

5. ARRAYS

- Advantages : ① Random access ② Cache friendly
- Vector advantages : ① Dynamic size ② Rich library function
- ③ Easy to know size ④ No need to pass size
- ⑤ Can be returned from a function ⑥ Initialized with default value
- ⑦ easy to copy a vector.

Left Rotate a given array by d places.

```
void leftrotate ( int arr[], int n, int d ) {
    reverse ( arr, 0, d - 1 );
    reverse ( arr, d, n - 1 );
    reverse ( arr, 0, n - 1 );
```

TC: $\Theta(n)$

SC: $\Theta(1)$

```
void reverse ( int arr[], int low, int high ) {
    while ( low < high ) {
        swap ( arr[low], arr[high] );
        low++;
        high--;
```

Maximum difference (\leftarrow find max^m diff value in array).

```
int maxdiff ( int arr[], int n ) {
    int minval = arr[0];
    int res = arr[1] - arr[0];
    for ( int i = 1 ; i < n ; i++ ) {
        res = max ( res, arr[i] - minval );
        minval = min ( minval, arr[i] );
    }
    return res;
```

TC: $\Theta(n)$

SC: $\Theta(1)$

Max^m Consecutive 1's in a binary array

binary array \rightarrow array of only '0' & '1' [0, 1, 0, 1, 0, 1]

```
int maxcons( int arr[], int n ) {
```

```
    int cur = 0;
```

```
    int res = 0;
```

```
    for( int i=0 ; i<n ; i++ ) {
```

```
        if (arr[i] == 0)
```

```
            if (cur == 0) :
```

```
                else {
```

```
                    cur++;
```

```
                res = max( res, cur );
```

```
    }
```

```
}
```

Trapping rain water problem



$\Rightarrow \text{ans} = 7$

consider all numbers in vector as bars, so find how many rain water can be stored.

```
int rainwater( int a[], int n ) {
```

```
    int l[n], r[n];
```

```
    l[0] = a[0];
```

```
    for( int i=1 ; i<n ; i++ ) {
```

```
        l[i] = max( l[i-1], a[i] );
```

```
}
```

```
r[n-1] = a[n-1];
```

```
for( int i=n-2 ; i>0 ; i-- ) {
```

```
    r[i] = max( r[i+1], a[i] );
```

```
3.
```

```

int ans=0;
for( int i=0; i<n; i++ ) {
    ans += min(lc[i], rc[i]) - a[i];
}
return ans;

```

Stock buy and sell problem. [given a vector of price of a stock find max^m profit you can extract]

```

int stockproblem( int a[], int n ) {
    int profit = 0;
    for( int i=0; i<n-1, i++ )
    {
        if( a[i] < a[i+1] )
            profit += a[i+1] - a[i];
    }
    return profit;
}

```

TC: O(n)
SC: O(1)

Max^m subarray sum [Subarray \Rightarrow contiguous part of array find a subarray with max^m sum value]

```

int maxmsubarray( int a[], int n ) {
    int res = a[0], maxim = a[0];
    for( int i=1; i<n; i++ ) {
        maxim = max( maxim + a[i], a[i] );
        res = max( maxim, res );
    }
    return res;
}

```

TC: O(n)
SC: O(1)

largest even-odd length { Kadane Algorithm }

```

int evenodd( int a[], int n ) {
    int ans = 1, cur = 1;
    for( int i=1; i<n; i++ ) {
        if( ( a[i] % 2 == 0 and a[i-1] % 2 != 0 ) or
            ( a[i] % 2 != 0 and a[i-1] % 2 == 0 ) )
            cur++;
        ans = max( ans, cur );
    }
    return ans;
}

```

TC: O(n)
SC: O(1)

(TC: O(n))

Max^m circular Subarray sum

→ here Method①: take max^m subarray sum for normal part and for circular part,

$$\text{max}^m \text{ circular subarray sum} = \text{Total subarray sum} - \text{min}^m \text{ subarray sum}$$

$$\Rightarrow \text{ans} = \max_m (\text{max}_m \text{ normal part}, \text{max}_m \text{ circular part})$$

→ here method ②: take max^m subarray sum for normal part and for circular part,

we invert given array (* by (-1)) and then find max^m subarray sum and add it to total array sum.

⇒ Method ① : for normal part : kadane Algo
 for circular part : modified kadane algo.

```
int maxCircularSubarray ( int a[], int n ) {
    int curn = a[0], maxn = a[0];
    for ( int i = 1; i < n; i++ ) {
        curn = max ( curn + a[i], a[i] );
        maxn = max ( maxn, curn );
    }
    int curc = a[0], resc = a[0];
    for ( int i = 1; i < n; i++ ) {
        curc = min ( curc + a[i], a[i] );
        resc = min ( resc, curc );
    }
    int tot = 0;
    for ( int i = 0; i < n; i++ )
        tot += a[i];
    resc = tot - resc;
    return max ( maxn, resc );
}
```

⇒ Method ② : for normal part : kadane Algo.
 for circular part : Invert + kadane algo + (sum + res)

```
int maxCircularSubarray ( int a[], int n ) {
    int curn = a[0], maxn = a[0];
    for ( int i = 1; i < n; i++ ) {
        curn = max ( curn + a[i], a[i] );
        maxn = max ( maxn, curn );
    }
    int tot = 0;
    for ( int i = 0; i < n; i++ )
        tot += a[i];
    tot += resc;
    return max ( maxn, tot );
}
```

```

for (int i=0; i<n; i++)
    a[i] = -a[i];
int curc = a[0], maxc = a[0];
for (int i=1; i<n; i++) {
    curc = max(circ + a[i], a[i]);
    maxc = max(circ, maxc);
}
maxc = tot + maxc;
return max(maxn, maxc);

```

Majority Element {Boyer-Moore Majority voting}

Majority is when count > n/2

```

int majority ( int a[], int n ) {
    int count=1, res=0;
    for ( int i=1; i<n; i++ ) {
        if ( a[res] == a[i] )
            count++;
        else
            count--;
        if ( count == 0 ) {
            res = i;
            count = 1;
        }
    }
}

```

Tc : O(n)
Sc : O(1)

→ Check for candidate
candidate = a[res]

```

int ans = 0;
for ( int i=0; i<n; i++ ) {
    if ( a[res] == a[i] )
        ans++;
}
if ( ans < n/2 )
    return -1;
else
    return a[res];

```

→ check if a[res]
is an actual majority element or not.

Min^m consecutive flips for binary array.

if ($a[0] == a[n-1]$) \Rightarrow no. of set's of 1's - no. of set's of 0's = 1
 else \Rightarrow no. of set's of 1's = no. of set's of 0's

```
void minmconsec( int a[], int n ) {
    for( int i=1; i<n; i++ ) {
        if ( a[i] != a[i-1] ) {
            if ( a[i] != a[0] )
                cout << "from" << i;
            else
                cout << i-1;
        }
    }
    if ( a[n-1] != a[0] )
        cout << n-1;
}
```

Sliding Window

- ① given array a and a int k , find max^m sum of k consecutive element

```
int maxmK( int a[], int n, int k ) {
    int sum = 0;
    for( int i=0; i<k; i++ )
        sum += a[i];
```

TC: O(n)
SC: O(1)

```
int ans = sum;
for( int i=k; i<n; i++ )
{ }
```

```
sum += a[i] - a[i-k];
ans = max( ans, sum );
```

```
}
```

② find Subarray with a given Sum S.

```

bool
int sol ( int a[], int n, int sum ) {
    int cur = a[0]; s = 0;
    for ( int e = 1; e < n; e++ ) {
        while ( cur < sum and s < e - 1 ) {
            cur -= a[s];
            s++;
        }
        if ( cur == sum )
            return true;
        if ( e < n )
            cur += a[e];
    }
    return ( cur == sum );
}

```

TC: O(n)
SC: O(1)

③ Nth - binacci number:

```

void sol() {
    int n, m;
    cin >> n >> m;
    int a[m];
    for ( int i = 0; i < n; i++ )
        a[i] = 0;
    a[n-1] = 1;
    int sum = 1;
    for ( int i = n; i < m; i++ ) {
        a[i] = sum;
        sum += a[i] - a[i-n];
    }
}

```

★ Prefix Sum

- ① given an array arr and a int l and r
find sum for range $l \rightarrow r$

```
int range ( int arr[], int n, int l, int r ) {
    int prefix[n];
    int sum = 0;
    for ( int i=0; i<n; i++ ) {
        sum += arr[i];
        prefix[i] = sum;
    }
    if ( l == 0 )
        return prefix[r];
    else
        return prefix[r] - prefix[l-1];
}
```

TC: O(n)

SC: O(n)

- ② find if equilibrium point exist { ie, sum of left = sum of right }

```
bool eqpt ( int a[], int n ) {
    int lsum = 0; sum = 0;
    for ( int i=0; i<n; i++ ) {
        sum += a[i];
    }
    for ( int i=0; i<n; i++ ) {
        if ( lsum == sum - a[i] )
            return true;
        lsum += a[i];
        sum -= a[i];
    }
}
```

TC: O(n)

SC: O(1)



find frequency in limited range

- ① Subtract 1 from all element {indexing from 0}.
- ② add n to every point the element point
- ③ $f_{req} = a[i]/n;$

```
void sol( int a[], int n ) {
    for( int i=0; i<n; i++ )
        a[i] --;
    for( int i=0; i<n; i++ )
        a[a[i]] += n;
    for( int i=0; i<n; i++ )
        cout << a[i]/n;
}
```

Leader in an array [every maxm is a leader. when we go right to left].

```
void sol( int a[], int n ) {
    int maxm = INT_MIN;
    for( int i=n-1; i>0; i-- ) {
        if ( a[i] > maxm ) {
            cout << a[i];
            maxm = a[i];
        }
    }
}
```

TC: O(n)
SC: O(1)

Smallest positive missing number.

```
int missingnumber ( int a[], int n ) {
    int p = 0;
    for ( int i = 0; i < n; i++ ) {
        if ( a[i] == i ) {
            p++;
            break;
        }
    }
}
```

Tc: O(n)

Sc: O(1)

```
if ( p == 0 )
    return 1;
for ( int i = 0; i < n; i++ ) {
    if ( a[i] <= 0 || a[i] > n )
        a[i] = 1;
```

```
for ( int i = 0; i < n; i++ ) {
    if ( ( a[i] - 1 ) % n + 1 == n )
        for ( int j = 0; j < n; j++ ) {
            if ( a[j] <= n )
                a[j] = n + 1;
        }
    return i + 1;
}
return n + 1;
```

3.

Rearranging sorted array alternatively (maxm minm format).

Tc: O(n)
Sc: O(1)

```
void sol ( int a[], int n ) {
    int maxm = a[n - 1] + 1;
    int mini = 0, maxi = n - 1;
    for ( int i = 0; i < n; i++ ) {
        if ( i % 2 == 0 ) {
            a[i] += ( a[maxi] % maxm ) * maxm;
            maxi--;
        }
    }
}
```

else {

$a[i] += (a[mini] - \% . maxm) * maxm;$
 $mini++;$

3. q to v

3.

for (int i=0; i<n; i++)

$a[i] = a[i] / maxm;$

3.

To store 2 value at 1 index

increment by $(arr[arr[i]\%n]*n)$

and to get old value $a[i]\%n$

to get new value $a[i]/n$

★ ★ ★ Rearrange an array with O(1) extra space.
 $\hookrightarrow a[i] = a[a[i]]$

void sol(int a[], int n) {

for (int i=0; i<n; i++)

$a[i] += (a[a[i]\%n]*n);$

for (int i=0; i<n; i++)

$a[i] = a[i]/n;$

3.

Largest subarray sum [Kadane algo] {2nd implementation}

int max_so_far = INT_MIN, max_end_here = 0;

int start = 0, end = 0, s = 0;

for (int i=0; i<n; i++) {

$max_end_here += a[i];$

if ($max_so_far < max_end_here$) {

$max_so_far = max_end_here;$

Start = s;

end = i;

3.

if (max_end - here < 0) {

 max_end - here = 0;

 s = i + 1;

3.

cout << max_so_far << start << end;

find max^m diff. ~~(j-i)~~ such that A[i] ≤ A[j] and i ≤ j

```
(def) int maxdiff (int a[], int n) {
```

```
    int l[n], r[n];
```

```
    l[0] = a[0];
```

```
    for (int i=1; i<n; i++)
```

```
        l[i] = min (l[i-1], a[i]);
```

```
        r[n-1] = a[n-1];
```

```
    for (int i=n-2; i>=0; i--)
```

```
        r[i] = max (r[i+1], a[i]);
```

```
    int i=0, j=0, diff = -1;
```

```
    while (i <n and j <n) {
```

```
        if (l[i] ≤ r[j]) {
```

```
            diff = max (diff, j-i);
```

```
            i++;
```

```
        } else {
```

```
            j++;
```

for eg:

a = 34, 8, 10, 3, 2, 80, 30, 33, 1

l = 34, 8, 8, 3, 2, 2, 2, 2, 1,

r = 80, 80, 80, 80, 80, 33, 33, 1

diff = 6

return diff;

3.

Sieve of Sundaram (print all primes $\leq n$)

of the form
 $i+j+2*i*j$

TC: $O(n)$
SC: $O(n)$

```
void fun(int n) {
    int newn = (n-1)/2;
    bool arr[newn+1];
    memset(arr, false, sizeof(arr));
    for (int i=1; i<=newn; i++) {
        for (int j=i; (i*j + 2*i*j) <= newn; j++)
            arr[i*j + 2*i*j] = true;
    }
    if (n>2)
        cout << 2 << endl;
    for (int i=1; i<=newn; i++)
        if (arr[i] == false)
            cout << 2*i+1 << " ";
}
```

3.

Longest span with same sum of 2 binary array

$a = 0, 1, 0, 0, 0, 0$
$b = 1, 0, 1, 0, 0, 1$
$c = -1, 1, -1, 0, 0, -1$

TC: $O(n)$
SC: $O(n)$

```
int sol (int a[], int b[], int n) {
    int c[n], m {int, int} m;
    for (int i=0; i<n; i++)
        c[i] = a[i] - b[i];
    int cur=0, res=0;
    for (int i=0; i<n; i++) {
        cur += c[i];
        if (cur == 0)
            res = i+1;
        if (m.find(cur) != m.end())
            res = max(res, i-m[cur]);
        else
            m[cur] = i;
    }
    return res;
}
```

Max^m occurred integer in n ranges.

```
int sol( int l[], int r[], int n ) {
    int M = 0;
    vector<int> a( 100000 );
    for( int i=0; i<n; i++ ) {
        a[ l[i] ]++;
        a[ r[i] +1 ]--;
        if( r[i] > M )
            M = r[i];
    }
}
```

3.

```
int s = a[0], ind;
for( int i=1; i<=M+1; i++ ) {
    a[i] += a[i-1];
    if( a[i] > s )
        s = a[i];
    ind = i;
}
```

3.

~~return i;~~

3.