

Day 6

12 November 2022 15:04

Given an array arr[] denoting heights of N towers and a positive integer K.

For **each** tower, you must perform **exactly one** of the following operations **exactly once**.

- **Increase** the height of the tower by **K**
- **Decrease** the height of the tower by **K**

Find out the **minimum** possible difference between the height of the shortest and tallest towers after you have modified each tower.

You can find a slight modification of the problem [here](#).

Note: It is **compulsory** to increase or decrease the height by **K** for each tower. **After** the operation, the resultant array should **not** contain any **negative integers**.

Minimize

Input:

K = 2, N = 4

Arr[] = {1, 5, 8, 10}

Output:

5

Explanation:

The array can be modified as {3, 3, 6, 8}. The difference between the largest and the smallest is 8-3 = 5.

Example 2:

Input:

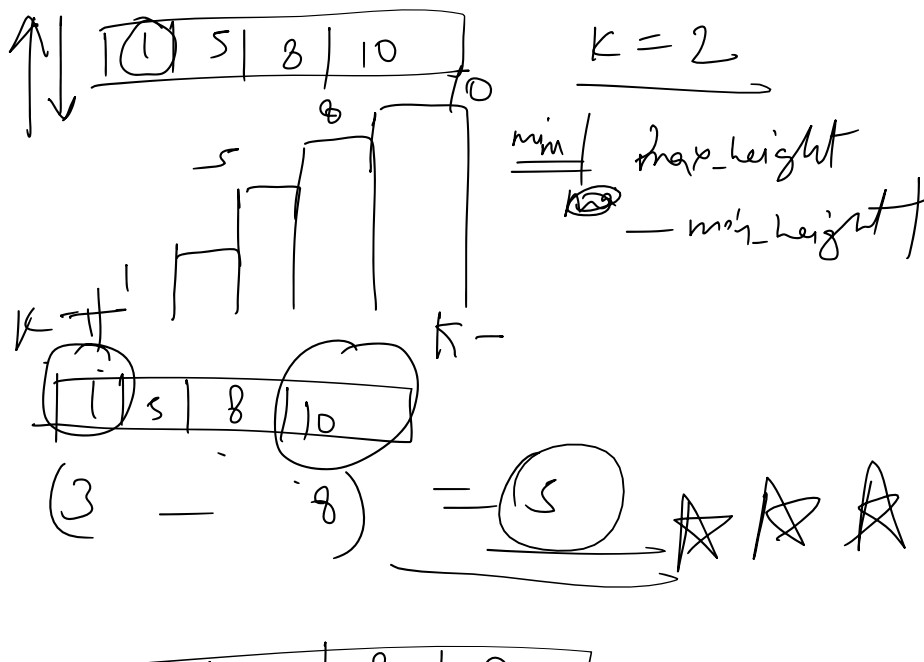
K = 3, N = 5

Arr[] = {3, 9, 12, 16, 20}

Output:

11

the heights 2

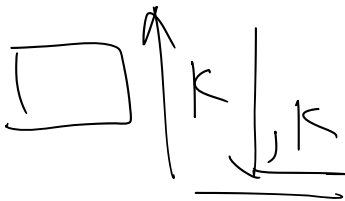


$$\begin{array}{|c|c|c|c|c|} \hline 1 & 5 & 8 & 10 & \\ \hline \end{array}$$

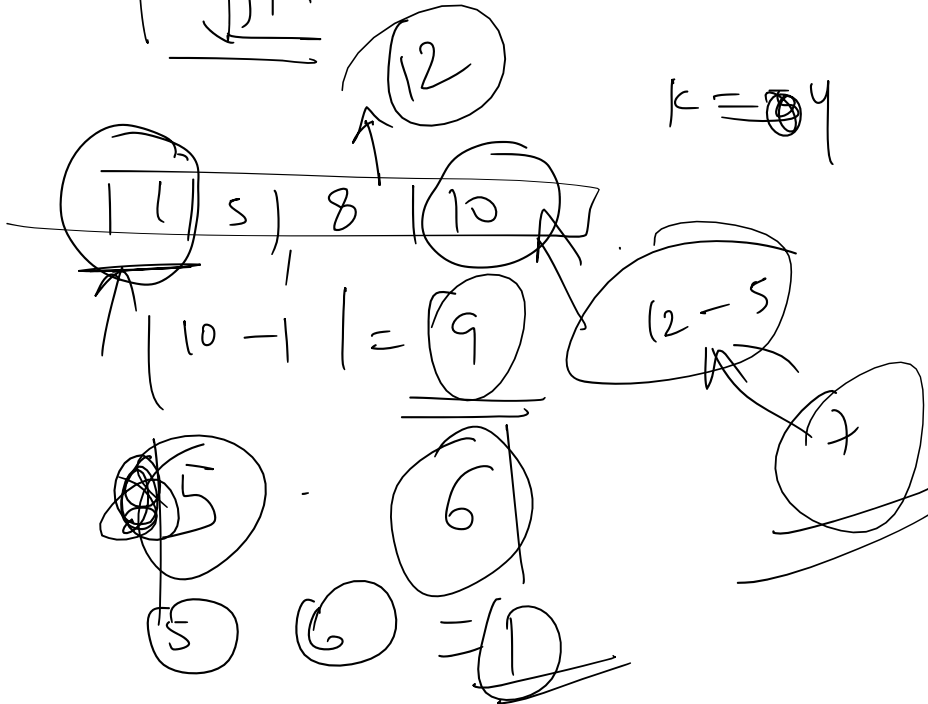
↑ ↓ ↑ ↓ ↑ ↓ ↑ ↓

min } difference (minimize)
max

Satyam

$$\begin{array}{|c|c|c|c|} \hline 0 & 1 & 2 & 3 \\ \hline 1 & 5 & 8 & 10 \\ \hline \end{array}$$


$k = 4$



(Baseline)
without any operations
largest
smallest

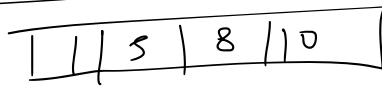
```
int getMinDiff(int arr[], int n, int k) {
    sort(arr, arr + n);
    int maxEle, minEle;
    int result = arr[n-1] - arr[0];

    for(int i = 1; i < n; i++){
        maxEle = max(arr[i-1] + k, arr[n-1] - k);
        minEle = min(arr[i] - k, arr[0] + k);
        if(minEle < 0){
            continue;
        }
        result = min(result, maxEle - minEle);
    }
    return result;
}
```

Algorithm ① sort the heights

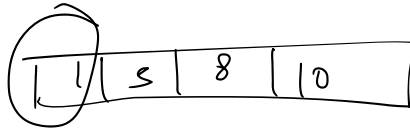
1 5 8 10 $k = 7$

1. Initialization



0

$k = 2$



$$\text{baseline} = (10 - 1) = \underline{9} \xrightarrow{k=2} \text{ans}$$

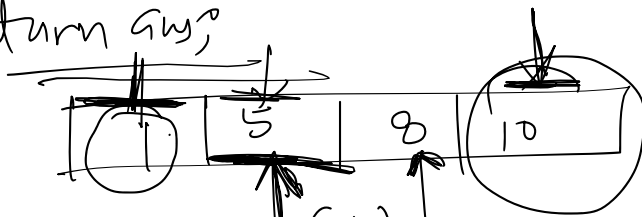
$$\text{largest} = 10 - k = \underline{8}$$

$$\text{smallest} = 1 + k = \underline{3}$$

```
for(int i=1; i<n; i++){
    mini = min(smallest, arr[i]-k);
    maxi = max(largest, arr[i-1]+k);
    ans = min(ans, maxi-mini);
}
```

3
return ans;

Ex 1
 $k=2$



$$\text{smallest} = 1 + 2 = \underline{3}$$

$$\text{largest} = 10 - 2 = \underline{8}$$

$$5 - 2 = \underline{3}$$

$$8 - k = \underline{6}$$

for (i=1 to n-1)

$$s = \min(5, 3)$$

$$l = \max(8, 1+k) \quad // \quad s = \underline{3}, \quad l = \underline{8}$$

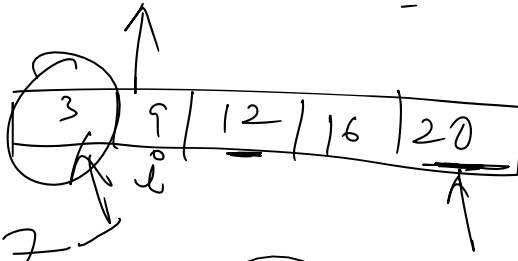
// ~~ans = 5~~

$$\begin{aligned} & \underline{10-2} \quad (8, 3) \quad // \quad 3 \\ & \max(\underline{8+2}, 8) \quad // \quad 10 \end{aligned}$$

1

$$\max(8+2, 8) // 10$$

Ex-2



$$k=3$$

$$ans = 17$$

$$smallest = 3 + k = 6 \quad \text{--- } 0^{th} \text{ index ignore}$$

$$largest = 20 - k = 17 \quad \text{--- } n-1^{th} \text{ index ignore}$$

$$i = 1 \text{ to } n-1$$

$$i=1^o \quad s = \min(s, 9-3) // s=6$$

$$l = \max(l, \underbrace{17}_{3+3} + k) // l=17$$

$$(17, 6)^3 + 3 \Rightarrow 17 - 6 \Rightarrow 11 \quad \text{--- } ans = 11$$

$$\underline{i=2^o}$$

$$s=6 \quad l=17 \quad \underline{ans=11} \quad k=3$$

$$s = \min(s, \underbrace{arr[2]}_{12} - k) // s=6$$

$$(12-3) \Rightarrow 9$$

$$l = \max(l, \underbrace{arr[1]}_{17} + k) // l=17$$

$$\max(17, 12) \Rightarrow 17$$

$$\underline{11}$$

$$\underline{i=3^o}$$

$$s=6 \quad l=17 \quad ans=11 \quad k=3$$

$$s = \min(s, \underline{16-3}) // (\underline{13}, 6) // 6$$

$$l = \max(l, 12+3) // (17, 15) // \underline{\underline{17}}$$

(11)

$$l^0 = 4 \quad s = 6 \quad l = 17 \quad aw = 11 \quad k = 3$$

$$s = \min(s, 20-3) // \underline{\underline{6}}$$

$$l = \max(l, 16+3) // \underline{\underline{(17, 19) 19}}$$

$$l - 8 \quad (13)$$

$$am = \min(13, 11)$$

(11) $am = 11$

(12.5) $am = 11$

Ex-3

1	2	5	8	10	13
0	1	2	3	4	5

 $k = 3$

$$am = 13 - 1 = \underline{\underline{12}}$$

$$smallest = \underline{\underline{4}} // 0^{th} \text{ index ignore}$$

$$largest = 13 - k = \underline{\underline{10}} // n-1^{th} \text{ index ignore}$$

$$l^0 = 1^0 \quad s = 4 \quad l = 10 \quad am = 12 \quad k = 3$$

$$s = \min(s, 2-3)$$

$$m =$$

~~20~~ ~~10~~ (10)

8K1P

$$l^0 = 2^0 \quad s = 7 \quad l = 10 \quad am = 12 \quad k = 3$$

$$s = \min(s, 5-3) // (4, 2) // s=2$$

$$l = \max(l, 2+3) // (10, 3) // l=10$$

$$ans = \min(\underset{\uparrow}{ans}, \underset{\uparrow}{l-s}) // \underline{\underline{ans=8}}$$

(12, 8)

$$i=3^o \quad s=2 \quad l=10 \quad ans=8 \quad k=3$$

$$s = \min(s, 8-3) // \min(2, 5) // \underline{\underline{2}}$$

$$l = \max(l, 5+3) // \max(10, 8) // \underline{\underline{10}}$$

$$ans = \underline{\underline{10-2}}$$

$$\underline{\underline{i=4^o}} \quad s=2 \quad l=10 \quad ans=8 \quad k=3$$

$$s = \min(s, 10-3) // 2$$

$$l = \max(l, 8+3) // \underline{\underline{11}}$$

$$ans = \underline{\underline{11-2}} \quad \underline{\underline{9}}$$

$$i=5^o \quad s=2 \quad l=11 \quad ans=8 \quad k=3$$

$$s = \underline{\underline{13-3}} // 2$$

$$l = \underline{\underline{10+3}} // 13$$

$$\underline{\underline{13-2}} \quad \underline{\underline{11}}$$

$$\underline{\underline{ans=8}} \quad \star \star$$

ans = 8 ★★

T.C - $O(n \log n + n)$

```
int getMinDiff(int arr[], int n, int k) {
    // sort the array
    sort(arr, arr+n);
    int ans = arr[n-1] - arr[0];
    int smallest = arr[0] + k;
    int largest = arr[n-1] - k;
    int mini, maxi;
    for(int i = 1; i < n; i++){
        // skip particular iteration
        if(arr[i] - k < 0) continue;
        mini = min(smallest, arr[i] - k);
        maxi = max(largest, arr[i] + k);
        ans = min(ans, maxi - mini);
    }
    return ans;
}
```

$O(n \log n)$

n

$O(n \log n)$

287. Find the Duplicate Number

Medium 17.2K 2.3K

Companies

Given an array of integers `nums` containing `n + 1` integers where each integer is in the range `[1, n]` inclusive. There is only **one repeated number** in `nums`, return *this repeated number*.

You must solve the problem **without** modifying the array `nums` and uses only constant extra space.

Example 1:

Input: `nums = [1,3,4,2,2]`
Output: 2

Example 2:

Input: `nums = [3,1,3,4,2]`
Output: 3

(1 → 4)

1	3	4	2	2
---	---	---	---	---

1 ~~3~~ $n+1$ integer $n=4 \rightarrow [1, n]$

↓ 4

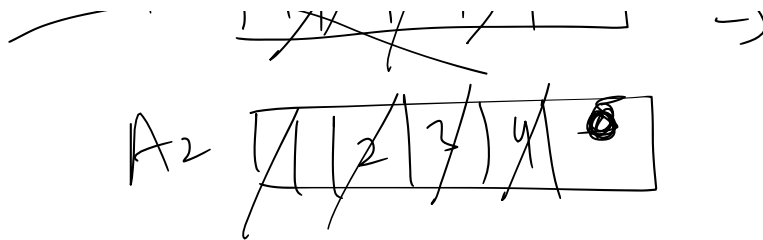
1	2	2	3
---	---	---	---

~~Ans~~

1	3	4	2	2
---	---	---	---	---

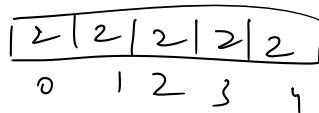
⇒

1 1 1 1

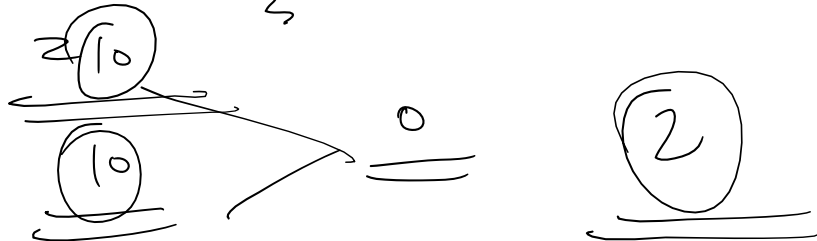


[2,2,2,2,2]

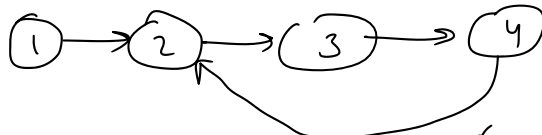
From <https://leetcode.com/problems/find-the-duplicate-number/>



$$2 \times (n+1) / 2$$



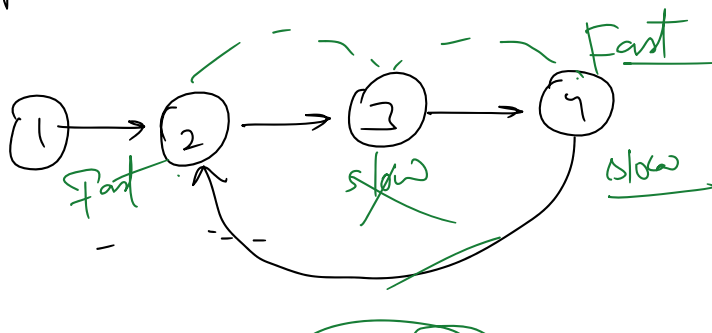
Cycle Detection in linked list



cycle present $\frac{2 \times 4}{2} = 4$

Slow and fast pointer

1 step at a time two step at a time



$n+1$ elements

$[1, n]$

$(0 \rightarrow n)$

Ex 1

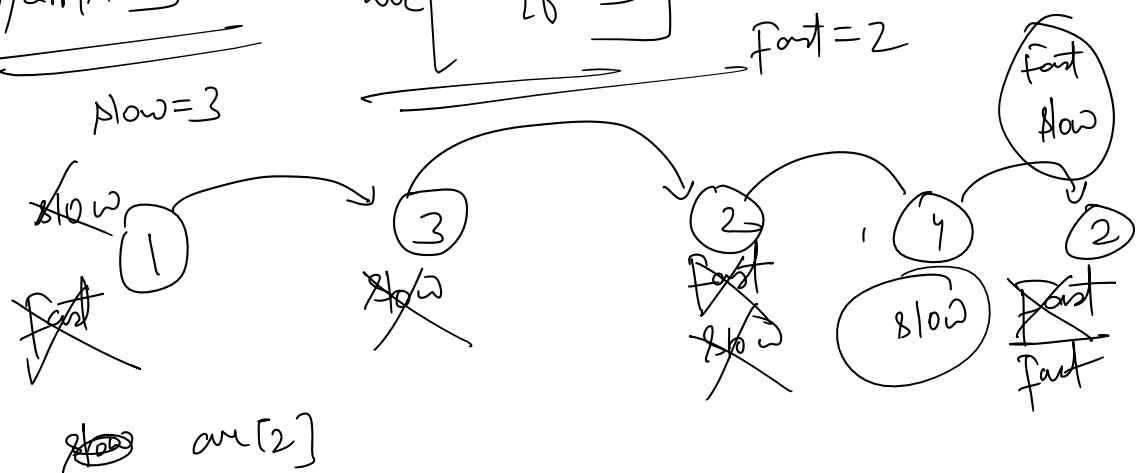
0	1	2	3	4
1	3	4	2	2

slow = arr[0] // 1
fast = arr[0] // 1

arr [2]
arr[4]

slow
1 step
// arr[slow]
slow = 3

fast
2 steps
arr[arr[fast]]
fast = 2

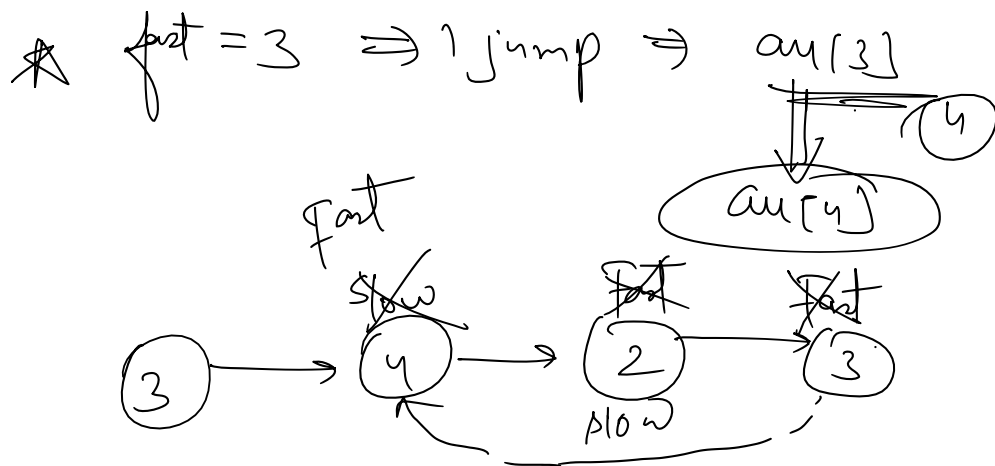


0	1	2	3	4
3	1	3	4	2

slow = arr[0], fast = arr[0]
slow = 3, fast = 3

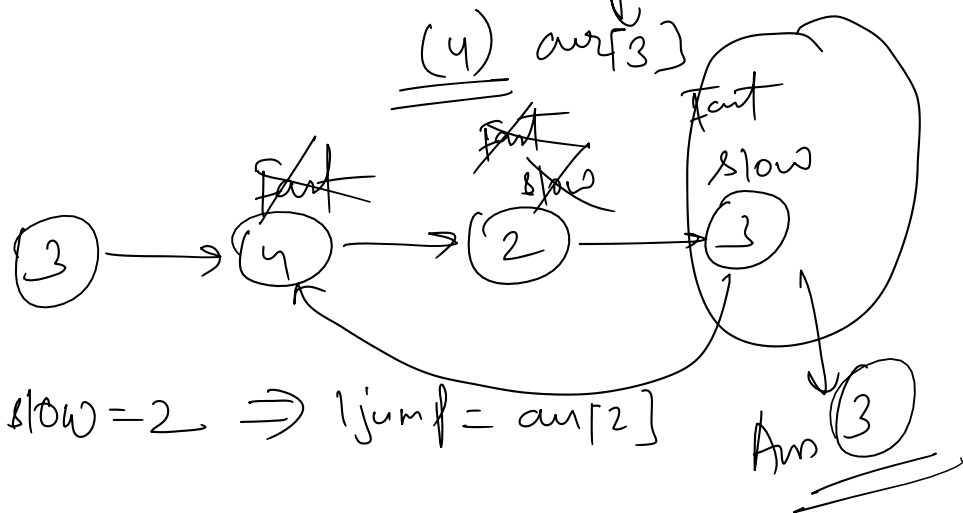


slow = 3 \Rightarrow jump arr[3]



★ $slow = 4 \Rightarrow 1 \text{ jump} = arr[4]$

★ $fast = 2 \Rightarrow 1 \text{ jump} = arr[2] (3)$

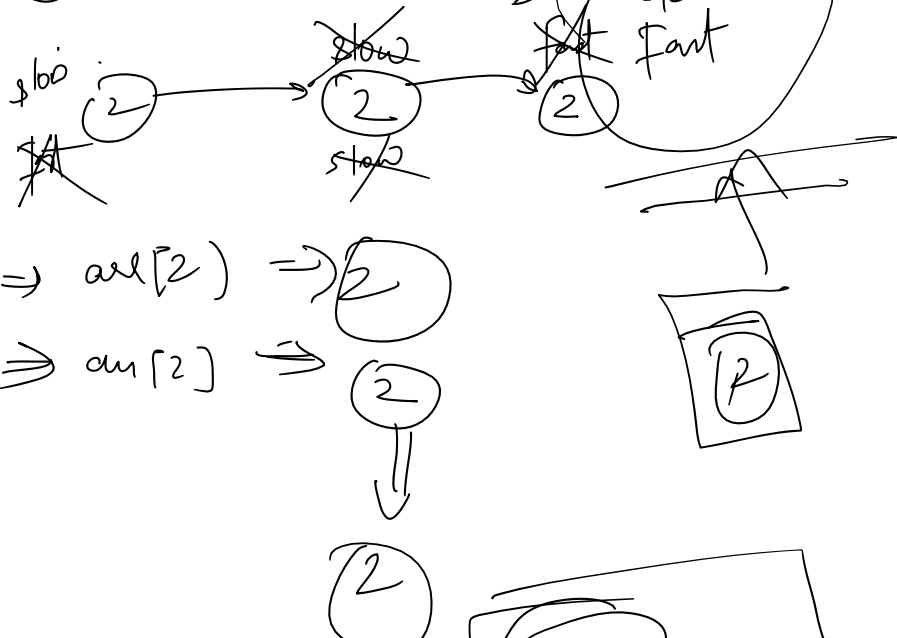


★ $slow = 2 \Rightarrow 1 \text{ jump} = arr[2]$

★

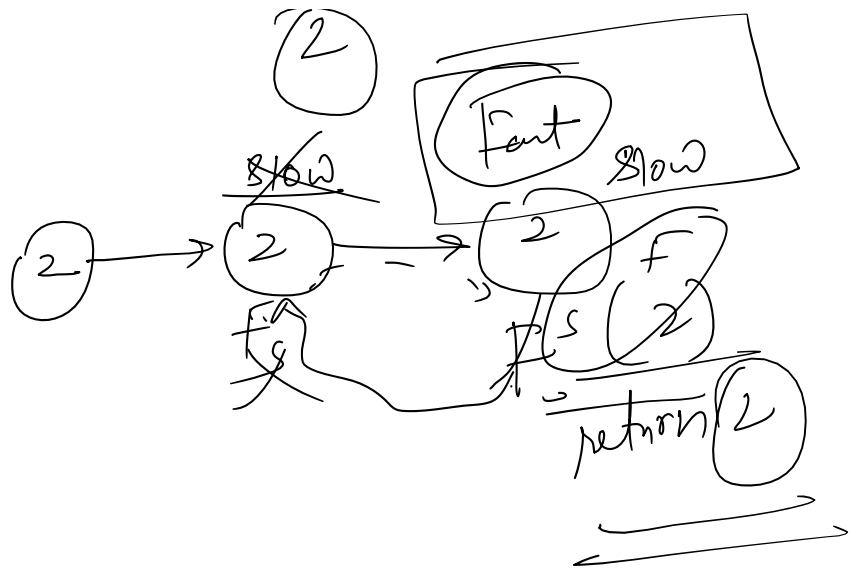
0	1	2	3	4
2	2	2	2	2

$slow = 2$
 $fast = 2$



$slow \Rightarrow 1 \text{ jump} \Rightarrow arr[2] \Rightarrow 2$

$fast \Rightarrow 2 \text{ jump} \Rightarrow arr[2] \Rightarrow 2$

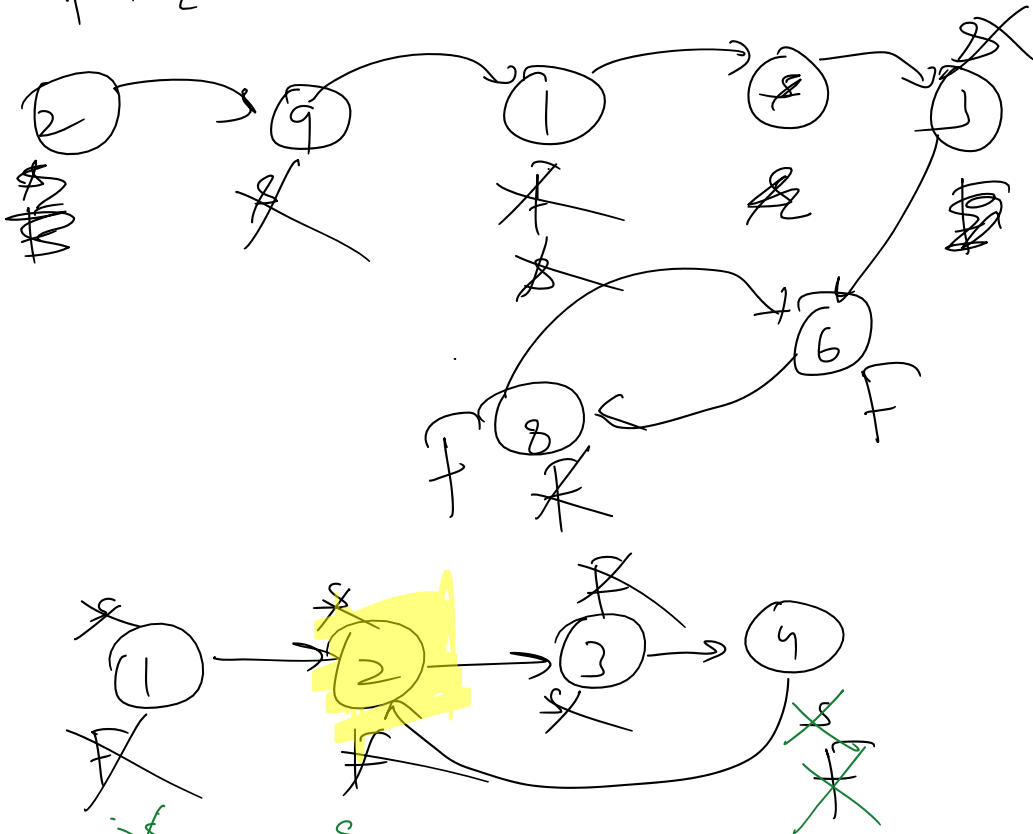


[2,5,9,6,9,3,8,9,7,1]

From <https://leetcode.com/problems/find-the-duplicate-number/>

0	1	2	3	4	5	6	7	8	9
2	5	9	6	9	3	8	9	7	1

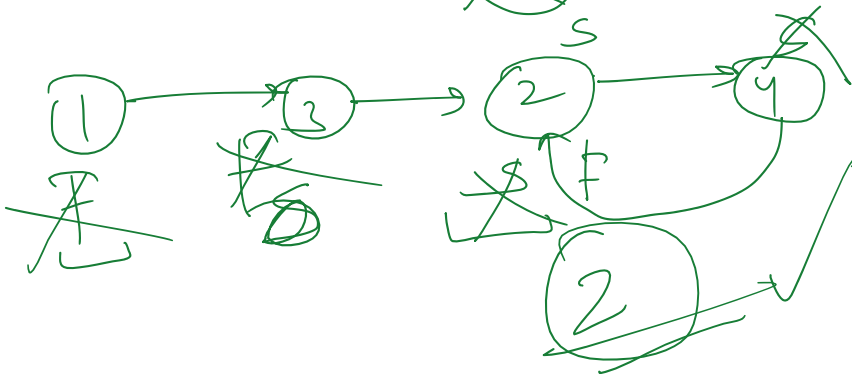
Slow = 2
Fast = 2



~~slow~~ ~~fast~~ ~~slow~~ ~~fast~~
 slow 1 step
 fast 2 step
 s
 f

1	3	4	2	2
0	1	2	3	4

slow = 0
 fast = 1



3	1	3	4	2
0	1	2	3	4

slow = 3
 fast = 3

वापिस नही जाएँ
 F

