Assignment 3

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2023-10-16

Summary

1. Using the information in this dataset, if an accident has just been reported and no further information is available, what should the prediction be? (INJURY = Yes or No?) Why?

Ans: Using the information in the dataset, the prediction is Injury = Yes. This is beacuse Injury = yes is 0.50878 and Injury = No is 0.49121. Since the probability of Injury = yes is greater than the Injury = No, I predict that Injury = Yes.

2.Select the first 24 records in the dataset and look only at the response (INJURY) and the two predictors WEATHER_R and TRAF_CON_R. Create a pivot table that examines INJURY as a function of the two predictors for these 24 records. Use all three variables in the pivot table as rows/columns. 1.Compute the exact Bayes conditional probabilities of an injury (INJURY = Yes) given the six possible combinations of the predictors.

Ans: Probability of predictions

TRAF CON R = 1 and WEATHER R = 0.6666667

TRAF CON R = 0 and WEATHER R = 2, 0.1818182.

 $TRAF_CON_R = 1$ and $WEATHER_R = 1 0.0000000$

TRAF CON R = 1 and WEATHER R = 2 0.0000000

TRAF CON R = 2 and WEATHER R = 1 0.0000000

TRAF CON R=2 and WEATHER R=2 1.0000000

2.2. Classify the 24 accidents using these probabilities and a cutoff of 0.5.

 $\begin{array}{l} {\rm Ans:} \; [1] \; 0.66666667 \; 0.1818182 \; 0.00000000 \; 0.00000000 \; 0.66666667 \; 0.1818182 \; [7] \; 0.1818182 \; 0.6666667 \; 0.1818182 \\ 0.1818182 \; 0.1818182 \; 0.0000000 \; [13] \; 0.66666667 \; 0.66666667 \; 0.66666667 \; 0.66666667 \; 0.1818182 \; 0.1818182 \; 0.1818182 \\ 0.1818182 \; 0.1818182 \; 0.66666667 \; 0.66666667 \; 1.0000000 \; 0.1818182 \\ \end{array}$

Qunatitative Predictions:

2.3.Compute manually the naive Bayes conditional probability of an injury given WEATHER_R = 1 and $TRAF_CON_R = 1$.

Ans: The result of naive bayes conditional probability of an injury given WEATHER_R = 1 and TRAF CON R = 1 is "0".

2.4.Run a naive Bayes classifier on the 24 records and two predictors. Check the model output to obtain probabilities and classifications for all 24 records. Compare this to the exact Bayes classification. Are the resulting classifications equivalent? Is the ranking (= ordering) of observations equivalent?

Ans: Refer to line 160 to 176.

3.Let us now return to the entire dataset. Partition the data into training (60%) and validation (40%). 1.Run a naive Bayes classifier on the complete training set with the relevant predictors (and INJURY as the response). Note that all predictors are categorical. Show the confusion matrix.

Confusion Matrix and Statistics

Reference

Prediction no yes no 5097 7405 yes 4230 8577

Accuracy : 0.5403

3.2. What is the overall error of the validation set?

The overall error of the validation set is 0.4668721

Load the required libraries and read the input file

```
library(e1071)
library(caret)

## Loading required package: ggplot2

## Loading required package: lattice

accidents <- read.csv("C:\\Users\\priya\\OneDrive\\Desktop\\FML\\Assignment 3\\accidentsFull.csv")
accidents$INJURY = ifelse(accidents$MAX_SEV_IR>0,"yes","no")

# Convert variables to factor
for (i in c(1:dim(accidents)[2])){
   accidents[,i] <- as.factor(accidents[,i])
}
head(accidents,n=24)</pre>
```

| ## | | HOUR_I_R | ALCHL_I | ALIGN_I | STRATUM_R | WRK_ZONE | WKDY_I_R | INT_HWY | LGTCON_I_R |
|----|----|----------|---------|---------|-----------|----------|----------|---------|------------|
| ## | 1 | 0 | 2 | 2 | 1 | 0 | 1 | 0 | 3 |
| ## | 2 | 1 | 2 | 1 | 0 | 0 | 1 | 1 | 3 |
| ## | 3 | 1 | 2 | 1 | 0 | 0 | 1 | 0 | 3 |
| ## | 4 | 1 | 2 | 1 | 1 | 0 | 0 | 0 | 3 |
| ## | 5 | 1 | 1 | 1 | 0 | 0 | 1 | 0 | 3 |
| ## | 6 | 1 | 2 | 1 | 1 | 0 | 1 | 0 | 3 |
| ## | 7 | 1 | 2 | 1 | 0 | 0 | 1 | 1 | 3 |
| ## | 8 | 1 | 2 | 1 | 1 | 0 | 1 | 0 | 3 |
| ## | 9 | 1 | 2 | 1 | 1 | 0 | 1 | 0 | 3 |
| ## | 10 | 0 | 2 | 1 | 0 | 0 | 0 | 0 | 3 |
| ## | 11 | 1 | 2 | 1 | 0 | 0 | 1 | 0 | 3 |
| ## | 12 | 1 | 2 | 1 | 1 | 0 | 1 | 0 | 3 |
| ## | 13 | 1 | 2 | 1 | 1 | 0 | 1 | 0 | 3 |
| ## | 14 | 1 | 2 | 2 | 0 | 0 | 1 | 0 | 3 |
| ## | 15 | 1 | 2 | 2 | 1 | 0 | 1 | 0 | 3 |
| ## | 16 | 1 | 2 | 2 | 1 | 0 | 1 | 0 | 3 |
| ## | 17 | 1 | 2 | 1 | 1 | 0 | 1 | 0 | 3 |
| ## | 18 | 1 | 2 | 1 | 1 | 0 | 0 | 0 | 3 |

| ## | 19 | 1 | 2 | 1 | 1 | 0 | 1 | 0 | | 3 |
|----------|--------|--------------|-------------|--------------------------|---------------------------------------|--------------|---------------|----------|-----------|------------|
| ## | 20 | 1 | 2 | 1 | 0 | 0 | 1 | 0 | | 3 |
| ## | 21 | 1 | 2 | 1 | 1 | 0 | 1 | 0 | | 3 |
| ## | | 1 | 2 | 2 | 0 | 0 | 1 | 0 | | 3 |
| ## | | 1 | 2 | 1 | 0 | 0 | 1 | 0 | | 3 |
| ## | 24 | 1 | 2 | 1 | 1 | 0 | 1 | 9 | | 3 |
| ## | | | PED_ACC_R F | | | | | | | |
| ## | | 0 | 0 | 1 | | 0 | 1 | 40 | 4 | |
| ## | | 2 | 0 | 1 | | 1 | 1 | 70 | 4 | |
| ## | 3 | 2 | 0 | 1 | | 1 | 1 | 35 | 4 | |
| | 4 | 2 | 0 | 1 | | 1 | 1 | 35 | 4 | |
| ## | 5 6 | 2 | 0 | 0 | | 1 | 1 | 25 70 | 4 4 | |
| ## | 7 | 0 | 0 | 0 | | 0 | 1 | 70 | 4 | |
| | 8 | 0 | 0 | 0 | | 0 | 1 | 35 | 4 | |
| | 9 | 0 | 0 | 1 | | 0 | 1 | 30 | 4 | |
| | 10 | 0 | 0 | 1 | | 0 | 1 | 25 | 4 | |
| | 11 | 0 | 0 | 0 | | 0 | 1 | 55 | 4 | |
| | 12 | 2 | 0 | 0 | | 1 | 1 | 40 | 4 | |
| | 13 | 1 | 0 | 0 | | 1 | 1 | 40 | 4 | |
| ## | 14 | 0 | 0 | 0 | | 0 | 1 | 25 | 4 | |
| ## | 15 | 0 | 0 | 0 | | 0 | 1 | 35 | 4 | |
| ## | 16 | 0 | 0 | 0 | | 0 | 1 | 45 | 4 | |
| ## | 17 | 0 | 0 | 0 | | 0 | 1 | 20 | 4 | |
| ## | 18 | 0 | 0 | 0 | | 0 | 1 | 50 | 4 | |
| ## | 19 | 0 | 0 | 0 | | 0 | 1 | 55 | 4 | |
| ## | 20 | 0 | 0 | 1 | | 1 | 1 | 55 | 4 | |
| | 21 | 0 | 0 | 1 | | 0 | 0 | 45 | 4 | |
| | 22 | 0 | 0 | 1 | | 0 | 0 | 65 | 4 | |
| | 23 | 0 | 0 | 0 | | 0 | 0 | 65 | 4 | |
| ## | 24 | 2 TRAE CON R | 0 | 1 20 TMW 1/12/1 | ד מ מייוויים. | 1 N 111DV | 0 | 55 | 4 | CD A CII |
| ## | 1 | | TRAF_WAY VE | EH_INVL WE <i>F</i> 1 | 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 | NJUKI_ | _CRASH N 1 | | PRPIIDMG_ | CRASH 0 |
| ## | 2 | 0 | 3 | 2 | 2 | | 0 | 1 | | 1 |
| ## | 3 | 1 | 2 | 2 | 2 | | 0 | 0 | | 1 |
| ## | 4 | 1 | 2 | 2 | 1 | | 0 | 0 | | 1 |
| ## | | 0 | 2 | 3 | 1 | | 0 | 0 | | 1 |
| ## | | 0 | 2 | 1 | 2 | | 1 | 1 | | 0 |
| ## | 7 | 0 | 2 | 1 | 2 | | 0 | 0 | | 1 |
| ## | 8 | 0 | 1 | 1 | 1 | | 1 | 1 | | 0 |
| ## | 9 | 0 | 1 | 1 | 2 | | 0 | 0 | | 1 |
| ## | | 0 | 1 | 1 | 2 | | 0 | 0 | | 1 |
| ## | | 0 | 1 | 1 | 2 | | 0 | 0 | | 1 |
| ## | | 2 | 1 | 2 | 1 | | 0 | 0 | | 1 |
| ## | | 0 | 1 | 4 | 1 | | 1 | 2 | | 0 |
| ## | | 0 | 1 | 1 | 1 | | 0 | 0 | | 1 |
| ## | | 0 | 1 | 1 | 1 | | 1 | 1 | | 0 |
| ## | | 0 | 1 | 1 | 1 | | 1 | 1 | | 0 |
| ## | | 0 | 1 | 1 | 2 | | 0 | 0 | | 1 |
| ## ## | | 0 | 1 | 1 | 2 2 | | 0 | 0 | | 1 |
| ## | | 0 | 1 1 | 1 1 | 2 | | 0 | 0 | | 1 1 |
| ## | | 0 | 3 | 1 | 1 | | 1 | 1 | | 0 |
| ## | | 0 | 3 | 1 | 1 | | 0 | 0 | | 1 |
| | | v | U | - | - | | • | Ū | | - |

```
## 23
             2
                     2
                                                                             0
                      2
## 24
              0
                               2
  FATALITIES MAX_SEV_IR INJURY
## 1
             0
                             yes
## 2
              0
## 3
             0
                        0
                             no
## 4
              0
                         0
                             no
## 5
              0
                         0
## 6
              0
                        1
                            yes
## 7
              0
                         0
                             no
## 8
              0
                        1
                             yes
## 9
              0
                         0
## 10
              0
                         0
                             no
                         0
## 11
              0
## 12
              0
                         0
                             no
## 13
              0
                             yes
## 14
              0
                         0
                             no
              0
## 15
                        1
                             ves
              0
## 16
                        1
                             yes
              0
                         0
## 17
## 18
              0
                        0
                             no
## 19
              0
                        0
                             no
## 20
              0
                        0
                             no
                            yes
## 21
              0
                        1
              0
## 22
                        0
                              no
## 23
              0
                        1
                              yes
## 24
              0
                              yes
p_yes <- mean(accidents$INJURY == "yes")</pre>
p_no <- mean(accidents$INJURY == "no")</pre>
p_yes
## [1] 0.5087832
p_no
## [1] 0.4912168
accidents24 <- accidents[1:24,c("INJURY","WEATHER_R","TRAF_CON_R")]</pre>
#head(accidents24)
dt1 <- ftable(accidents24)</pre>
dt2 <- ftable(accidents24[,-1]) # print table only for conditions</pre>
                   TRAF_CON_R 0 1 2
## INJURY WEATHER_R
## no
                             3 1 1
         1
##
                             9 1 0
## yes
                             6 0 0
         1
##
         2
                             2 0 1
```

```
TRAF_CON_R 0 1 2
##
## WEATHER R
                         9 1 1
## 1
## 2
                        11 1 1
# Injury = yes
p1 = dt1[3,1] / dt2[1,1] # Injury, Weather=1 and Traf=0
p2 = dt1[4,1] / dt2[2,1] # Injury, Weather=2, Traf=0
p3 = dt1[3,2] / dt2[1,2] # Injury, W=1, T=1
p4 = dt1[4,2] / dt2[2,2] # I, W=2, T=1
p5 = dt1[3,3] / dt2[1,3] # I, W=1,T=2
p6 = dt1[4,3] / dt2[2,3] \#I, W=2, T=2
# Injury = no
n1 = dt1[1,1] / dt2[1,1] # Weather=1 and Traf=0
n2 = dt1[2,1] / dt2[2,1] # Weather=2, Traf=0
n3 = dt1[1,2] / dt2[1,2] # W=1, T=1
n4 = dt1[2,2] / dt2[2,2] # W=2, T=1
n5 = dt1[1,3] / dt2[1,3] # W=1,T=2
n6 = dt1[2,3] / dt2[2,3] # W=2,T=2
print(c(p1,p2,p3,p4,p5,p6))
```

[1] 0.6666667 0.1818182 0.0000000 0.0000000 0.0000000 1.0000000

```
print(c(n1,n2,n3,n4,n5,n6))
```

- ## [1] 0.3333333 0.8181818 1.0000000 1.0000000 1.0000000 0.0000000
 - 2. Let us now compute Classify the 24 accidents using these probabilities and a cutoff of 0.5.

```
prob.inj <- rep(0,24)

for (i in 1:24) {
    print(c(accidents24$WEATHER_R[i],accidents24$TRAF_CON_R[i]))
    if (accidents24$WEATHER_R[i] == "1") {
        if (accidents24$TRAF_CON_R[i]=="0"){
            prob.inj[i] = p1
        }
        else if (accidents24$TRAF_CON_R[i]=="1") {
            prob.inj[i] = p3
        }
        else if (accidents24$TRAF_CON_R[i]=="2") {
            prob.inj[i] = p5
        }
    }
    else {
        if (accidents24$TRAF_CON_R[i]=="0"){
            prob.inj[i] = p2
        }
}</pre>
```

```
else if (accidents24$TRAF_CON_R[i]=="1") {
    prob.inj[i] = p4
}
else if (accidents24$TRAF_CON_R[i]=="2") {
    prob.inj[i] = p6
}
}
```

```
## [1] 1 0
## Levels: 1 2 0
## [1] 2 0
## Levels: 1 2 0
## [1] 2 1
## Levels: 1 2 0
## [1] 1 1
## Levels: 1 2 0
## [1] 1 0
## Levels: 1 2 0
## [1] 2 0
## Levels: 1 2 0
## [1] 2 0
## Levels: 1 2 0
## [1] 1 0
## Levels: 1 2 0
## [1] 2 0
## Levels: 1 2 0
## [1] 2 0
## Levels: 1 2 0
## [1] 2 0
## Levels: 1 2 0
## [1] 1 2
## Levels: 1 2 0
## [1] 1 0
## Levels: 1 2 0
## [1] 1 0
## Levels: 1 2 0
## [1] 1 0
## Levels: 1 2 0
## [1] 1 0
## Levels: 1 2 0
## [1] 2 0
## Levels: 1 2 0
## [1] 2 0
## Levels: 1 2 0
## [1] 2 0
## Levels: 1 2 0
## [1] 2 0
## Levels: 1 2 0
## [1] 1 0
## Levels: 1 2 0
## [1] 1 0
## Levels: 1 2 0
```

```
## [1] 2 2
## Levels: 1 2 0
## [1] 2 0
## Levels: 1 2 0
accidents24$prob.inj <- prob.inj
accidents24$prob.inj
  [1] 0.6666667 0.1818182 0.0000000 0.0000000 0.6666667 0.1818182 0.1818182
## [8] 0.6666667 0.1818182 0.1818182 0.0000000 0.6666667 0.6666667
## [15] 0.6666667 0.6666667 0.1818182 0.1818182 0.1818182 0.1818182 0.6666667
## [22] 0.6666667 1.0000000 0.1818182
accidents24$pred.prob <- ifelse(accidents24$prob.inj>0.5, "yes", "no")
accidents24$pred.prob
## [1] "yes" "no" "no" "no" "yes" "no" "no"
                                                 "yes" "no" "no" "no"
## [13] "yes" "yes" "yes" "yes" "no" "no"
                                           "no"
                                                 "no" "yes" "yes" "yes" "no"
Compute manually the naive Bayes conditional probability of an injury given WEATHER_R = 1 and
TRAF CON R = 1.
P_{V1_IY} = \frac{dt1[3,1]+dt1[3,2]+dt1[3,3]}{dt1[3,1]+dt1[3,2]+dt1[3,3]+dt1[4,1]+dt1[4,2]+dt1[4,3]}
P T1 IY = (dt1[3,2]+dt1[4,2])/(dt1[3,1]+dt1[3,2]+dt1[3,3]+dt1[4,1]+dt1[4,2]+dt1[4,3])
     = (dt1[3,1]+dt1[3,2]+dt1[3,3]+dt1[4,1]+dt1[4,2]+dt1[4,3])/24
P_{V1}IN = \frac{dt1[1,1]+dt1[1,2]+dt1[1,3]}{dt1[1,1]+dt1[1,2]+dt1[1,3]+dt1[2,1]+dt1[2,2]+dt1[2,3]}
P_T1_IN = (dt1[1,2]+dt1[2,2])/(dt1[1,1]+dt1[1,2]+dt1[1,3]+dt1[2,1]+dt1[2,2]+dt1[2,3])
      = (dt1[1,1]+dt1[1,2]+dt1[1,3]+dt1[2,1]+dt1[2,2]+dt1[2,3])/24
P_IY_W1.T1= (P_W1_IY*P_T1_IY*PIY)/((P_W1_IY*P_T1_IY*PIY)+(P_W1_IN*P_T1_IN*PIN))
P_IY_W1.T1
```

[1] 0

Run a naive Bayes classifier on the 24 records and two predictors. Check the model output to obtain probabilities and classifications for all 24 records. Compare this to the exact Bayes classification. Are the resulting classifications equivalent? Is the ranking (= ordering) of observations equivalent?

```
## A-priori probabilities:
## Y
##
     no
           ves
## 0.625 0.375
## Conditional probabilities:
##
        TRAF CON R
## Y
                             1
##
    no 0.80000000 0.13333333 0.06666667
##
     yes 0.88888889 0.00000000 0.11111111
##
##
        WEATHER_R
## Y
                 1
##
    no 0.3333333 0.6666667
##
     yes 0.6666667 0.33333333
Let us use caret
library(klaR)
## Loading required package: MASS
nb2 <- train(INJURY ~ TRAF_CON_R + WEATHER_R,
     data = accidents24, method = "nb")
## Warning: model fit failed for Resample01: usekernel=FALSE, fL=0, adjust=1 Error in NaiveBayes.defaul
    Zero variances for at least one class in variables: TRAF_CON_R1
## Warning: model fit failed for Resample02: usekernel=FALSE, fL=0, adjust=1 Error in NaiveBayes.defaul
     Zero variances for at least one class in variables: TRAF_CON_R1
## Warning: model fit failed for Resample03: usekernel=FALSE, fL=0, adjust=1 Error in NaiveBayes.defaul
    Zero variances for at least one class in variables: TRAF_CON_R1
## Warning: model fit failed for Resample04: usekernel=FALSE, fL=0, adjust=1 Error in NaiveBayes.defaul
    Zero variances for at least one class in variables: TRAF_CON_R1, TRAF_CON_R2
## Warning: model fit failed for Resample05: usekernel=FALSE, fL=0, adjust=1 Error in NaiveBayes.defaul
     Zero variances for at least one class in variables: TRAF_CON_R1, TRAF_CON_R2, WEATHER_R2
## Warning: model fit failed for Resample06: usekernel=FALSE, fL=0, adjust=1 Error in NaiveBayes.defaul
     Zero variances for at least one class in variables: TRAF_CON_R1, TRAF_CON_R2
## Warning: model fit failed for Resample07: usekernel=FALSE, fL=0, adjust=1 Error in NaiveBayes.defaul
    Zero variances for at least one class in variables: TRAF_CON_R1, TRAF_CON_R2
## Warning: model fit failed for Resample08: usekernel=FALSE, fL=0, adjust=1 Error in NaiveBayes.defaul
     Zero variances for at least one class in variables: TRAF_CON_R1
```

Zero variances for at least one class in variables: TRAF_CON_R1, TRAF_CON_R2

Warning: model fit failed for Resample09: usekernel=FALSE, fL=0, adjust=1 Error in NaiveBayes.defaul

```
## Warning: model fit failed for Resample10: usekernel=FALSE, fL=0, adjust=1 Error in NaiveBayes.defaul
    Zero variances for at least one class in variables: TRAF_CON_R1, TRAF_CON_R2
## Warning: model fit failed for Resample11: usekernel=FALSE, fL=0, adjust=1 Error in NaiveBayes.defaul
     Zero variances for at least one class in variables: TRAF_CON_R1
## Warning: model fit failed for Resample12: usekernel=FALSE, fL=0, adjust=1 Error in NaiveBayes.defaul
     Zero variances for at least one class in variables: TRAF_CON_R1, TRAF_CON_R2
## Warning: model fit failed for Resample13: usekernel=FALSE, fL=0, adjust=1 Error in NaiveBayes.defaul
    Zero variances for at least one class in variables: TRAF_CON_R1, TRAF_CON_R2
## Warning: model fit failed for Resample14: usekernel=FALSE, fL=0, adjust=1 Error in NaiveBayes.defaul
     Zero variances for at least one class in variables: TRAF_CON_R1
## Warning: model fit failed for Resample15: usekernel=FALSE, fL=0, adjust=1 Error in NaiveBayes.defaul
    Zero variances for at least one class in variables: TRAF_CON_R1
## Warning: model fit failed for Resample16: usekernel=FALSE, fL=0, adjust=1 Error in NaiveBayes.defaul
    Zero variances for at least one class in variables: TRAF_CON_R1, TRAF_CON_R2
## Warning: model fit failed for Resample17: usekernel=FALSE, fL=0, adjust=1 Error in NaiveBayes.defaul
     Zero variances for at least one class in variables: TRAF CON R1
## Warning: model fit failed for Resample18: usekernel=FALSE, fL=0, adjust=1 Error in NaiveBayes.defaul
    Zero variances for at least one class in variables: TRAF_CON_R1, TRAF_CON_R2
## Warning: model fit failed for Resample19: usekernel=FALSE, fL=0, adjust=1 Error in NaiveBayes.defaul
    Zero variances for at least one class in variables: TRAF_CON_R1
## Warning: model fit failed for Resample20: usekernel=FALSE, fL=0, adjust=1 Error in NaiveBayes.defaul
     Zero variances for at least one class in variables: TRAF_CON_R1, TRAF_CON_R2
## Warning: model fit failed for Resample21: usekernel=FALSE, fL=0, adjust=1 Error in NaiveBayes.defaul
    Zero variances for at least one class in variables: TRAF_CON_R1, TRAF_CON_R2
## Warning: model fit failed for Resample22: usekernel=FALSE, fL=0, adjust=1 Error in NaiveBayes.defaul
    Zero variances for at least one class in variables: TRAF_CON_R1
## Warning: model fit failed for Resample23: usekernel=FALSE, fL=0, adjust=1 Error in NaiveBayes.defaul
    Zero variances for at least one class in variables: TRAF_CON_R1
## Warning: model fit failed for Resample24: usekernel=FALSE, fL=0, adjust=1 Error in NaiveBayes.defaul
     Zero variances for at least one class in variables: TRAF_CON_R1, TRAF_CON_R2
## Warning: model fit failed for Resample25: usekernel=FALSE, fL=0, adjust=1 Error in NaiveBayes.defaul
    Zero variances for at least one class in variables: TRAF_CON_R1, TRAF_CON_R2
```

Warning in nominalTrainWorkflow(x = x, y = y, wts = weights, info = trainInfo,

Warning in train.default(x, y, weights = w, ...): missing values found in

: There were missing values in resampled performance measures.

aggregated results

3.Let us now return to the entire dataset. Partition the data into training (60%) and validation (40%). Run a naive Bayes classifier on the complete training set with the relevant predictors (and INJURY as the response). Note that all predictors are categorical. Show the confusion matrix.

```
##
## Naive Bayes Classifier for Discrete Predictors
## Call:
## naiveBayes.default(x = X, y = Y, laplace = laplace)
## A-priori probabilities:
## Y
          nο
                   yes
## 0.4939745 0.5060255
##
## Conditional probabilities:
        HOUR_I_R
##
## Y
##
     no 0.5689490 0.4310510
##
     yes 0.5703131 0.4296869
##
##
        ALIGN_I
## Y
                            2
                 1
##
     no 0.8712206 0.1287794
     yes 0.8652300 0.1347700
##
##
##
        WRK_ZONE
## Y
     no 0.97664374 0.02335626
##
```

```
##
     ves 0.97727805 0.02272195
##
        WKDY_I_R
##
## Y
##
     no 0.2194049 0.7805951
     yes 0.2381510 0.7618490
##
##
##
        INT_HWY
## Y
                    0
                                  1
##
     no 0.8513837786 0.1481362982 0.0004799232
##
     yes 0.8593737800 0.1397673147 0.0008589053
##
##
        LGTCON_I_R
## Y
                            2
##
     no 0.6870101 0.1251000 0.1878899
##
     yes 0.7014914 0.1096275 0.1888811
##
##
        PROFIL_I_R
## Y
                 0
##
     no 0.7531595 0.2468405
##
     yes 0.7633326 0.2366674
##
##
        SPD_LIM
## Y
                    5
                                 10
     no 0.0000799872 0.0004799232 0.0043992961 0.0085586306 0.1121420573
##
##
     yes 0.0001561646 0.0003123292 0.0040602795 0.0039041149 0.0906535488
##
        SPD_LIM
## Y
                                 35
                   30
                                               40
                                                            45
##
     no 0.0860662294 0.1896496561 0.0962246041 0.1553351464 0.0407934730
     yes 0.0860466932 0.2123057703 0.1068946670 0.1574139143 0.0394315609
##
##
        SPD_LIM
## Y
                   55
                                 60
                                               65
                                                            70
                                                                          75
     no 0.1590145577 0.0355143177 0.0645496721 0.0409534474 0.0062390018
##
##
     yes 0.1549152807 0.0430233466 0.0621535098 0.0311548372 0.0075739830
##
##
        SUR COND
## Y
                                            3
##
     no 0.774196129 0.176931691 0.016717325 0.028155495 0.003999360
##
     yes 0.815725775 0.151245413 0.010697275 0.016709612 0.005621926
##
        TRAF_CON_R
##
## Y
                 0
     no 0.6566149 0.1902096 0.1531755
##
##
     yes 0.6213009 0.2191770 0.1595221
##
##
        TRAF_WAY
## Y
                              2
     no 0.57998720 0.36690130 0.05311150
##
##
     yes 0.56063090 0.39743890 0.04193019
##
        WEATHER_R
##
## Y
##
     no 0.8390657 0.1609343
##
     yes 0.8744437 0.1255563
```

```
#generating the confusion matrix using the train.df, the prediction and the classes
confusionMatrix(train.df$INJURY, predict(nbTotal, train.df[, vars]), positive = "yes")
```

```
## Confusion Matrix and Statistics
##
##
             Reference
## Prediction no yes
##
          no 5097 7405
##
          yes 4230 8577
##
                  Accuracy : 0.5403
##
                    95% CI : (0.5341, 0.5464)
##
       No Information Rate: 0.6315
##
##
       P-Value [Acc > NIR] : 1
##
##
                     Kappa: 0.0776
##
   Mcnemar's Test P-Value : <2e-16
##
##
##
               Sensitivity: 0.5367
##
               Specificity: 0.5465
            Pos Pred Value: 0.6697
##
##
            Neg Pred Value: 0.4077
                Prevalence: 0.6315
##
##
            Detection Rate: 0.3389
##
      Detection Prevalence: 0.5060
##
         Balanced Accuracy: 0.5416
##
##
          'Positive' Class : yes
##
What is the overall error of the validation set?
confusion_matrix= confusionMatrix(valid.df$INJURY, predict(nbTotal, valid.df[, vars]), positive = "yes"
print(confusion_matrix)
## Confusion Matrix and Statistics
##
##
             Reference
## Prediction
              no yes
          no 3203 5016
##
          yes 2862 5793
##
##
##
                  Accuracy: 0.5331
##
                    95% CI: (0.5256, 0.5407)
##
       No Information Rate: 0.6406
```

P-Value [Acc > NIR] : 1

Mcnemar's Test P-Value : <2e-16

Kappa: 0.0594

##

##

##

```
##
               Sensitivity : 0.5359
##
               Specificity: 0.5281
##
            Pos Pred Value : 0.6693
##
            Neg Pred Value: 0.3897
##
                Prevalence : 0.6406
            Detection Rate: 0.3433
##
     Detection Prevalence: 0.5129
##
##
         Balanced Accuracy: 0.5320
##
##
          'Positive' Class : yes
##
#Calculated overall error
overall_error <- 1 - confusion_matrix$overall["Accuracy"]</pre>
cat("overall error of the validation set:", overall_error, "\n")
```

overall error of the validation set: 0.4668721