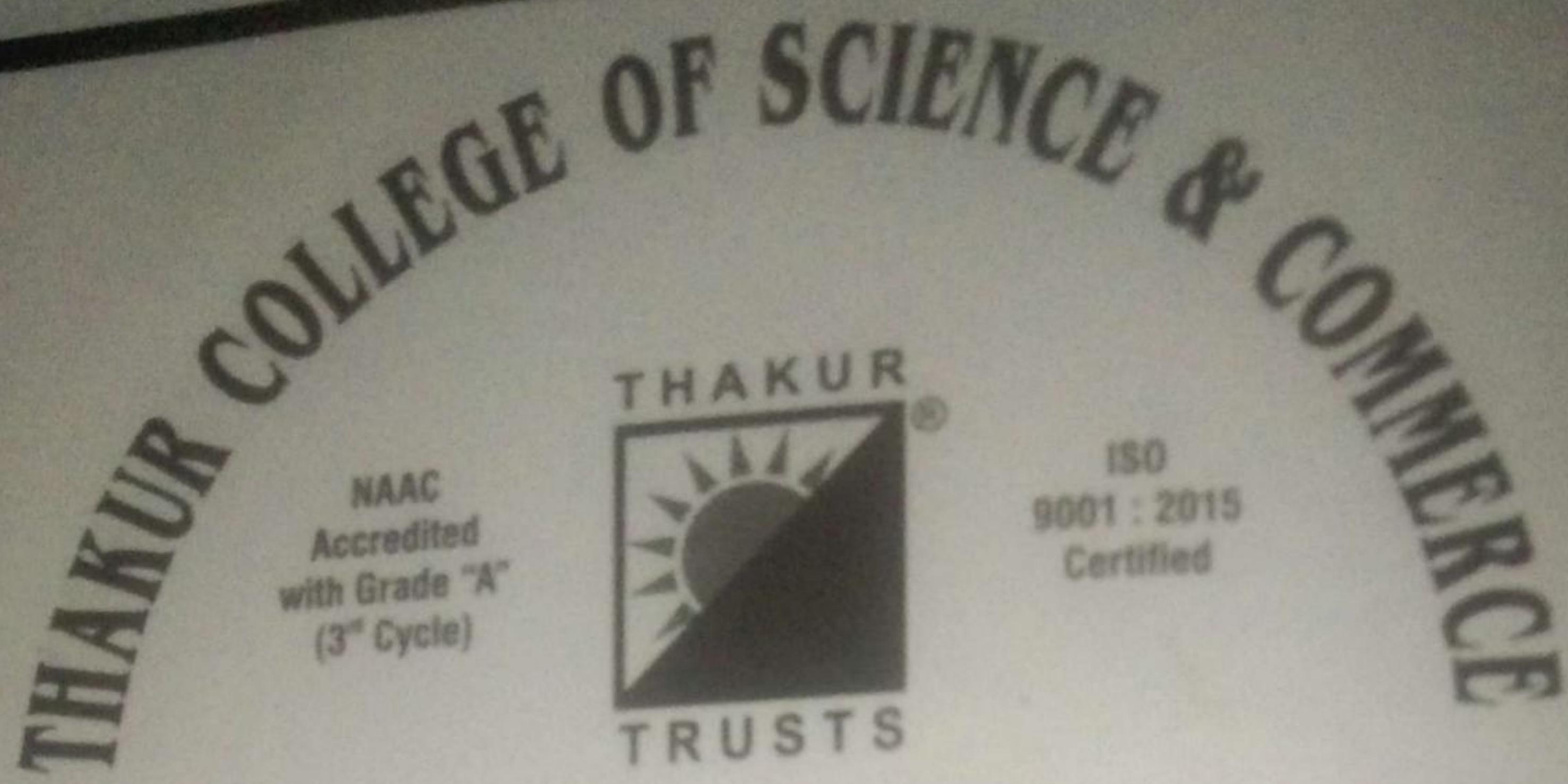


PERFORMANCE

Term	Remarks	Staff Member's Signature
I	Partial	A.W.
II	Complete	G.D.



Degree College
Computer Journal
CERTIFICATE

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Class fy bsc.cs Roll No. 1753 Year 2019-20

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Saw
who has worked for the year 2019- 20 in the Computer
Laboratory.

Teacher In-Charge

Head of Department

Date : _____

Examiner

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PRACTICAL - 01

AIM : Basics of R software

1) R is a software for statistical analysis and data computing.

2) It is an effective data handling software and outcome storage is possible.

3) It is capable of graphical display

4) It is a free software.

Q1 Solve the followings

$$1) 4+6+8 \div 2-5$$

$$> 4+6+8/2-5$$

[1] 9

$$2) 2^2 + [-3] + \sqrt{45}$$

$$> 2^2 + \text{abs}(-3) + \text{sqr}(45)$$

[1] 13.7082

$$3) 5^3 + 7 \times 5 \times 8 + 46/5$$

$$> 5^3 + 7 * 5 * 8 + 46/5$$

[1] 414.2

$$4) \sqrt{4^2 + 5 \times 3 + 7/6}$$

$$> \text{sqr}(4^2 + 5 * 3 + 7/6)$$

[1] 5.671567

6) round off

$46 \div 7 + 9 * 8$

41

> round(46/7 + 9*8)

[1] 79

> c(2,3,5,7)*2
[1] 4 6 10 14

> c(2,3,5,7)*c(2,3)
[1] 4 9 10 21

> c(2,3,5,7)*c(2,3,6,2)
[1] 4 9 30 14

> c(1,6,2,3)*c(-2,-3,-4,-1)
[1] -2 -18 -8 -3

> c(2,3,5,7)^2
[1] 4 9 25 49

> c(4,6,8,9,14,5)^nc(1,2,3)
[1] 4 36 512 9162125

> c(6,2,7,5)/c(4,5)
[1] 1.56 0.40 1.75 1.00

Q3 >x=20 >y=30 >z=2

>x^2+y^3+z

[1] 27402

> sqrt(x^2+y)

[1] 26.73644

>x^z+y^z

[1] 1300

Q4 >x<-matrix(nrow=4, ncol=2, data=c(1,2,3,4,5,6,7,8))

	[,1]	[,2]
[1]	1	5
[2]	2	6
[3]	3	7
[4]	4	8

Q5 Find $x+y$ and $2x+3y$ where $X = \begin{bmatrix} 4 & -2 & 6 \\ 7 & 0 & 7 \\ 9 & -5 & 3 \end{bmatrix}$

$$Y = \begin{bmatrix} 1 & -5 & 7 \\ 12 & -4 & 9 \\ 15 & -6 & 5 \end{bmatrix}$$

> $x <- \text{matrix}(nrow=3, ncol=3, \text{data} = c(4, 7, 9, -2, 0, 7, 15, -5, 6))$

> $x [,1] [,2] [,3]$

[1,]	4	-2	6
[2,]	7	0	7
[3,]	9	-5	3

> $y <- \text{matrix}(nrow=3, ncol=3, \text{data} = c(10, 12, 15, -5, -4, -6, 7, 9, 5))$

> $y [,1] [,2] [,3]$

[1,]	10	-5	7
[2,]	12	-4	9
[3,]	15	6	5

> $x + y$

	[,1]	[,2]	[,3]
[1,]	14	-7	13
[2,]	19	-4	16
[3,]	24	-11	8

> $2*x + 3*y$

	[,1]	[,2]	[,3]
[1,]	38	-19	33
[2,]	50	-12	41
[3,]	63	-28	21

Q6 Marks of statistics of CS Batch A

$x = c(60, 20, 35, 24, 46, 56, 55, 45, 27, 22,$
 $47, 58, 54, 40, 50, 32, 36, 29, 35, 39)$

> $x = c(\text{data})$

> $\text{breaks} = \text{seq}(20, 60, 5)$

> $a = \text{cut}(x, \text{breaks}, \text{right} = \text{FALSE})$

> $b = \text{table}(a)$

> $c = \text{transform}(b)$

> c

	a	Freq
1	[20, 25)	3
2	[25, 30)	2
3	[30, 35)	1
4	[35, 40)	4
5	[40, 45)	1
6	[45, 50]	3
7	[50, 55)	2
8	[55, 60)	4

Q8

TOPIC: Probability distribution

1) Check whether the followings are P.m.f or not.

2	$P(x)$
0	0.1
1	0.2
2	-0.5
3	0.4
4	0.3
5	0.5

If the given data is P.m.f then

$$\sum P(x) = 1$$

$$\begin{aligned} \therefore P(0) + P(1) + P(2) + P(3) + P(4) + P(5) &= P(x) \\ &= 0.1 + 0.2 - 0.5 + 0.4 + 0.3 + 0.5 \\ &= 1.0 \end{aligned}$$

$\therefore P(2) = -0.5$, it can't be a
 \therefore Probability mass function
 $\therefore P(x) \geq 0 \forall x$

2)	x	$P(x)$
	1	0.2
	2	0.2
	3	0.3
	4	0.2
	5	0.2

The condition for p.m.f is $\sum P(x) = 1$

so,

$$\begin{aligned}\sum P(x) &= P(1) + P(2) + P(3) + P(4) + P(5) \\ &= 0.2 + 0.2 + 0.3 + 0.2 + 0.2 \\ &= 1.1\end{aligned}$$

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\therefore The given data is not a pmf because the $P(x) \neq 1$

3) x $P(x)$

10 0.2

20 0.2

30 0.35

40 0.15

50 0.1

The condition for P.m.f is

i) $P(x) \geq 0 \quad \forall x$ satisfy

$$\begin{aligned}\sum P(x) &= P(10) + P(20) + P(30) + P(40) + P(50) \\ &= 0.2 + 0.2 + 0.35 + 0.15 + 0.1 \\ &= 1\end{aligned}$$

\therefore The given data is P.m.f

Code:

> Prob = c(0.2, 0.2, 0.35, 0.15, 0.1)

> sum(Prob)

[1] 1

Q2 Find the c.d.f for the following P.m.f and sketch the graph.

x 10 20 30 40 50

$P(x)$ 0.2 0.2 0.35 0.15 0.1

$$F(x) = 0 \quad \text{for } x < 10$$

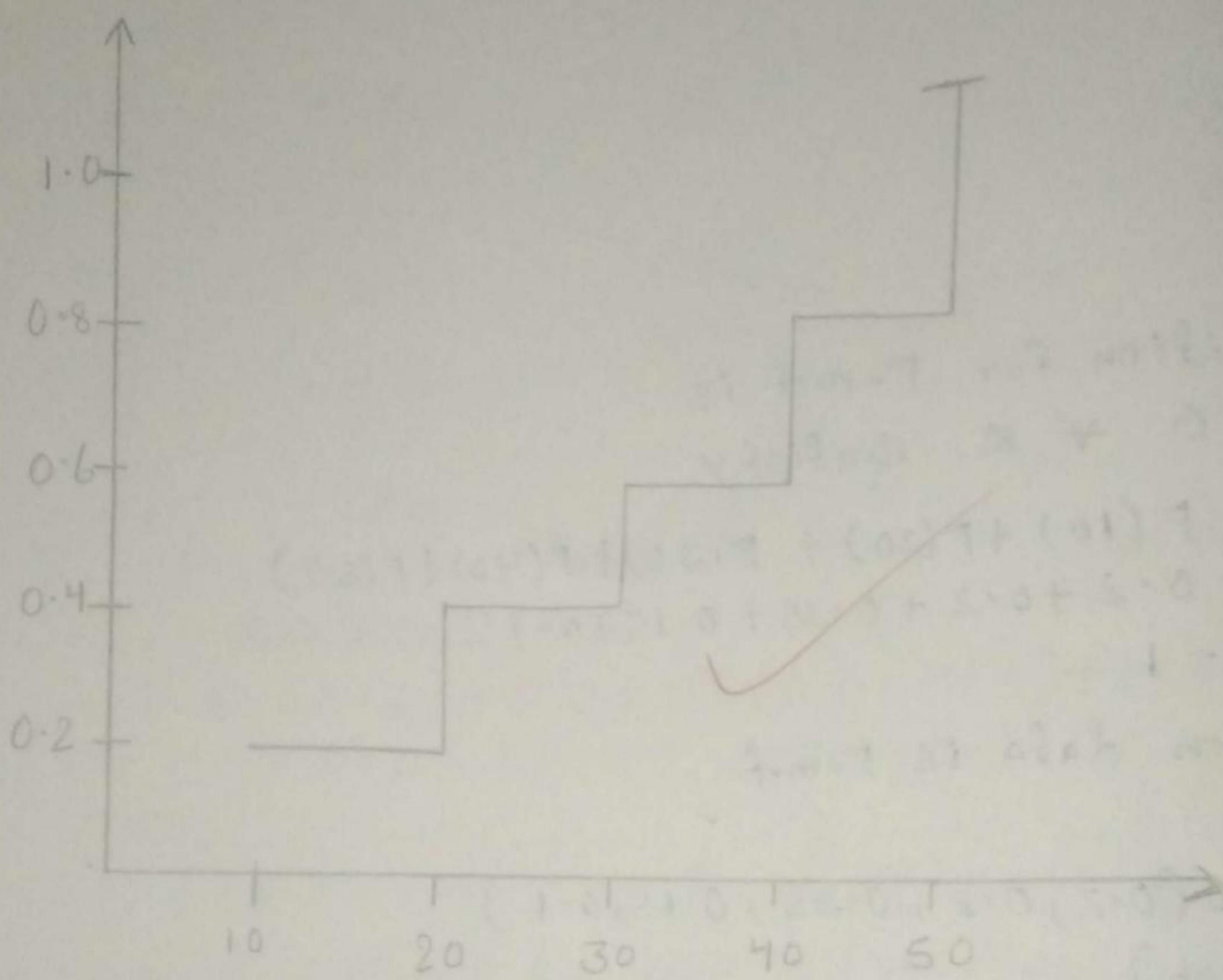
$$0.2 \quad 10 \leq x < 20$$

$$0.4 \quad 20 \leq x < 30$$

$$0.75 \quad 30 \leq x < 40$$

$$0.90 \quad 40 \leq x < 50$$

$$1.0 \quad x \geq 50$$



> $x = c(10, 20, 30, 40, 50)$

> $\text{plot}(x, \text{cumsum}(\text{prob}), \text{"s"})$

Q2 Find

x	1	2	3	4	5	6
$P(x)$	0.15	0.25	0.1	0.2	0.2	0.1

$$\begin{aligned}
 F(x) &= 0 & x < 1 \\
 &= 0.15 & 1 \leq x < 2 \\
 &= 0.40 & 2 \leq x < 3 \\
 &= 0.50 & 3 \leq x < 4 \\
 &= 0.70 & 4 \leq x < 5 \\
 &= 0.90 & 5 \leq x < 6 \\
 &= 1.00 & x \geq 6
 \end{aligned}$$

> Prob = c(0.15, 0.25, 0.1, 0.2, 0.2, 0.1)

> sum(Prob)

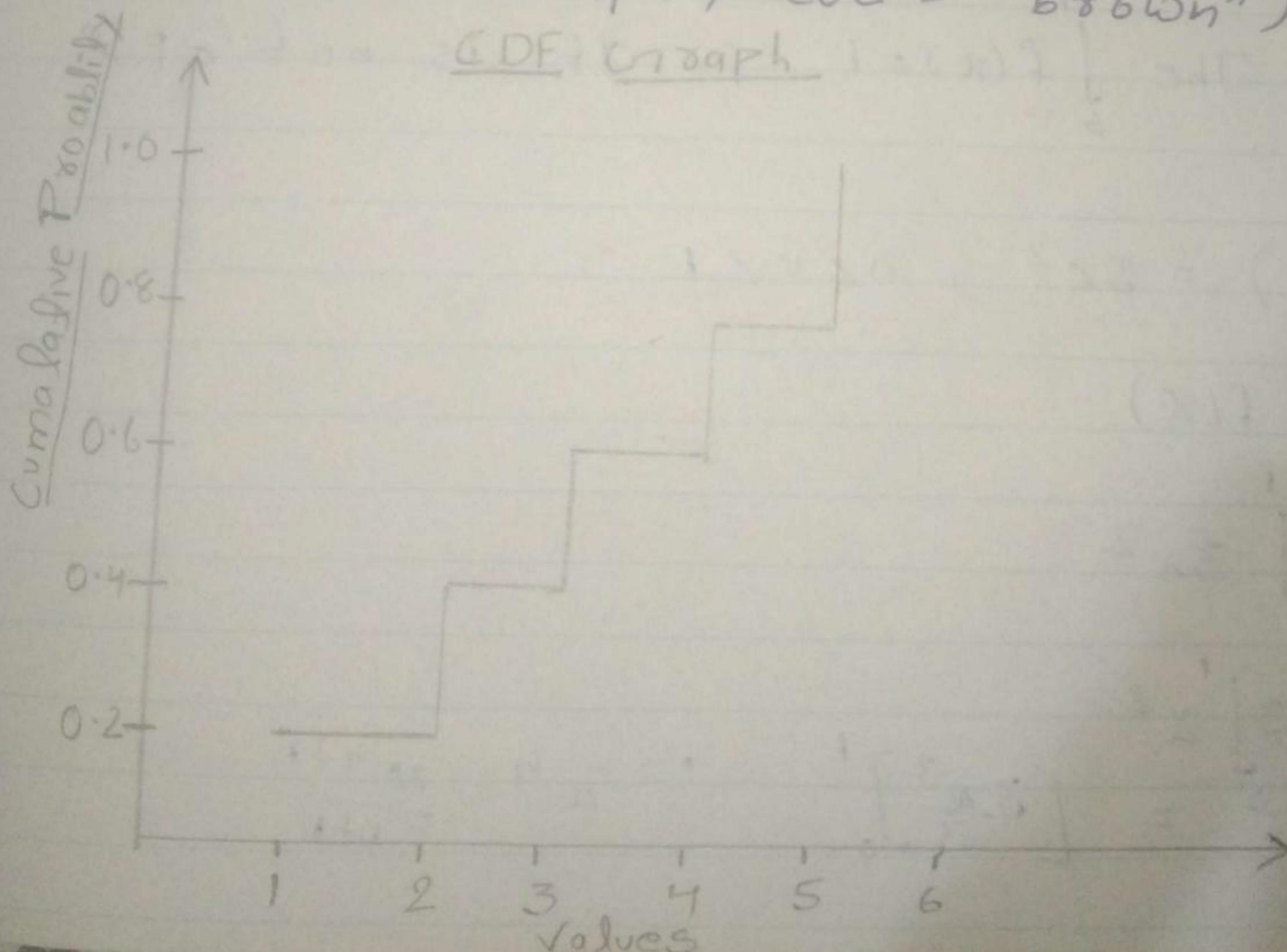
[1] 1

> cumsum(Prob)

[1] 0.15, 0.40, 0.50, 0.70, 0.90, 1.00

> x = c(1, 2, 3, 4, 5, 6)

> Plot(x, cumsum(Prob), "s", xlab = "value",
 ylab = "Cumulative Probability",
 main = "CDF Graph", col = "brown")



• Ques

Q3 Check that whether the following is P.d.f or not

$$(i) f(x) = 3-2x ; 0 \leq x \leq 1$$

$$(ii) f(x) = 3x^2 ; 0 < x < 1$$

$$(i) f(x) = 3-2x$$
$$\rightarrow \int_0^1 f(x) dx$$

$$= \int_0^1 (3-2x) dx$$

$$= \int_0^1 3 dx = \int_0^1 2x dx$$

$$= [3x - x^2]_0^1 = 2$$

\therefore The $\int_0^1 f(x) dx = 1 \therefore$ It is not a PDF

$$2) f(x) = 3x^2 ; 0 < x < 1$$

$$\int_0^1 f(x) dx$$

$$= \int_0^1 3x^2 dx$$

$$= 3 \int_0^1 x^2 dx$$

$$= \left[3 \frac{x^3}{3} \right]_0^1 \quad \because x^n = \frac{x^{n+1}}{n+1}$$

$$= ue^3$$

$$= 1$$

$$\int_0^1 f(u) = 1 \quad \therefore f \text{ is a pdf.}$$

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PRACTICAL-03

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TOPIC: Binomial distribution

$$\# P(X=20) = \text{dbinom}(20, n, P)$$

$$\# P(X \leq 20) = \text{Pbinom}(20, n, P)$$

$$\# P(X > 20) = 1 - \text{Pbinom}(20, n, P)$$

If 20 is Unknown

$$P_1 = P(X \leq 20) = \text{qbinom}(P_1, n, P)$$

- 1) Find the Probability of exactly 10 success in hundred trials with $P=0.1$.
- 2) Suppose there are 12 mcq, Each question has 5 options out of which 1 is correct. Find the Probability of having exactly 4 correct answers.
 - i) Atmost 4 correct answers
 - ii) More than 5 correct answers
- 3) Find the Complete distribution when $n=5$ and $P=0.1$.
- 4) $n=12$, $P=0.25$, find the following Probabilities.
 - i) $P(X=5)$
 - ii) $P(X \leq 5)$
 - iii) $P(X > 7)$
 - iv) $P(5 < X < 7)$

$\Rightarrow x = \text{dbinom}(10, 100, 0.1)$

$> x$

[I] 0.1318653

Q3 3/ $> \text{dbinom}(4, 12, 0.2)$

[I] 0.1328756

"> $\text{Pbinom}(4, 12, 0.2)$

[I] 0.927445

""> $1 - \text{Pbinom}(5, 15, 0.2)$

[I] 0.01940528

4/ $\text{dbinom}(0:5, 5, 0.1)$

0 - 0.59049

1 - 0.32805

2 - 0.07290

3 - 0.00810

4 - 0.00045

5 - 0.00001

4/ $> \text{dbinom}(5, 12, 0.25)$

[I] 0.1032414

2> $\text{Pbinom}(5, 12, 0.25)$

[I] 0.9455978

3> $1 - \text{Pbinom}(7, 12, 0.25)$

[I] 0.00278151

4> $\text{dbinom}(6, 12, 0.25)$

[I] 0.04014945

(S)

- Q: 5) The Probability of a salesman making a sale to customer is 0.15. Find the Probability of
i) No sales out of 10 customers
ii) More than 3 sales out of 20 customers

(i) 6) A sales man has 20% probability of making a sale to customer out of 30 customers. What minimum number of sales he can make with 88% of probability.

7) X follows binomial distribution with $n=10$, $P=0.3$. Plot the graph of P.m.f and C.d.f.

> dbinom(0, 10, 0.15)
 // [1] 0.1968744

> 1 - Pbinom(3, 20, 0.15)
 // [1] 0.3522748

> qbinom(0.88, 30, 0.2)
 // [1] 9

> n = 10
 > P = 0.3
 > x = 0:n
 > Prob = dbinom(x, n, P)

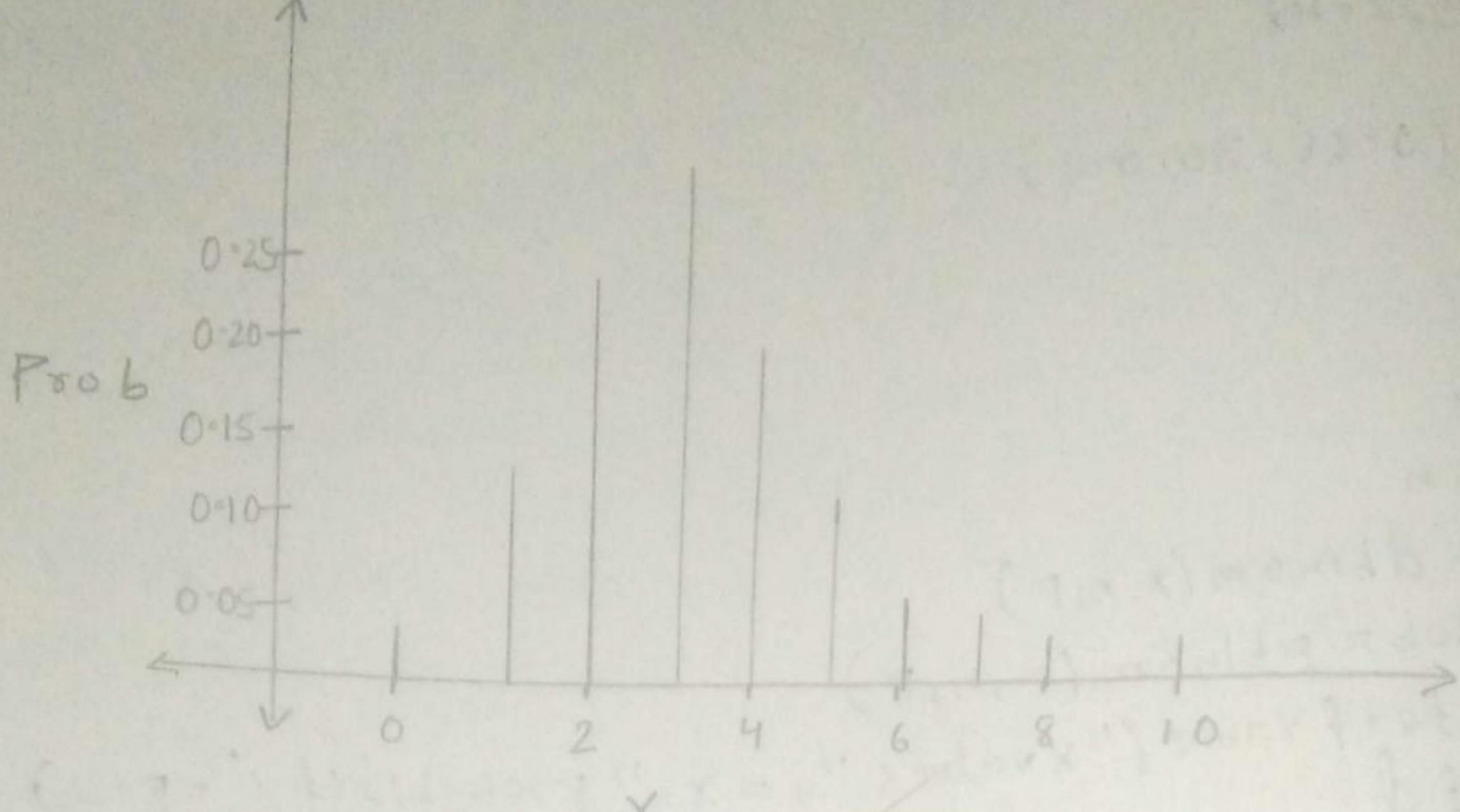
> CumProb = Pbinom(x, n, P)

> d = data.frame("xvalues" = x, "Probability" = Prob)
 > Print(d)

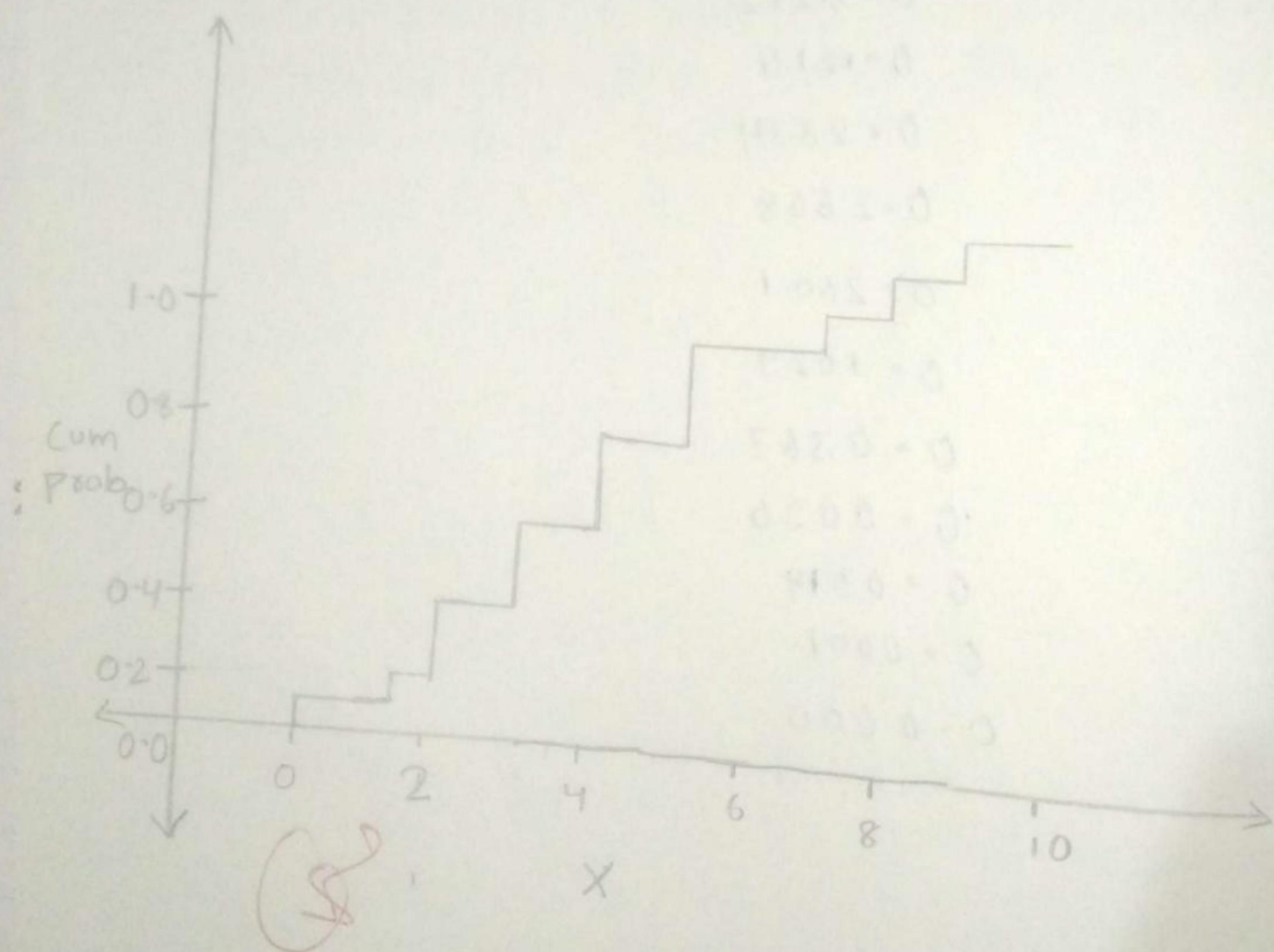
	xvalues	Probability
1	0	0.0282
2	1	0.1210
3	2	0.2334
4	3	0.2668
5	4	0.2001
6	5	0.1029
7	6	0.0367
8	7	0.0090
9	8	0.0014
10	9	0.0001
11	10	0.0000

$\rightarrow \text{Plot}(x, \text{Prob}, "h")$

Q3



$\rightarrow \text{Plot}(x, \text{cumprob}, "s")$



PRACTICAL-04

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AIM: Normal Distribution

$$(i) P(X = 20) = dnorm(20, \mu, \sigma)$$

$$(ii) P(X \leq 20) = pnorm(20, \mu, \sigma)$$

$$(iii) P(X > 20) = 1 - pnorm(20, \mu, \sigma)$$

To generate random numbers from a normal distribution (n, random numbers) the R code `rnorm(n, \mu, \sigma)`.

A random variable X follows normal distribution with Mean = $\mu = 12$ and $S.D = \sigma = 3$. Find

$$(i) P(X \leq 15) \quad (ii) P(10 \leq X \leq 13) \quad (iii) P(X > 14)$$

(iv) Generate 5 observations (random numbers)

```
> p1 = pnorm(15, 12, 3)
```

```
> p1
```

```
[1] 0.8413447
```

```
> cat("P(X <= 15) = ", p1)
```

```
P(X <= 15) = 0.8413447
```

```
> p2 = pnorm(13, 12, 3) - pnorm(10, 12, 3)
```

```
> p2
```

```
[1] 0.3780661
```

```
> cat("P(10 <= X <= 13) = ", p2)
```

```
P(10 <= X <= 13) = 0.3780661
```

```
> p3 = 1 - pnorm(14, 12, 3)
```

```
> p3
```

```
[1] 0.2524925
```

```

> cat("P(x>14) = ", P^3)
P(x>14) = 0.2524925
> P^4 = rnorm(5, 12, 3)
> P^4
[1] 15.254723 16.648505 11.280515 6.419944
[2] 12.272460

```

- Q2. x follows normal distribution with $\mu = 10, \sigma = 2$. Find (i) $P(x \leq 7)$
(ii) $P(5 < x < 12)$ (iii) $P(x > 12)$
(iv) Generate 10 observations
(v) Find K such that $P(x < K) = 0.4$

```
> q1 = rnorm(7, 10, 2)
```

```
> q1
```

```
[1] 0.6668072
```

```
> q2 = rnorm(5, 10, 2) - rnorm(12, 10, 2)
```

```
> q2
```

```
[1] -0.8351351
```

```
> q3 = 1 - rnorm(12, 10, 2)
```

```
> q3
```

```
[1] 0.1586553
```

```
> q4 = rnorm(10, 10, 2)
```

```
> q4
```

```
[1] 11.608931 9.920417 12.637741
[2] 8.673354 8.721380 8.193726
[3] 9.366824 11.707106 9.537584
[4] 10.715006
```

> a5 = rnorm(0.4, 10, 2)

> a5

[1] 9.493306

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Q3 Generate 5 random numbers from a normal distribution $\mu = 15$, $\sigma = 4$. Find Sample Mean, Median, S.D and print it.

> > rnorm(5, 15, 4)

[1] 10.7649 7.793249 9.953444 13.345900
17.509668

> am = mean(z)

> am

[1] 11.87345

> cat("Sample mean is = ", am)

Sample mean is = 11.87345

> me = median(z)

> me

[1] 10.76499

> cat("Median is = ", me)

Median is = 10.76499

> n = 5

> v = (n - 1) * var(z) / n

> v

[1] 11.09965

> sd = sqrt(v)

> sd

[1] 3.331613

> cat("SD is = ", sd)

S.D is = 3.331613

Q4 $X \sim N(30, 100)$, $\sigma = 10$

(i) $P(X \leq 40)$

(ii) $P(X > 35)$

(iii) $P(25 < X < 35)$

(iv) Find k such that $P(X < k) = 0.6$

> f1 = pnorm(40, 30, 10)

> f1

[1] 0.8413447

> f2 = 1 - pnorm(35, 30, 10)

> f2

[1] 0.3085375

> f3 = pnorm(25, 30, 10) - pnorm(35, 30, 10)

> f3

[1] -0.3829249

> f4 = qnorm(0.6, 30, 10)

> f4

[1] 32.53347

Q5 Plot the standard normal graph.

> z = seq(-3, 3, by = 0.1)

> y = dnorm(z)

> plot(z, y, xlab = "X values", ylab = "Probability",
main = "standard normal graph")

Q5

Q2

Practical-05

Aim: Normal & T-test

Q1 Test the Hypothesis $H_0: \mu = 15$, $H_1: \mu \neq 15$
Random sample of size 400 is drawn
and it is calculated the sample
mean is 14 and the standard
deviation is 3. Test the hypothesis
at 5% level of significance.

Soln:- $> m_0 = 15$

$> m_x = 14$

$> s_d = 3$

$> n = 400$

$> z_{\text{cal}} = (m_x - m_0) / (s_d / (\sqrt{n}))$

$> z_{\text{cal}}$

[1] -6.666667

$> \text{cat}(" \text{calculate value at } 2 \text{ is } =,")$

calculate value at 2 is = ,

$> \text{cat}(" \text{calculate value at } z \text{ is } = ", z_{\text{cal}})$

calculate value at z is = -6.666667

$> p_{\text{value}} = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$

$> p_{\text{value}}$

[1] 2.616796e-11

Since P value is less than 0.05 we Reject $H_0: \mu = 15$

Q2

Test the Hypothesis is $H_0: \mu = 10$?
 $H_1: \mu \neq 10$ Random Sample of

size 400 is drawn with sample of size mean 10.2 and standard deviation 2.25. Test the hypothesis at 5% level of significance.

In:- > $m_0 = 10$

> $m_x = 10.2$

> $s_d = 2.25$

> $n = 400$

> $z_{\text{cal}} = (m_x - m_0) / (s_d / (\sqrt{n}))$

> z_{cal}

[1] 1.777778

> cat("Calculate value of z is =", z_{cal})

calculate value of z is = 1.777778

> pvalue = 2 * (1 - pnorm(abs(z_{cal})))

> pvalue

[1] 0.07544036

Q3 Test the Hypothesis H_0 proportion of smokers in a college is 0.2 a sample is collected and sample proportion is calculated as 0.125. Test the hypothesis at 5% level of significance (sample size = 400).

In:- $P \rightarrow \text{population}$

$p \rightarrow \text{sample}$

> $P = 0.2$

> $p = 0.125$

> $n = 400$

> $Q = 1 - P$

> $z_{\text{cal}} = (p - P) / (\sqrt{P * Q / n})$

> z_{cal}

[1] -3.075

~~Q4~~ Last year Farmers lost 20% of their crop's a Random sample of 60 fields collected. If will found that 9 field crops are insect populated. Test the hypothesis at 1% level of significance.

$$P = 0.2 \text{ (capital)}$$

$$P = 9/60$$

$$\rightarrow > P = 0.2$$

$$> P = 9/60$$

$$> n = 60$$

$$> z_{\text{cal}} = (P - p) / (\sqrt{p * (1-p) / n})$$

$$> z_{\text{cal}}$$

$$[1] - 0.9682458$$

$$> P\text{value} = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$$

$$> P\text{value}$$

$$[1] 0.3329216$$

\therefore The value is 0.1 so value is accepted.

~~Q5~~ Test the hypothesis $H_0: \mu = 12.5$ from the following sample at 5% level of significance

$$> x = c(12.25, 11.97, 12.15, 12.08, 12.31, 12.28, 11.94, 11.89, 12.16, 12.04)$$

$$> n = \text{Length}(x)$$

$$> \bar{x} = \text{mean}(x)$$

$$> mx$$

$$[1] 12.107$$

```

> variance = (n-1) * var(x) / n
> variance
[1] 0.019521
> sd = sqrt(variance)
> sd
[1] 0.1397176
> mo = 12.5
> t = (mx - mo) / (sd / sqrt(n))
> t
[1] -8.894909
> pvalue = 2 * (1 - pnorm(abs(t)))
> pvalue
[1] 0

```

\therefore The value is less than 0.05 the value is accepted.

Q8

Practical - 06

Aim: Large sample test

Q1 Let the population mean (the amount spent by customer in a Restaurant) is 250^{mo} . A sample of 100 customers selected. Sample mean is calculated as 275^{mx} and SD as 30 . Test the hypothesis that population mean is 250 or not at 5% level of significance.

Soln:-
 $H_0: \mu = 275$ against $H_1: \mu \neq 275$
 $> m_0 = 250$
 $> m_x = 275$
 $> n = 100$
 $> sd = 30$
 $> z_{\text{cal}} = (m_x - m_0) / (sd / \sqrt{n})$
 $> z_{\text{cal}}$
 $> [1] 8.333333$

$> \text{Pvalue} = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$
 $> \text{Pvalue}$
 $[1] 0$
 $> \text{cat}("z_{\text{cal}}:", z_{\text{cal}})$
 $> z_{\text{cal}}: 8.333333$
 $> \text{cat}("Pvalue:", Pvalue)$
 $> Pvalue: 0$

$\therefore \text{Pvalue} = 0 < 0.05$ we reject H_0 at 5% level of significance.

Q2 In a Random sample of 1000 students it is found that 750 use blue ⁵⁴ pen. Test the hypothesis that population proportion is 0.8 at 1% level of significance.

```

Sln:-  $H_0: P = 0.8$  against  $H_1: P \neq 0.8$ 
> P = 0.8
> Q = 1 - P
> P = 750 / 1000
> n = 1000
> zcal = (P - P) / (sqrt(P * Q / n))
> zcal
> [1] -3.952847
> pvalue = 2 * (1 - pnorm(abs(zcal)))
> pvalue
> [1] 7.2268e-05

```

\therefore The value is less than 0.01 we reject.

Q3 Two Random Sample of size 1000 & 2000 are drawn from two population with the same $\sigma^2 = 2.5$. The sample means are 67.5 & 68 respectively. Test the hypothesis $H_0: \mu_1 = \mu_2$ against $H_1: \mu_1 \neq \mu_2$ at 5% level of significance.

```

Sln:-  $H_0: \mu_1 = \mu_2$  as  $H_1: \mu_1 \neq \mu_2$ 
> n1 = 1000

```

```

>n2=2000
>mx1=67.5
>mx2=68
>sdi=2.5
>sd2=2.5
>zcal=(mx1-mx2)/sqrt(((sdi^2/n1)+(sd2^2/n2)))
>zcal
>[1]-5.163978
>cat("zcal:",zcal)
>zcal:-5.163978
>pvalue=2*(1-pnorm(abs(zcal)))
>pvalue((2.025)2dp)on0.97-1)*s=solve
>[1]2.417564e-07
∴ Rejected.

```

Q4 The study of Noise Level in two Hospitals is given below. Test the claim that the two Hospital Have same Level of Noise at one (1%) level of significance.

	Hospital A	Hospital B
Size	84	84
Mean	61.2	59.4
S.D	7.9	7.5

```

> n1 = 84
> n2 = 34
> mx1 = 61.2
> mx2 = 59.4
> sd1 = 7.9
> sd2 = 7.5
> zcal = (mx1 - mx2) / sqrt((sd1^2/n1) +
  & (sd2^2/n2))
> zcal
[1] 1.162528
> cat("zcal =", zcal)
zcal = 1.162528
> Pvalue = 2 * (1 - pnorm(abs(zcal)))
> Pvalue
[1] 0.2450211
> cat("Pvalue =", Pvalue)
> Pvalue

```

\therefore The value is greater than 0.01
we accept the values.

In A sample of 600 students in a college 400 use Blue ink in Another college from a sample of 900 students 450 use Blue ink. Test the Hypothesis that the proportion of students using blue ink in two colleges are equal or not. At 1% level of significance.

~~H0~~ \rightarrow H0

$$> n_1 = 600$$

$$> n_2 = 900$$

$$> P_1 = 400/600$$

$$> P_2 = 450/900$$

$$> z_{\text{cal}} = \frac{(P_1 - P_2)}{\sqrt{P_1(1-P_1)/n_1 + P_2(1-P_2)/n_2}}$$

$$> z_{\text{cal}}$$

$$[1] 6.381534$$

$$> P_{\text{value}} = 2 * (1 - pnorm(\text{abs}(z_{\text{cal}})))$$

$$> P_{\text{value}}$$

$$[1] 1.753222e-10$$

\therefore value is less than 0.01 the value is rejected.

~~H0~~ First sample size.

$$n_1 = 200$$

$$n_2 = 200$$

$$P_1 = 44/200$$

$$P_2 = 30/200$$

$\rightarrow H_0: P_1 = P_2$ as $H_1: P_1 \neq P_2$

$$n_1 = 200$$

$$n_2 = 200$$

$$P_1 = 44/200$$

$$P_2 = 30/200$$

$$P = \left(\frac{n_1 * P_1 + n_2 * P_2}{n_1 + n_2} \right) \left(\frac{1}{n_1 + n_2} \right)$$

$$q = 1 - P$$

$$z_{\text{cal}}^2 = (P_2 - P_1) / \sqrt{q} \cdot \left(P \cdot q \cdot \left(\frac{1}{n_1} + \frac{1}{n_2} \right) \right)$$

$$z_{\text{cal}}^2$$

[1] 1.802741

$$p\text{value} = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$$

$$p\text{value}$$

[1] 0.07142888

∴ Accept greater than 0.05.

Q9

Practical-07

Topic: Small Sample test

- Q1 The marks of 10 students are given by
 63, 63, 66, 67, 68, 69, 70, 71, 72. Test the hypothesis that the sample comes from the population with average 66.

$$\rightarrow H_0: \mu = 66$$

$$> z_e = c(66, 63, 66, 67, 68, 69, 70, 71, 72)$$

$$> t\text{-test}(z_e)$$

One Sample t-test

data: x

$$t = -72.125, df = 8, p\text{-value} = 1.521e-12$$

alternative hypothesis: true mean is not equal to 0.

95 percent confidence interval:

$$65.82588 \quad 70.17412$$

Sample estimates:

mean of x

68

\therefore The value is less than 0.05 we reject the hypothesis at 5% Level of significance.

- Q2 Two groups of student scored the following marks. Test the hypothesis that there is no significance difference b/w the 2 groups.

GR1 = 18, 22, 21, 17, 20, 17, 23, 20, 22, 21

GR2 = 16, 20, 14, 21, 20, 18, 13, 15, 17, 21

H₀: There is no difference b/w the 2 groups.

> x = c(18, 22, 21, 17, 20, 17, 23, 20, 22, 21)
 > y = c(16, 20, 14, 21, 20, 18, 13, 15, 17, 21)
 > t.test(x, y)

Welch Two Sample t-test

data : x and y

t = 2.2573, df = 16.376, P-value = 0.03798
 alternative hypothesis: true difference in means is not equal to 0.

95 percent confidence interval:

0.1628205 5.0371795

sample estimates:

mean of x mean of y

20.1 17.5

> P-value = 0.03798

> if (Pvalue > 0.05) { cat("accept H₀") }
 else { cat("reject H₀") }

reject H₀

(PAIRED-T-Test)

3) The sales data of 86 shops before & after a special campaign are given below

Before : 53, 28, 31, 48, 50, 42

After : 58, 29, 30, 55, 56, 45

Test the hypothesis that the campaign is effective or not.

H₀ : There is no significance difference of sales before & after campaign.

→ > x = c(Before)

> y = c(After)

> t.test(x, y, paired = T, alternative = "greater")

Paired t-test

data : x & y

t = -2.7815, df = 5, p-value = 0.9806

alternative hypothesis.

The difference in means is greater than 0.

95 Percent Confidence interval:

-6.035547 inf

Sample estimates

means of the difference
- 3.5

58

∴ P-value is greater than 0.05, we accept
the hypothesis at 5% Level of significance.

Following are the weights before & after
the diet program. Is the diet program
effective?

Before : 126, 125, 115, 130, 123, 119

After : 100, 114, 95, 90, 115, 99

H₀ :- There is no significant difference

> x = c(Before)

> y = c(After)

> t.test(x, y) paired = T, alternative = "less"
Paired t-test

data: x & y

t = 4.3458, df = 5, pvalue = 0.9963

alternative hypothesis: true difference
in means is less than 0.

95 percent confidence interval:

- Inf 29.0295

Sample estimates:

mean of the differences

19.83333

∴ P-value is greater than 0.05 we accept
the hypothesis at 5% Level of significance.

Q5 2 medianis are applied to two groups of patient respectively.

group1: 10, 12, 13, 11, 14

group2: 8, 9, 12, 14, 15, 10, 9

Is there any significance difference b/w 2 medicines.

H0: There is no significance difference.

```
> x = c(group1)
```

```
> y = c(group2)
```

```
> t.test(x, y)
```

data: x & y

t = 0.80384, df = 9.7594, Pvalue = 0.4406

alternative hypothesis: true difference in means is not equal to 0.

95 percent confidence interval

- 0.9698553 4.2981886

Sample estimates:

mean of x mean of y
12.0000 10.3333

∴ Pvalue is greater than 0.05 we accept the hypothesis at 5% level of significance

(S)

Aim: Large and Small Test

Q1: H_0 : The arithmetic mean of a sample of 100 items from a large population is 52. If the standard deviation is 7, test the hypothesis that the population mean is 55 against the alternative hypothesis that it is more than 55 at 5% LOS.

Sol: $H_0 : \mu = 55$, $H_1 : \mu \neq 55$

> n = 100

> m2e = 52

> mo = 55

> sd = 7

> zcal = $(m2e - mo) / (sd / \sqrt{n})$

> zcal

[1] -4.285714

> Pvalue = $2 * (1 - pnorm(\text{abs}(zcal)))$

> Pvalue

[1] 1.82153e-05 ✓

As value is less than 0.05 we reject H_0 at 5% level of significance.

Q2: In a big city 350 out of 700 males are found to be smokers. Does the information supports

Q3
Is exactly half of the males in the city are smokers?
Test at 1% LOS.

$$\rightarrow H_0: p = 0.5 \text{ against } H_a: p \neq 0.5$$

$$> p = 0.5$$

$$> q = 1-p$$

$$> n = 100$$

$$> z_{\text{cal}} = (p - P) / (\sqrt{p(1-p)/n})$$

$$> z_{\text{cal}}$$

[1] 0

$$> p\text{value} = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$$

> pvalue

[1]

As pvalue is greater than 0.05 we accept H_0 at 1% level of significance.

Q3
Thousands articles from a factory : A are found to have 2% defectives, 1506 articles from a 2nd factory B are found to have 1% defective. Test at 5% LOS that the two factory are similar or are not.

Sohit: $H_0: p_1 = p_2$ against $H_a: p_1 \neq p_2$

$$\geq n_1 = 1000$$
$$> n_2 = 1500$$

```

> P1 = 2 / 1000
> P2 = 1 / 1500
> P = (n1 * P1 + n2 * P2) / (n1 + n2)      60
> P
[1] 0.0012
> q = 1 - P
[1] 0.9988
> zcal = (P1 - P2) / sqrt(P * q * (1/n1 + 1/n2))
> zcal
[1] 0.9433752
> pvalue = 2 * (1 - pnorm(abs(zcal)))
> pvalue
[1] 0.345489

```

\therefore pvalue is greater than 0.05 use accept H_0 and 5% level of significance.

Q A sample of size 400 was drawn at a sample mean is 99. Test at 5% LOS that the sample comes from a population with mean 100 and variance 64.

H₀: $H_0: \mu = 100$ against $H_1: \mu \neq 100$

```

> var = 64
> n = 400
> m0 = 100
> mx = 99
> sd = sqrt(var)
> sd
[1] 8

```

```

>zcal = (m1-m0) / (sd / sqrt(n)))
>zcal
>zcal = (m2-m0) / (sd / sqrt(n)))
>zcal
[1] 2.5
>pvalue = 2 * (1 - pnorm(abs(zcal)))
>pvalue
[1] 0.01241933

```

Since pvalue is less than 0.05 we reject H_0 at 5% level of significance.

Q5 The Flower stems are selected and the heights are found to be (cm) 63, 63, 68, 69, 71, 71, 72 test the hypothesis that the mean height is 66 or not at 1% LOS.

Sol:- $H_0: \mu = 66$ against $H_1: \mu \neq 66$

```

> zl = c(63, 63, 68, 69, 71, 71, 72)
> t.test(zl)

```

One sample t-test

data: zl

$t = 47.94$, $df = 6$, $p\text{-value} = 5.522e-09$

alternative hypothesis: true mean is not equal to 0.

95 percent confidence interval.

64.66479 71.62092

Sample estimates:

mean of zl

68.14286

since P value is less than 0.05 we reject H_0 at 5% Level of significance.

Two random samples were drawn from 2 normal populations and their values are A: 66, 67, 75, 76, 82, 84, 88, 90, 92 B: 64, 66, 74, 78, 82, 85, 87, 92, 93, 95, 97.

Test whether the population have the same variance at 5%. LOSR - II : 0.1

$H_0: \sigma_1^2 = \sigma_2^2$ against $H_1: \sigma_1^2 \neq \sigma_2^2$

$> x = c(66, 67, 75, 76, 82, 84, 88, 90, 92)$

$> y = c(64, 66, 74, 78, 82, 85, 87, 92, 93, 95, 97)$

$> var.test(x, y)$

F test to compare two variances
data: x and y

F = 0.788803, num df = 7, denom df = 10,

pvalue = 0.7737

alternative hypothesis: true ratio of variances is not equal to 1.

95 percent confidence interval:

0.199509 3.751881

Sample estimates:

ratio of variances

0.7880255

P-Value is greater than 0.05 we accept H_0 at 5% level of significance.

12

A company producing light bulbs find that mean life span of the population of bulbs is 1200 hours with s.d 125. A sample of 100 bulbs have mean 1150 hours. Test whether the population have difference between population and sample mean is significantly different?

→ $H_0: \mu = 1150$ against $H_1: \mu \neq 1150$
> n = 100
> m₀ = 1150
> m₀ = 1200
> sd = 125
> zcal = $(m - m_0) / (sd / (\sqrt{n}))$
> zcal
[1] -4
> pvalue = 2 * (1 - pnorm(abs(zcal)))
> pvalue
[1] 6.334248e-05
∴ pvalue is less than 0.05 we reject H_0 .

From each of two consignments of apples, a sample of size 200 is drawn and number of bad apples are counted. Test whether the proportion of rotten apples

in two assignments are significantly different
at 1% LOS?

62

Consignment	Sample size	No. of bad apples
1	200	44
2	300	56

$H_0: P_1 = P_2$ against: $P_1 \neq P_2$

$$> n_1 = 200$$

$$> n_2 = 300$$

$$> P_1 = 44/200$$

$$> P_2 = 56/300$$

$$> P = (n_1 * P_1 + n_2 * P_2) / (n_1 + n_2)$$

$$> P$$

$$[1] 0.2$$

$$> q = 1 - P$$

$$[1] 0.8$$

$$> z_{cal} = (P_1 - P_2) / \sqrt{P * q * (1/n_1 + 1/n_2)}$$

$$> z_{cal}$$

$$[1] 0.9128709$$

$$> pvalue = 2 * (1 - pnorm(abs(z_{cal})))$$

$$> pvalue$$

$$[1] 0.8618104$$

∴ Pvalue is greater than 0.05 we accept H_0
at 1% Level of Significance.

Q

TOPIC: Non-Parametric Testing of Hypothesis Using R-Environment.

Q: The following data represent earnings (in dollars) for a random sample of five common stocks listed on the New York Stock Exchange. Test whether median earnings is 4 dollars.

Data = 1.68, 3.35, 2.50, 6.23, 3.24

```
> x <- c(1.68, 3.35, 2.50, 6.23, 3.24);
```

```
> n <- length(x);
```

```
> n
```

```
[1] 5
```

```
> x > 4;
```

```
[1] FALSE FALSE FALSE TRUE FALSE
```

```
> s <- sum(x > 4); s
```

```
[1] 1
```

```
> binom.test(s, n, p = 0.5, alternative = "greater");
```

Exact binomial test

data: s and n

number of successes = 1, number of trials = 5, p-value = 0.96

alternative hypothesis: true probability of series is greater than 0.5,

95 percent confidence interval:

0.01020622 100000000

Sample estimates:

Probability of success 0.2

- ② The scores of 8 students in reading before and after lesson are as follows:
Test whether there is effect of reading

Student NO:	1	2	3	4	5	6	7	8
Score before:	10	15	16	12	09	07	11	12
Score After:	13	16	15	13	09	10	13	10

CODE:

```
> b <- c(10, 15, 16, 12, 09, 07, 11, 12);  
> a <- c(13, 16, 15, 13, 08, 10, 13, 10);  
> D <- b - a;  
  
> wilcox.test(D, alternative = "greater");
```

Wilcox signed rank test with
continuity correction data: D
 $N = 10.5$, p-value = 0.8722
alternative hypothesis: true location is
greater than 0

Warning message:

In `wilcox.test.default(D, alternative = "greater")`

cannot compute exact P-value with ties.
∴ P-value is greater than 0.05 we accept it.

Q3 The diameter of a ball bearing was measured by 6 inspectors, each using two different kinds of calipers. The results were, Test whether average ball bearing for

Inspectors:	1	2	3	4	5	6
Caliper 1:	0.265	0.268	0.266	0.267	0.269	0.264
Caliper 2:	0.263	0.262	0.270	0.261	0.271	0.260

Caliper 1 and Caliper 2 are same

Code:

```
> x <- c(0.265, 0.268, 0.266, 0.267, 0.269, 0.264);  
> y <- c(0.263, 0.262, 0.270, 0.261, 0.271, 0.260);  
> wilcox.test(x, y, alternative = "greater")
```

Wilcoxon rank sum test

data: x and y

W = 24, P = 0.197

alternative hypothesis: true location shift is greater than 0

∴ P-value is greater than 0.05 we accept it.

④ An officer has three elective type writers A, B, and C. In a study of machine usage, firm has kept records of machine usage rate of seven weeks. Machine A was out of repairs for two weeks. It is of interest to find out which machine has better usage rate. Analyze the following data on wage rates and determine if there is a significant difference in average rate.

A	B	C
12.3	15.7	32.4
15.4	10.8	41.2
10.3	45.0	35.1
08.0	12.3	25.0
14.6	08.2	08.2
—	20.1	18.4
—	26.3	32.5

CODE:

```

>XL-C(12.3, 15.4, 10.3, 8.0, 14.6);
>n1<-length(x);
>n1
[1] 5
>Y<-C(15.7, 10.8, 45.0, 12.3, 8.2, 20.1,
       26.3);
>n2<-length(y);
>n2
[1] 7

```

```
[1] 7
> z <- c(32.4, 41.2, 35.1, 25.0, 18.4,
      32.5);
> n3 <- length(z);
> n3
[1] 7
> x <- c(xe, y, z);
> g <- c(rep(1, n1), rep(2, n2), rep(3, n3));
> Kruskal.test(x, g)
```

Kruskal-Wallis rank sum test
 data : x and g
 Kruskal-Wallis chi-squared = 5.217,
 df = 2, p-value = 0.07365

\therefore P-value is greater than 0.05 we accept it.

Q

Practical-10

22

AIM: chi-square tests & ANOVA
(Analysis of variance)

- Q1 Use the following data to test whether the condition of home & condition of child are independent or not.

Cond. child	Cond. Home	clean	dirty
clean	70	50	80
Pai r ly clean	80	20	35
Dirty			45

H₀: Condition of Home & child are independent.

```

>x = c(70, 80, 35, 50, 20, 45)
>m = 3
>n = 2
>y = matrix(x, nrow = m, ncol = n)

```

	[, 1]	[, 2]	
[1,]	70	50	66
[2,]	80	20	
[3,]	35	45	

> $P^V = \text{chisq.test}(y)$

> P^V

Person's chi-squared test
data : y

$$\chi^2\text{-squared} = 25.646$$

$$df = 2$$

$$P\text{-value} = 2.698e-06$$

// They are dependent

∴ Pvalue is less than 0.05 we reject
the hypothesis ~~at 5%~~ Level of significance.

Q2 Test the hypothesis that vacation &
disease are independent or Not.

Disease		Vaccine	
		Affected	Not Affected
Affected	70	46	
	35	37	

H_0 : Disease & Vaccine are independent

> $x = c(70, 35, 46, 37)$

> $m = 2$

> $n = 2$

```
> y = matrix(x, nrow=m, ncol=n).
```

```
> y  
[1] [2]
```

```
[1,] 70 46
```

```
[2,] 35 37
```

```
> pv = chisq.test(y)
```

```
> pv
```

Person's chisquared test with
yates continuity correction

data: y

x-square = 2.0275

df = 1

p-value = 0.1545

∴ p-value is more than 0.05 we accept
the hypothesis at 5% Level of
significance.

// They are independent.

(Q)