

DATA STRUCTURES & ALGORITHMS

10: GRAPHS; PART-II

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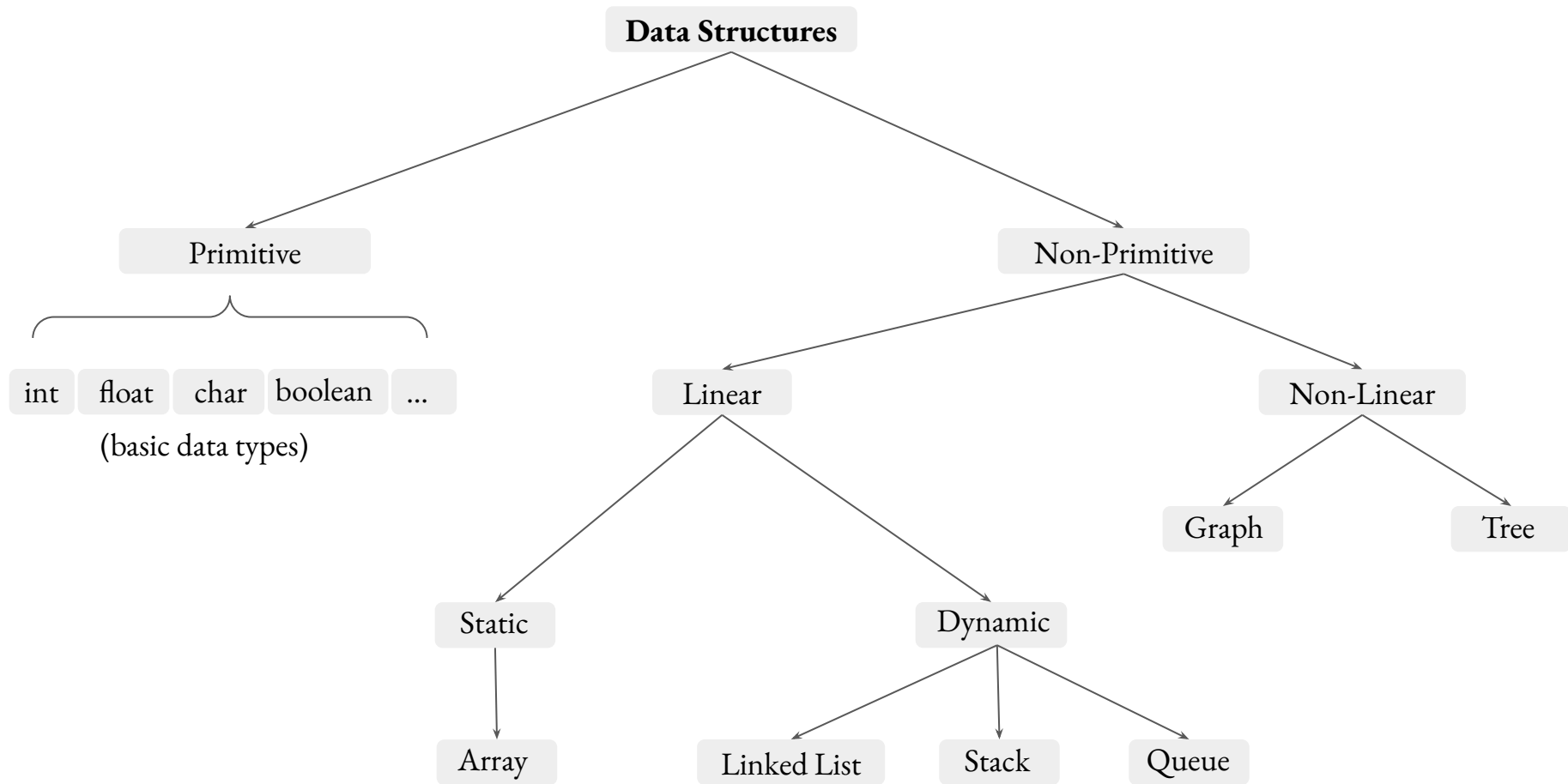
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Update in the class test dates:

- CT-02 → 26-Apr-2024, Friday
- CT-03 → 17-May-2024, Friday
- CT-04 → 31-May-2024, Friday



GRAPHS

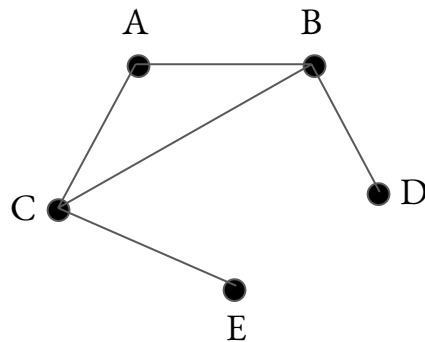
Connected Graph

A graph G is connected if there is a path between any two of its vertices.

Diameter of Graph

The maximum distance between any two vertices in connected graph.

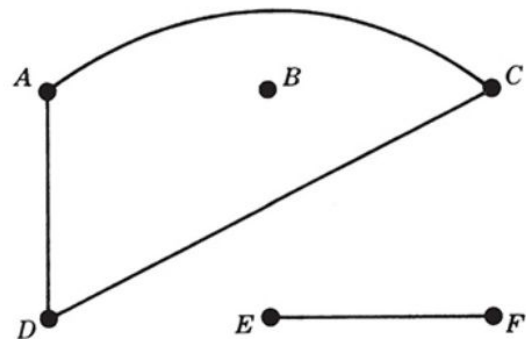
$\text{diam}(G) = 3$ in the example.



Connected Components

A subgraph where every vertex is reachable from every other vertex.

$\{A, D, C\}$, $\{E, F\}$ and $\{B\}$ are the connected components in the graph shown to right side.

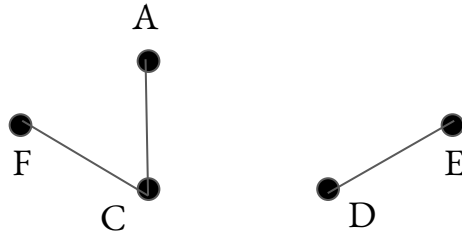
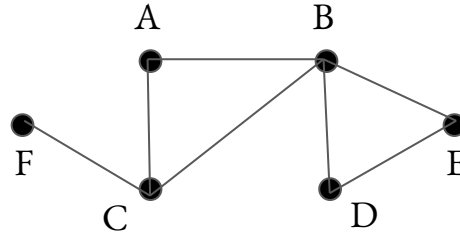


Note: An isolated vertex is considered a connected component.

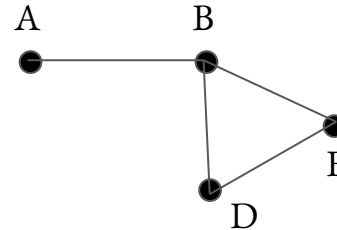
GRAPHS

Cut Point / Vertex

A vertex v in G when removed, i.e., $G - v$ will lead to more number of connected components.



$G - B$



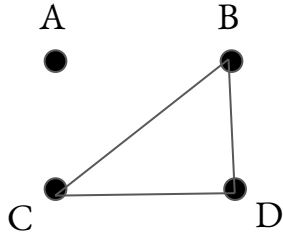
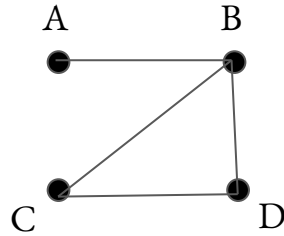
$G - C$

Both **B** and **C** are
cut points of G

GRAPHS

Bridge

An edge e in G when removed, i.e., $G - e$ will lead to more number of connected components.



$G - \{A, B\}$

$\{A, B\}$ is a bridge

GRAPHS

Directed Graphs

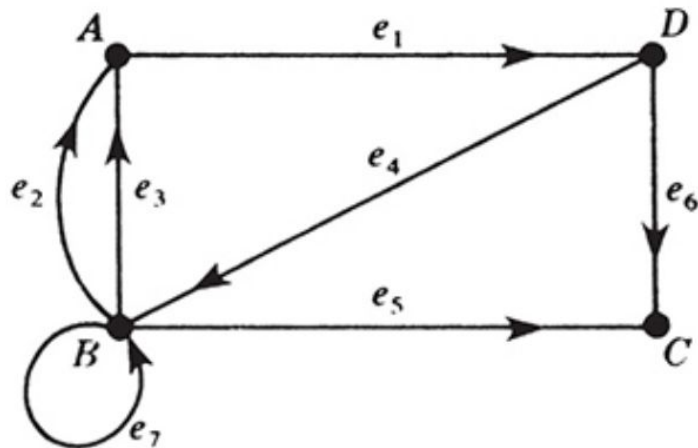
A directed graph **G** or digraph consists of two things:

- (i) A set **V** whose elements are called vertices, nodes, or points.
- (ii) A set **E** of ordered pairs **(u, v)** of vertices called **arcs** or **directed edges**.

Suppose **e = (u, v)** is a directed edge in a **digraph G**. Then the following terminology is used:

- (i) **e** begins at **u** and ends at **v**.
- (ii) **u** is the origin or initial point of **e**, and **v** is the destination or terminal point of **e**.
- (iii) **v** is a successor of **u**.
- (iv) **u** is adjacent to **v**, and **v** is adjacent from **u**.

GRAPHS



$G(V, E)$ is a directed graph:

$$V(G) = \{A, B, C, D\}$$

$$E(G) = \{e_1, e_2, \dots, e_7\}$$

$$= \{(A, D), (B, A), (B, A), (D, B), (B, C), (D, C), (B, B)\}$$