91) T(n) = 3T (n/2) + n" \rightarrow T(n)= aT(n/6)+f(n2) a)1, b),1 On compairing a=3, b=2, \f(n)=n2 Now, C = laga = laga = 1.584 ne 2 nº 584 x n2 f(n)>n° T(n)= o(n2) 92) T(n)= 4T(n/2)+n2 \rightarrow a)1, b)1 $a=4, b=2, f(n)=n^2$ C= log 4 = 02 nc = n2 = f(n) = n2 · . T(n) . O (n² lg2n) 93) T(n)=T(n/2)+2" a=1 f(n) z 2" c-lega = legc = 0 nc = 100 = 1 f(n), n° T(n), o(2ⁿ)

(4) T(n) 22 T(n/2) + n -> a=2 b=2, f(n)=n2 C= loga = log_2" negna \$(n) = n° T(n)= 0 (n2 leg n) 95) T(n)= 16T(n/4) + n -> a=16, b=4 f(n) = n $c = \log 16 = \log (4)^2 = 2 \log 4$ = 2nc > n2 7(n) conc .. T(n)=0 (n2)

30) $T(n)=2T(n/2)+n \log n$ $\rightarrow a=2, b=2$ $f(n)=n \log n$ $c=\log 2=1$ $n^c=n^2=n$ $n \log n > n$ $f(n) > n^c$ $f(n) > n^c$ g7) T(n) = 2T(n/2) + n/lagn > a=2, b=2, f(n)= n/legn C= lag 2 = 1 nc=n1=n · n < n · . f(n) < nc $T(n) = \theta(n)$ 98) T(n)=2T(n/4)+n0.51 → a = 2, b = 4, f(n) = n° · 51 $C = \log_{10} a = \log_{10} 2 = 0.5$ $n^{c} = n^{0.5}$ $n^{0.5} < n^{0.5}$ \$(n)>nc · . T(n) = 0 (n°.51) gg) T(n) 2 0.5 T(n/2) + 1/n \rightarrow a=0.5, b=2a 1/1 but here a is 0.5 so me cannet apply Maeter's Theorem. 910) T(n)= 16T(n/4)+n! $\rightarrow a=16, b=4, f(n)=n!$ · · · C = lag a z lag 16 2 2 $n^{c} = n^{2}$ As n/ >n² ·. T(n) = 0(n!)

911) 4T(n/2) + lag n -, a=4, b=e, f(n)=lagn $C = lag_{ba} - lag_{2}^{4} = 2$ $n^{2} = n^{2}$ f(n). legn : lagn < n= f(n)(n° T(n): 0 (nc) = 0 (n2) Q12) T(n) 2 squt(n) T(n/2) + logn _, a=In, b=2 C= lego = legon = 1 legon · · · _ leg_n < leg(n) · . f(n)>nc T(n) = 0 (f(n)) = 0 (lag (n)) (13) T(n)=3T(n/2)+n \rightarrow a=3; b=2; f(n)=nC = laga = lag = 1.5849 $n^{c} = n^{1.5489}$ n< n1.5849 \Rightarrow $f(n) < n^c$ $T(n) = 0 (n^{1.5841})$ Q14) T(n) = 3T(n/3) + sgrt (n) $\rightarrow \alpha=3, b=3$ C = leg a = leg 3 = 1 $n^{c} = n^{2} = n$ As sgut (n) < n f(n) < nc T(n) 20(n)

\$15)
$$T(n) : 4T(n/2) + n$$
 $\rightarrow 0 : 4, b : 2$
 $C : lag a : lag 4 : 2$
 $h^{C} : n^{2}$
 $n < n^{2}$ (for any constant)

 $f(n) < n^{C}$
 $f(n) = 0 (n^{2})$

\$16) $T(n) = 3T(n/4) + n lag n$
 $\rightarrow a : 3, b : 4, f(n) = n lag n$
 $C : lag a : lag 3 : 0.792$
 $n^{C} : n^{C} : 192$
 $n^{C} : 192$
 $n^{C} : 192$
 $n^{C} : 193$
 $n^{C} : 193$

T(n) = 0 (n2) 920) T(n) = 64T(n/8) - n2 lagn -> a=64 b=8 C = log a = log 64 = log (8) $N^{c} = n^{2}$ $\frac{1}{T(n)} = o(n^2 \log n)$ g21) T(n)= 7T (n/3)+n2 $\rightarrow a = 7, b = 3; f(n) = n^2$ C= loga = log37 = 1.7712 nc = n1.7712 n1.7712 < n2 T(n) = 0 (n2) 822) T(n)= T(n/2)+n(2-(esn) \rightarrow a=1,b=2C= laga = lag1 = 0 n° = n° = 1 n(2-(cosn)) n^{c} T(n) = o (n(2-cosn))

g19) T(n)=4T(n/2) + n/logn

 $c = \log a = \log 4 = 2 \log n$

lagn (n²