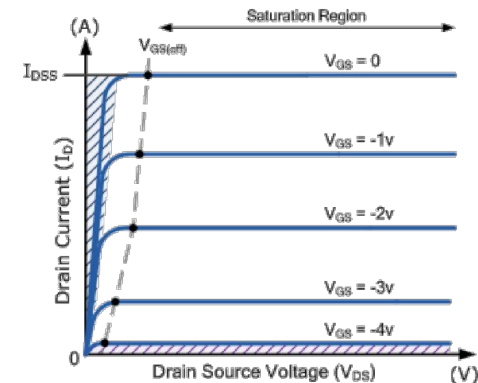
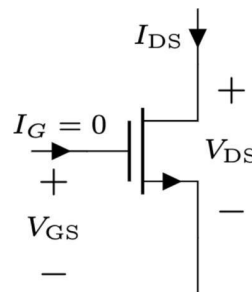
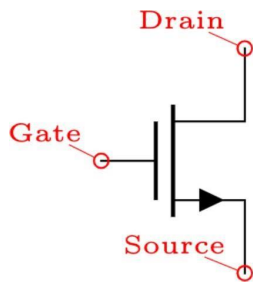


# Lecture-8:

## BJT

# Transistors as Digital Switch

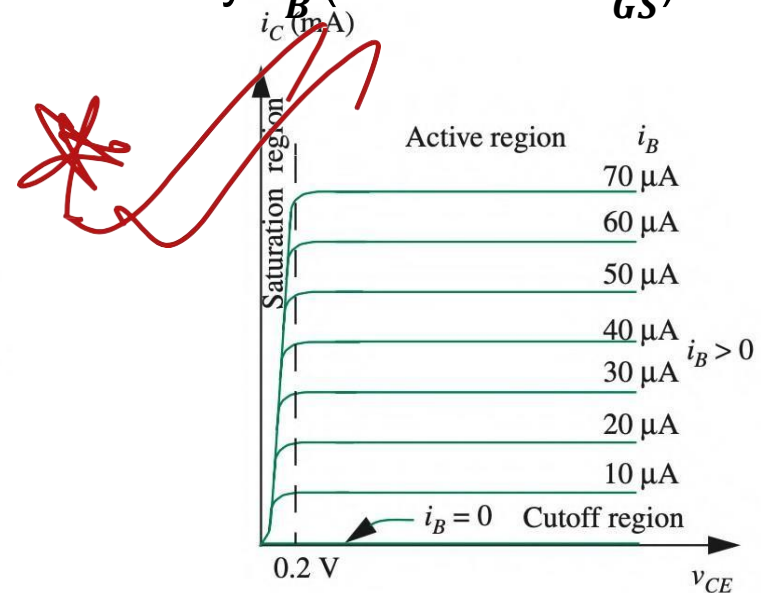
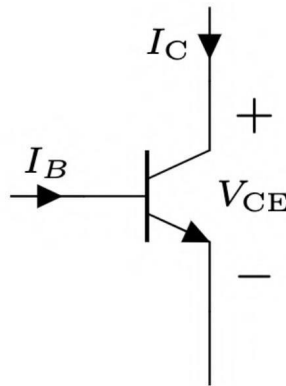
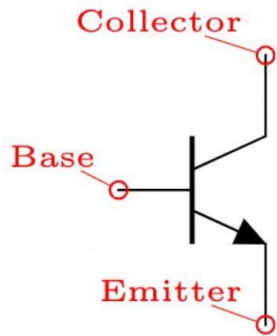
- Transistors are 3 terminal non-linear devices, can be used as switch
- 2 types – **Voltage Controlled**, **Current Controlled**
- **M**etal **O**xide **S**emiconductor **F**ield **E**ffect **T**ransistor (**MOSFET**) are **voltage controlled**
- Control,  $C = V_{GS}$ . The IV characteristics ( $I_{DS}$  vs  $V_{DS}$ ) depends on  $V_{GS}$
- Actual dependency is complex.
- Will start with a simple (but approximate) one – **S-Model** (Switch Model)



# Bipolar Junction

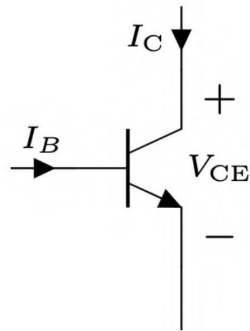
## Transistor

- **Current-controlled** transistor, 3 terminals – Base, Emitter, Collector
- $IV$  between  $C$  and  $E$  ( $I_C$  vs  $V_{CE}$ ) is controlled by base current,  $I_B$
- $IV$  is quite like MOSFET, but there are some differences
- We can use a S-model here too, but controlled by  $I_B$  (instead of  $V_{GS}$ )



# ★ BJT vs MOSFET - Differences

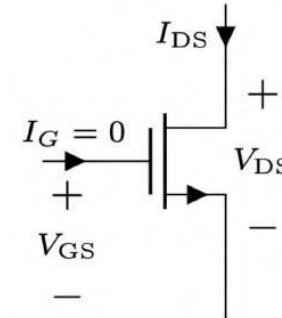
## BJT



**Current** controlled,  $I_B$  controls ( $I_C$  vs  $V_{CE}$ )

**Base** current,  $I_B$ , is the control. Hence  $I_E \neq I_C$ , rather  
 $I_E = I_C + I_B$

## MOSFET

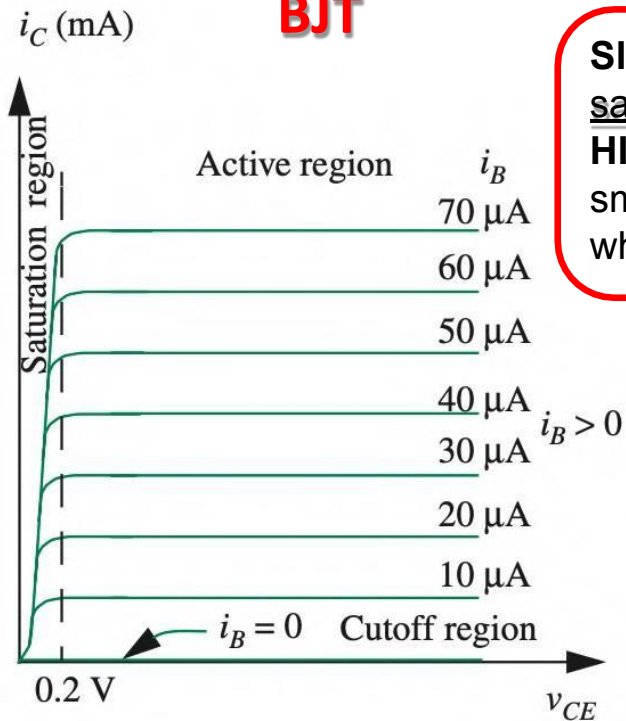


**Voltage** controlled,  $V_{GS}$  controls ( $I_{DS}$  vs  $V_{DS}$ )

**Gate** current,  $I_G$ , is always 0. Hence  $I_S = I_D = I_{DS}$ .

# BJT vs MOSFET - Differences

## BJT

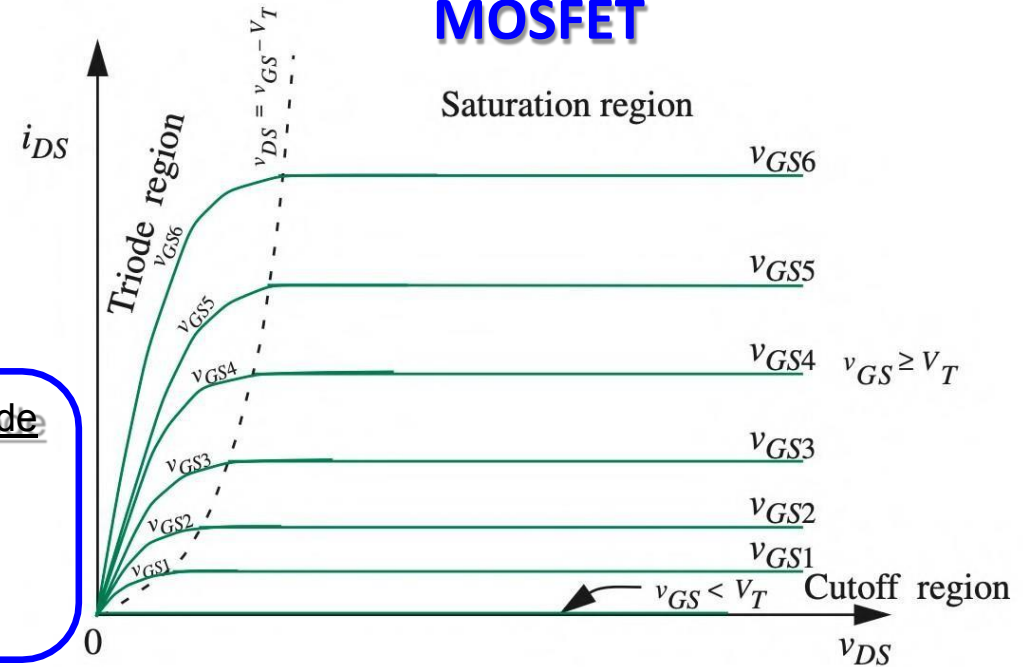


Slope in the saturation region is **HIGH**, hence very small resistance when "ON"

Slope in the Triode region is **LOW**, hence significant resistance when "ON"

Current in **active** region changes linearly with control  $I_B$ .  
Hence,  $I_C \propto I_B$

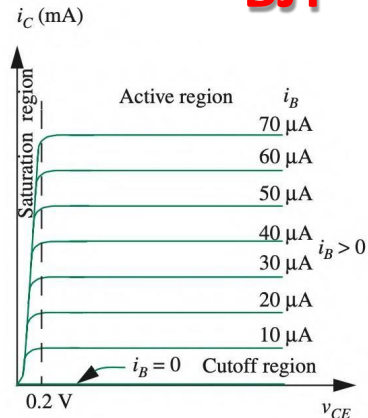
## MOSFET



Current in **Saturation** region changes quadratically with control  $V_{GS}$ .  
Hence,  $I_{DS} \propto V_{GS}^2$

# BJT vs MOSFET - Similarities

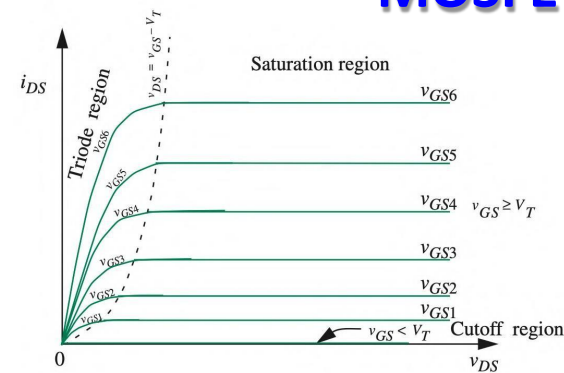
## BJT



- **Saturation** mode for small  $V_{CE}$  ( $< 0.2$  V)
- Approximately Short circuit in **Saturation** mode ( $I_B$  **HIGH**)
- Open circuit in **Cutoff** mode ( $I_B = 0$ )
- Can use as a switch  $\Rightarrow$  S-Model!

$$V_{BE} < 0.7$$

## MOSFET



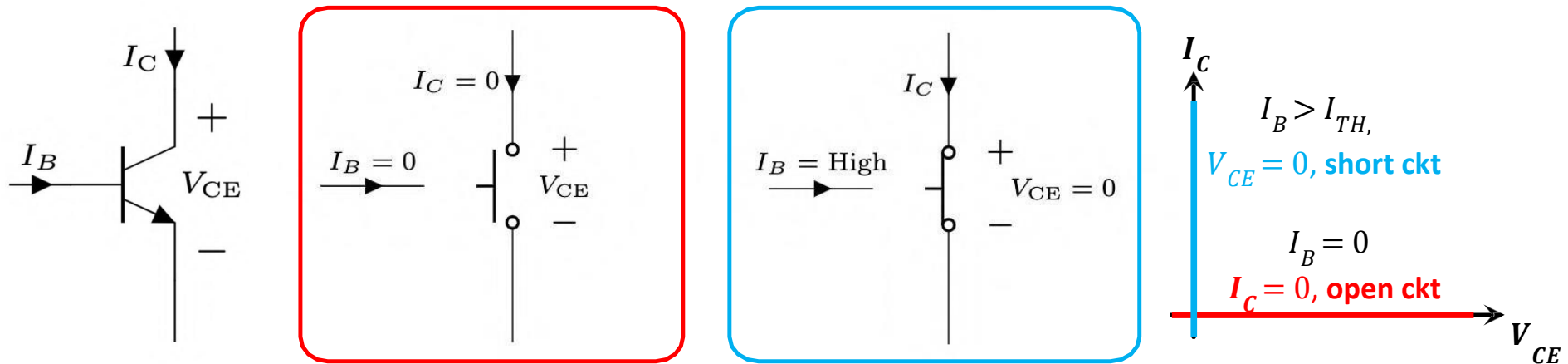
- **Triode** mode for small  $V_{DS}$  ( $< V_{OV}$ )
- Approximately Short circuit in **Triode** mode ( $V_{GS}$  **HIGH**)
- Open circuit in **Cutoff** mode ( $V_{GS} < V_T = 0$ )
- Can use as a switch  $\Rightarrow$  S-Model!

# BJT S-Model

- The BJT (approximately) behaves like a switch

- $C = I_B$ . Here,  $C = "0" \Rightarrow I_B = 0$ , and  $C = "1" \Rightarrow I_B > I_{TH}$

	Representation
Logic 0	$I_B = 0$
Logic 1	$I_B > I_{TH}, I_B = HIGH$



# Current-Controlled Logic Gates using BJT

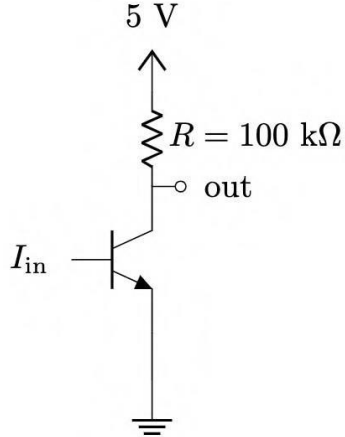
- Just replace switches with BJTs!
- Major problem: Cannot cascade!

(Why?)

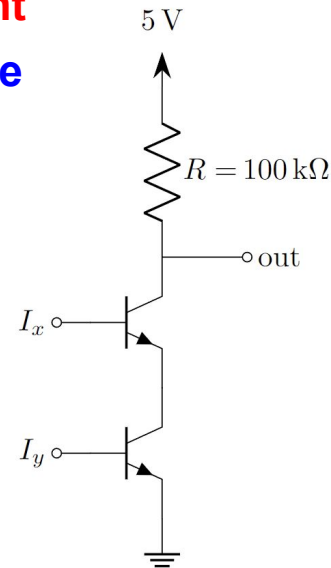
• Input Logic Variable:

- Output Logic Variable:

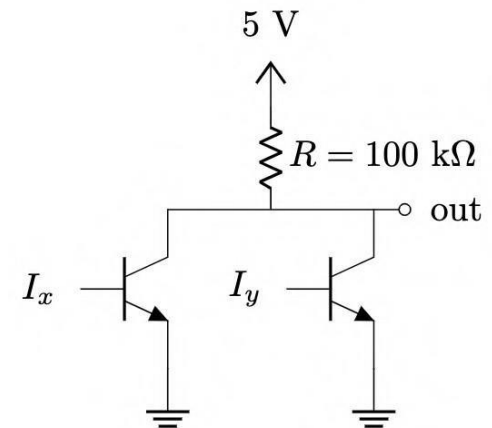
**Current**  
**Voltage**



BJT Inverter (NOT Gate)



BJT NAND Gate

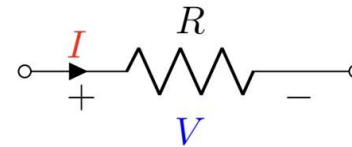


BJT NOR Gate

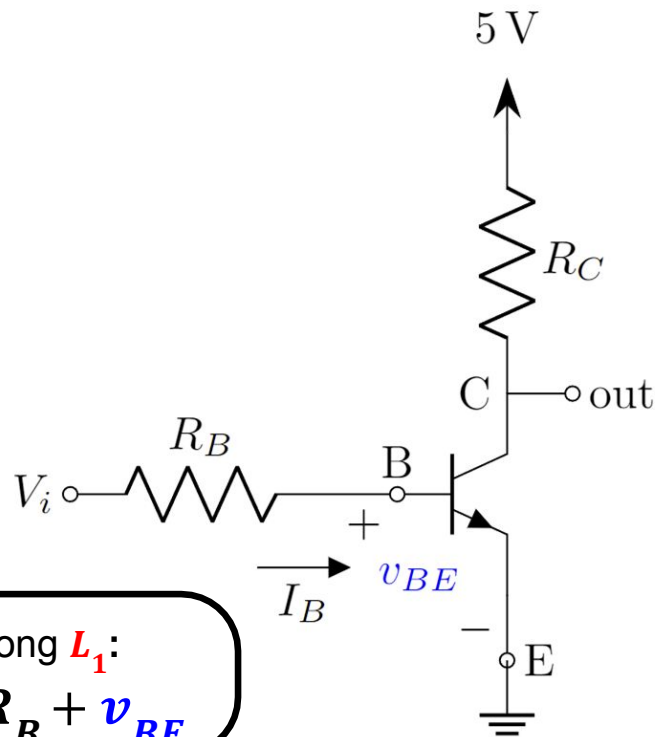


# From Current Controlled to Voltage Controlled

How to convert current  $I$  into voltage  $V$ ?



$$V = IR$$



KVL along  $L_1$ :

$$V_i = I_B R_B + v_{BE}$$

$$V_i = I_B R_B + v_{BE}$$

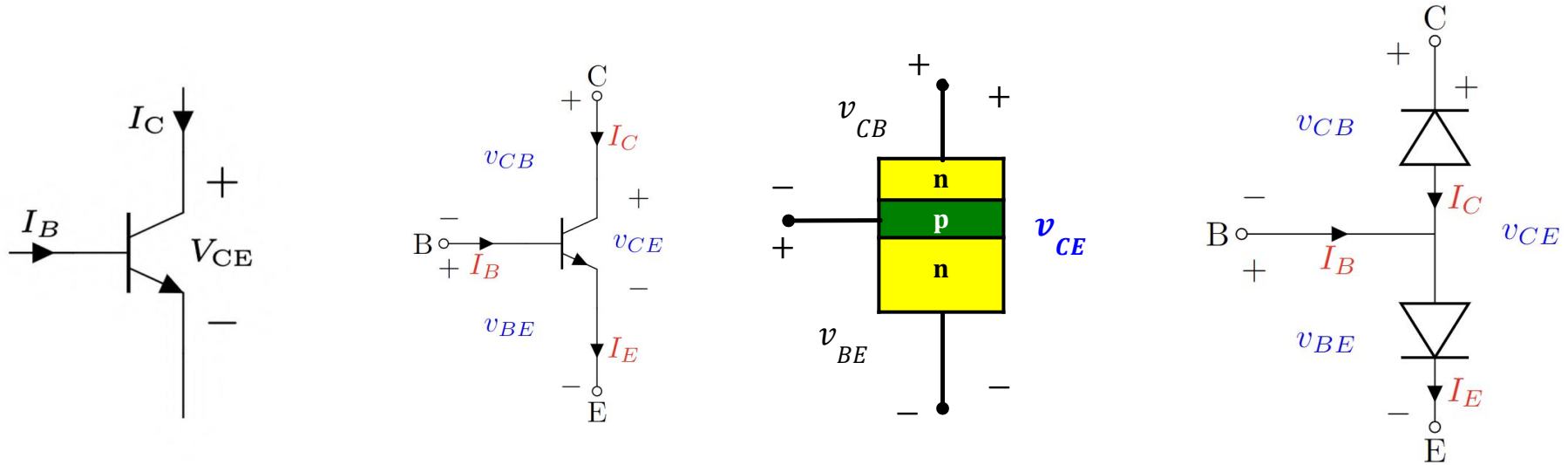
$$I_B = \frac{V_i - v_{BE}}{R_B}$$

$v_{BE}$  depends on  $I_B$ .

How?

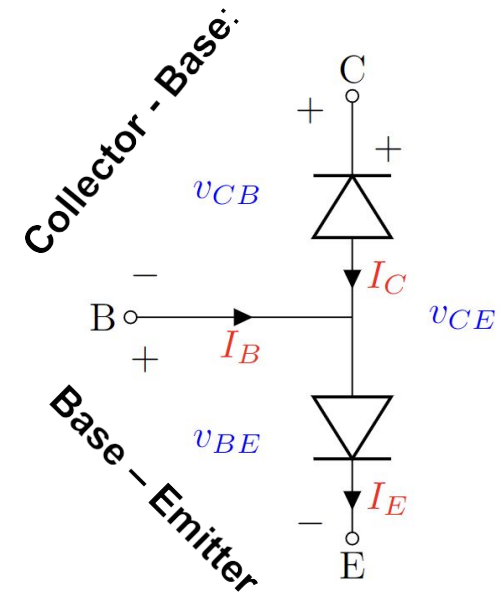
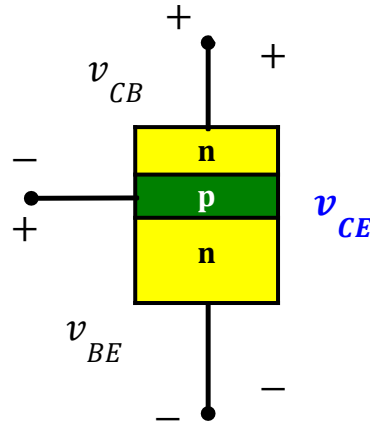
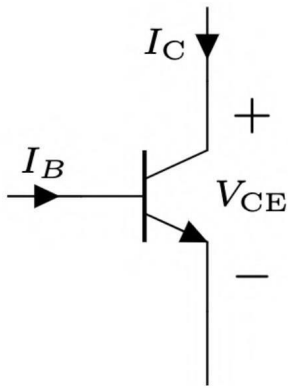
# Parameters of BJT

A BJT can be thought of as two “pn” junctions placed back-to-back.



1st pn junction: Across **Base – Emitter**: Voltage  $v_{BE}$   
2nd pn junction: Across **Collector - Base**: Voltage  $v_{CB}$

# Parameters of BJT

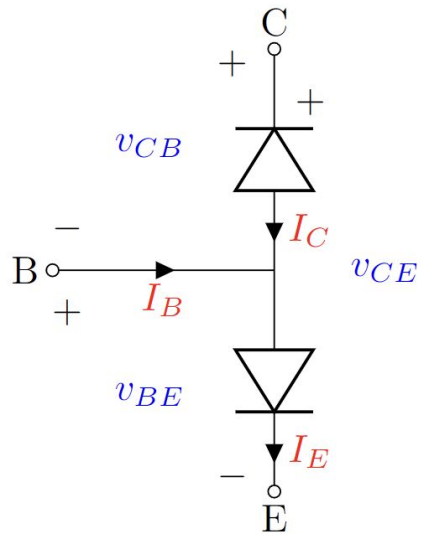


**Base – Emitter:** Emitter is highly-doped. So, **BE** junction has higher cut in voltage ( $V_{BE} = 0.7 \text{ V}$  usually)

**Base – Collector:** Collector is less-doped (compared to Emitter).  
So, **BC** junction has **lower** cut in voltage ( $V_{BC} = 0.5 \text{ V}$  usually)

# Parameters of BJT

A BJT can be thought of as two “pn” junctions placed back-to-back.



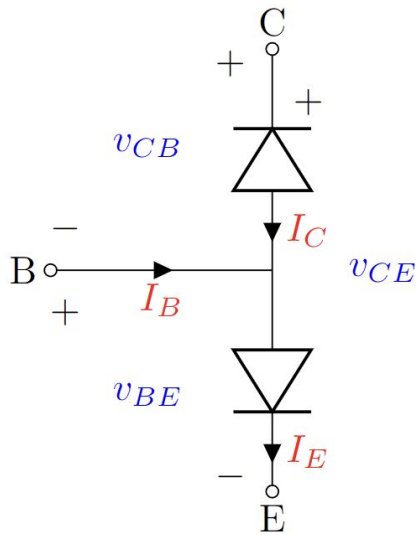
Modes	BE Junction	$v_{BE}$	CB Junction	$v_{CB}$	$v_{CE}$
Cut-off	Reverse Bias	$v_{BE} < 0.7 \text{ V}$	Reverse Bias	$v_{CB} > -0.4 \text{ V}$	
Active	Forward Bias	$v_{BE} = 0.7 \text{ V}$	Reverse Bias	$v_{CB} > -0.4 \text{ V}$	$v_{CE} > 0.3 \text{ V}$
Saturation	Forward Bias	$v_{BE} = 0.7 \text{ V}$	Forward Bias	$v_{CB} = -0.5 \text{ V}$	$v_{CE} = 0.2 \text{ V}$
Reverse Active	Reverse Bias	$v_{BE} < 0.6 \text{ V}$	Forward Bias	$v_{CB} = -0.5 \text{ V}$	$v_{CE} < 0.1 \text{ V}$

1st pn junction: Across **Base – Emitter**: Voltage  $v_{BE}$   
 2nd pn junction: Across **Collector - Base**: Voltage  $v_{CB}$

$$v_{CE} = v_{CB} + v_{BE}$$

# Parameters of BJT

Current relationships between the three currents in an npn BJT.



$$I_B + I_C = I_E$$

$$I_C = \beta I_B$$

$$I_C = \alpha I_E$$

$\beta$ : Common Emitter Current Gain  
 $\alpha$ : Common Base Current Gain

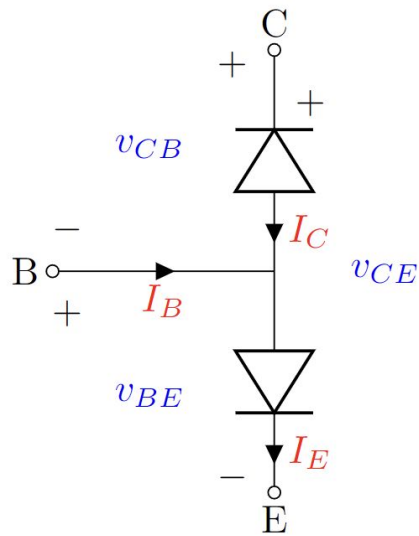
Only valid for active mode

1st pn junction: Across **Base – Emitter**: Voltage  $v_{BE}$   
2nd pn junction: Across **Collector - Base**: Voltage  $v_{CB}$

$$v_{CE} = v_{CB} + v_{BE}$$

# Parameters of BJT

A BJT can be thought of as two “pn” junctions placed back-to-back.



Modes	Conditions!
Cut-off	$v_{BE} < 0.7\text{ V}$ and $v_{CB} > -0.4\text{ V}$
Active	$v_{BE} = 0.7\text{ V}$ and $v_{CE} > 0.3\text{ V}$
Saturation	$v_{BE} = 0.7\text{ V}$ and $v_{CE} = 0.2\text{ V}$ and $I_C < \beta I_B$
Reverse Active	$v_{BC} = 0.7\text{ V}$ and $v_{EC} > 0.1\text{ V}$

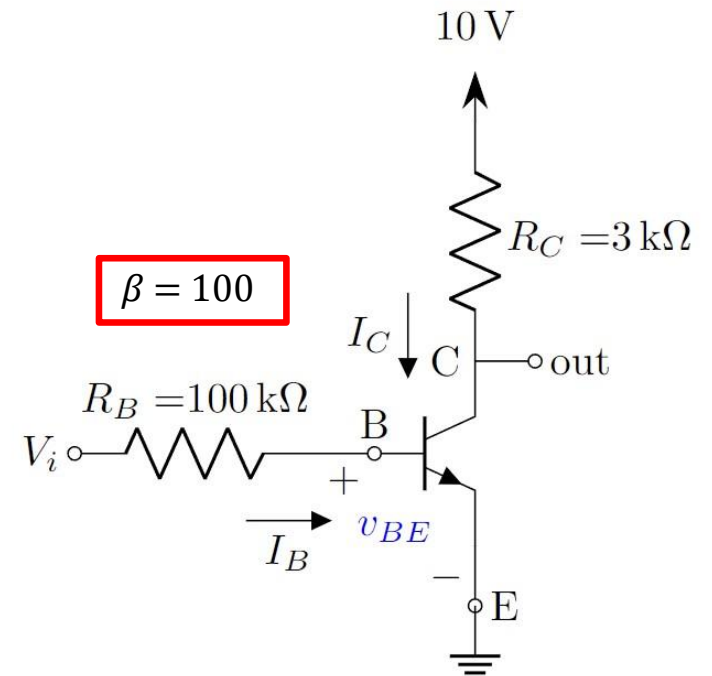
1st pn junction: Across **Base – Emitter**: Voltage  $v_{BE}$   
 2nd pn junction: Across **Collector - Base**: Voltage  $v_{CB}$

$$v_{CE} = v_{CB} + v_{BE}$$



# BJT Problem 1

Analyze the circuit to find  $I_C$  and  $v_{out}$  using the Method of Assumed State. Here, the input of the BJT is  $V_i = 1\text{ V}$ . You must validate your assumptions.



# BJT Problem 1

Analyze the circuit to find  $I_C$  and  $v_{out}$  using the Method of Assumed State. Here, the input of the BJT is  $V_i = 1\text{ V}$ . You must validate your assumptions.

## Assume:

Let the BJT be in **ACTIVE** mode

$$\text{So, } v_{BE} = 0.7\text{ V} \\ v_{CE} > 0.3\text{ V}$$

## Solve:

Equations:

$$I_B = \frac{V_i - v_{BE}}{R_B} = \frac{1 - 0.7}{100} \text{ mA} = 3\text{ }\mu\text{A}$$

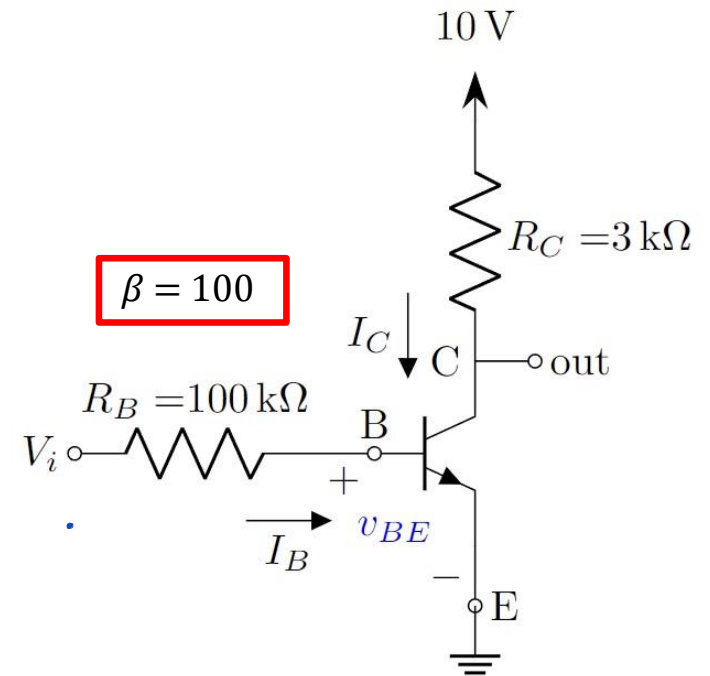
$$I_C = \beta I_B = 100 \times 3 \times 10^{-3} \text{ mA} = 0.3\text{ mA}$$

$$v_{out} = 10 - I_C R_C = (10 - 0.3 \times 3) \text{ V} = 9.1\text{ V}$$

**Verify:** For **ACTIVE** condition  $\rightarrow v_{CE} > 0.3\text{ V}$

$$\text{Here, } v_{CE} = v_{out} = 9.1\text{ V} > 0.3\text{ V}$$

**Assumption is Correct!**





# BJT Problem 1

Analyze the circuit to find  $I_C$  and  $v_{out}$  using the Method of Assumed State. Here, the input of the BJT is  $V_i = 5\text{ V}$ . You must validate your assumptions.

## Assume:

Let the BJT be in **ACTIVE** mode

So,  $v_{BE} = 0.7\text{ V}$   
 $v_{CE} > 0.2\text{ V}$

## Solve:

Equations:

$$I_B = \frac{V_i - v_{BE}}{R_B} = \frac{5 - 0.7}{100} \text{ mA} = 43 \mu\text{A}$$

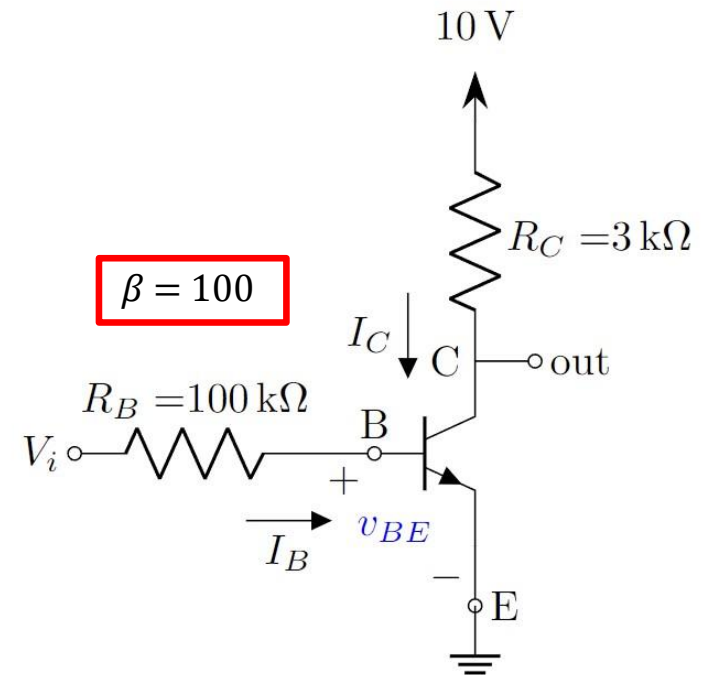
$$I_C = \beta I_B = 100 \times 43 \times 10^{-3} \text{ mA} = 4.3 \text{ mA}$$

$$v_{out} = 10 - I_C R_C = (10 - 4.3 \times 3) \text{ V} = -2.9 \text{ V}$$

**Verify:** For **ACTIVE** condition  $\rightarrow v_{CE} > 0.2\text{ V}$

Here,  $v_{CE} = v_{out} = -2.9\text{ V} < 0.2\text{ V}$

**Assumption is Wrong!**



# BJT Problem 1

Analyze the circuit to find  $I_C$  and  $v_{out}$  using the Method of Assumed State. Here, the input of the BJT is  $V_i = 5\text{ V}$ . You must validate your assumptions.  $V_{BE, sat} = 0.8$

## Assume:

Let the BJT be in **Saturation** mode

So,  $v_{BE} = 0.7\text{ V}$  and  $I_C < \beta I_B$

## Solve:

Equations:  $I_B = \frac{V_i - v_{BE}}{R_B} = \frac{5 - 0.7}{100} \text{ mA} = 43 \mu\text{A}$

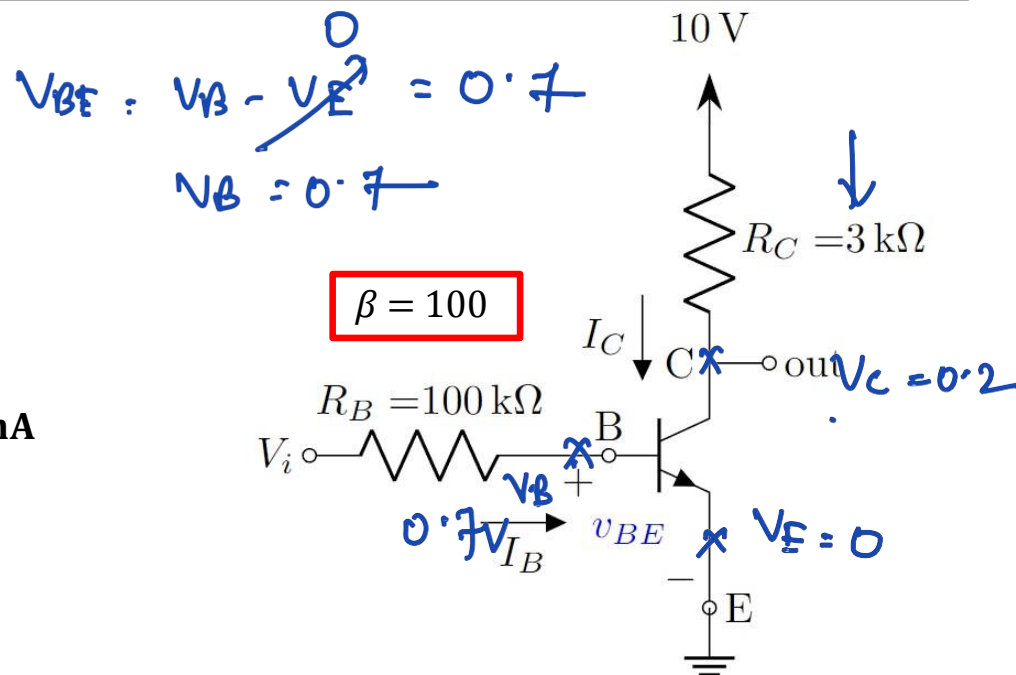
$$\frac{I_C}{I_B} < \beta \quad \checkmark \quad I_C = \beta I_B \quad \frac{10 - v_{CE}}{R_C} = \frac{10 - 0.2}{3} \text{ mA} = 3.27 \text{ mA}$$

$$v_{out} = v_{CE} = 0.2 \text{ V}$$

**Verify:** For **Saturation** condition  $\rightarrow I_C < \beta I_B$

Here,  $\beta = 100$

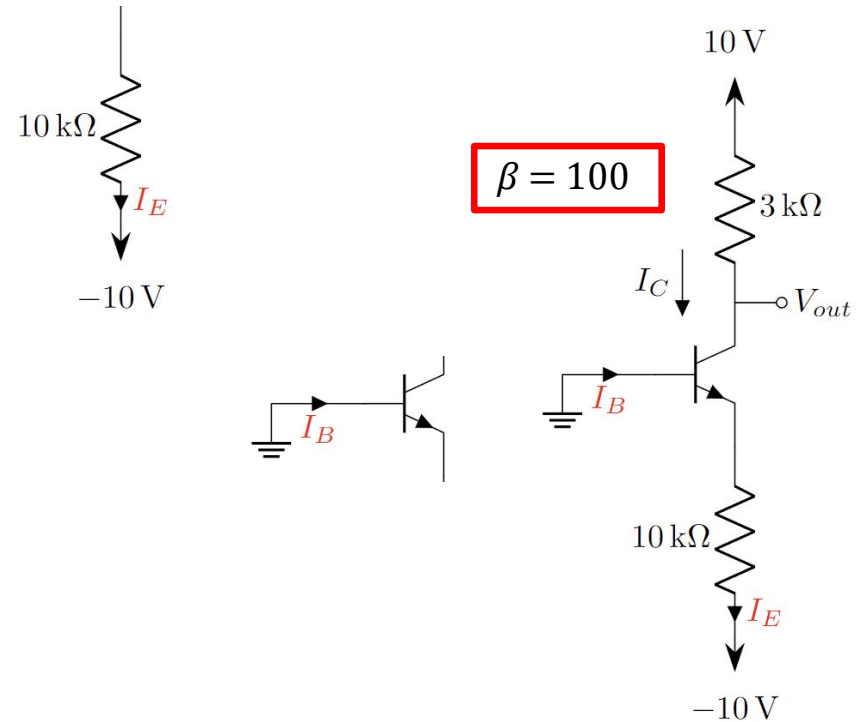
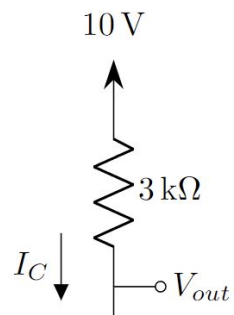
$$\frac{I_C}{I_B} = \frac{3.27}{0.043} = 76 < 100$$



**Assumption is Correct!**

# BJT Problem 2

Analyze the circuit to find  $I_B$ ,  $I_C$ ,  $I_E$  and  $v_{out}$  using the Method of Assumed State. You must validate your assumptions.



# BJT Problem 2

Analyze the circuit to find  $I_B$ ,  $I_C$ ,  $I_E$  and  $v_{out}$  using the Method of Assumed State. You must validate your assumptions.

## Assume:

Let the BJT be in **Active** mode

$$\text{So, } v_{BE} = 0.7 \text{ V} \\ v_{CE} > 0.2 \text{ V}$$

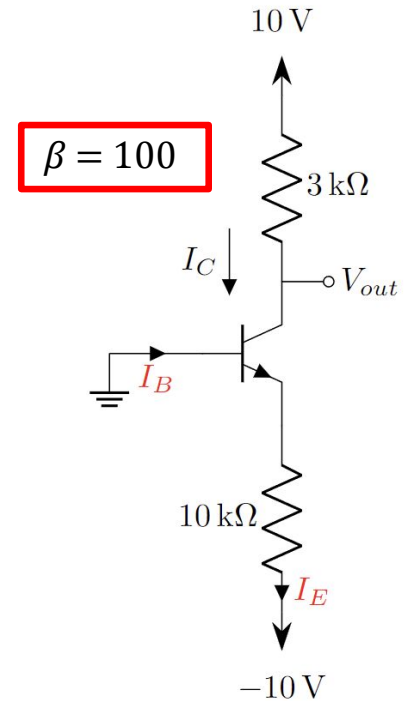
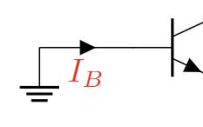
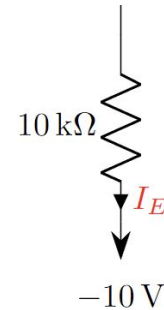
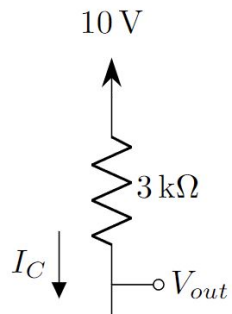
## Solve:

Equations:

$$I_E = \frac{v_E - (-10)}{10} = \frac{-0.7 + 10}{10} \text{ mA} = \mathbf{0.93 \text{ mA}}$$

$$I_B = \frac{1}{\beta} I_C = \frac{1}{\beta} \cdot \alpha I_E = \frac{1}{\beta} \cdot \frac{\beta}{\beta + 1} I_E = \frac{1}{\beta + 1} I_E \approx \mathbf{9.21 \text{ }\mu\text{A}}$$

$$v_{out} = v_C = 10 - 3I_C = 10 - 3\beta I_B \\ = (10 - 3 \cdot 100 \cdot 9.207 \times 10^{-3}) \text{ V} \\ = \mathbf{7.237 \text{ V}}$$



# BJT Problem 2

Analyze the circuit to find  $I_B$ ,  $I_C$ ,  $I_E$  and  $v_{out}$  using the Method of Assumed State. You must validate your assumptions.

## Assume:

Let the BJT be in **Active** mode

So,  $v_{BE} = 0.7 \text{ V}$

$v_{CE} > 0.2 \text{ V}$

## Solve:

Equations:  $I_E = 0.93 \text{ mA}$

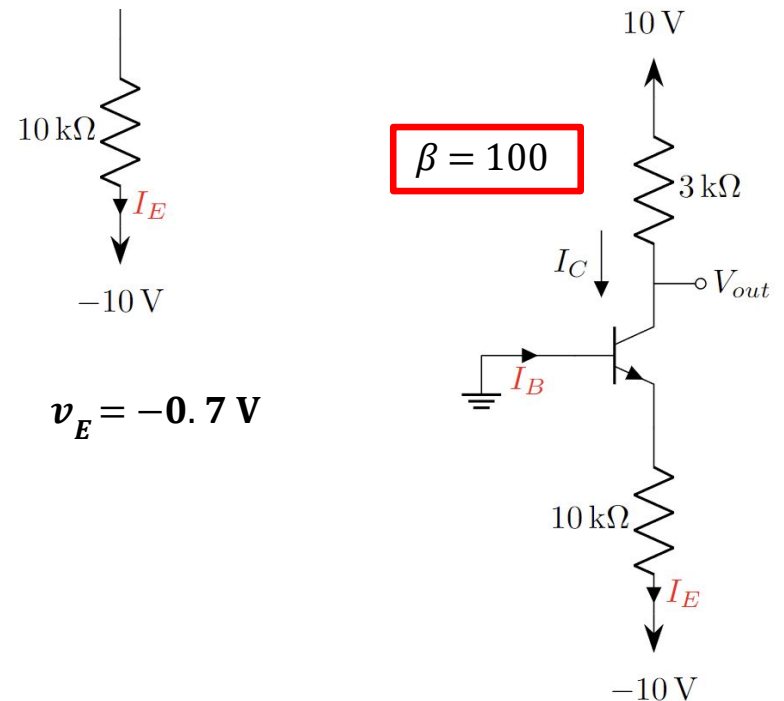
$I_B = 9.21 \text{ } \mu\text{A}$

$v_{out} = v_C = 7.237 \text{ V}$        $v_B = 0 \text{ V}$

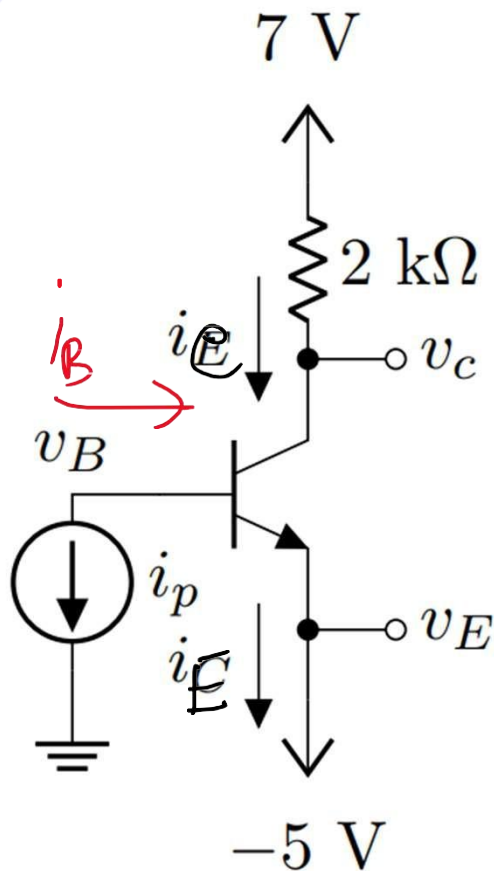
**Verify:** For **ACTIVE** condition  $\rightarrow v_{CE} > 0.2 \text{ V}$

Here,  $v_{CE} = 7.237 + 0.7 \text{ V} = 7.937 \text{ V} > 0.2 \text{ V}$

**Assumption is Correct!**



## Example 2



Analyze the circuit above to find  $i_B$ ,  $i_C$ ,  $i_E$  and  $v_{CE}$ . Assume, the BJT is in Saturation. Here, use the Method of Assumed State. You must validate your assumptions. Assume,  $i_p = -1\text{mA}$ ;  $\beta = 100$

Sol<sup>n</sup>:

$$i_B = -i_p = -(-1) = 1\text{ mA}$$

$$V_E = -5\text{V}$$

In saturation mode

So,  $V_{BE} = 0.8\text{ V}$  &

$$V_{CE} = 0.2\text{ V}$$

$$\Rightarrow V_C - V_E = 0.2\text{V} \Rightarrow V_C = 0.2 + V_E = 0.2 + (-5)$$

$$\therefore V_C = -4.8\text{ V}$$

$$i_C = (7 - V_C) / 2 = (7 + 4.8) / 2 = 5.9\text{ mA}$$

$$i_E = i_C + i_B = 6.9\text{ mA}$$

Verify:

$$\beta = 100$$

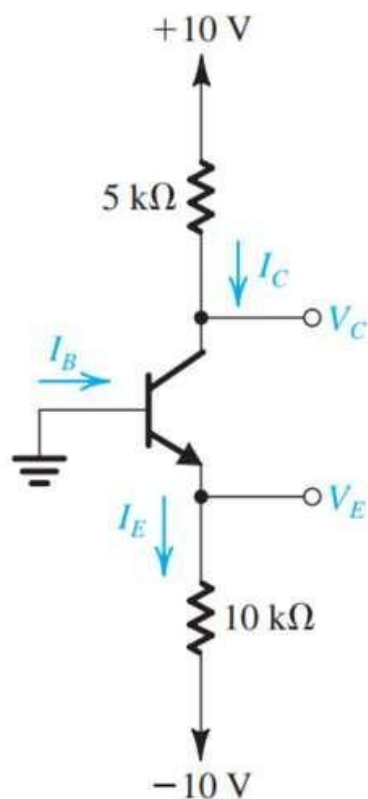
$$i_C / i_B = 5.9 / 1 = 5.9 < \beta$$

$\therefore$  Assumption Correct

# Example 7

In the circuit shown in Fig. the voltage at the emitter was measured and found to be  $-0.7\text{ V}$ .

If  $\beta = 50$ , find  $I_E$ ,  $I_B$ ,  $I_C$ , and  $V_C$ .



**Sol<sup>n</sup>:**

$$I_E = \frac{V_E - (-10)}{10\text{ k}\Omega} = \frac{-0.7 + 10}{10} = 0.93\text{ mA}$$

$$\alpha = \frac{\beta}{\beta + 1} = \frac{50}{51}$$

Assuming forward active mode,

$$I_C = \alpha I_E = 0.9118\text{ mA}$$

$$V_C = 10 - 5I_C = 5.44\text{ V}$$

So,  $V_{CE} = V_C - V_E = 6.141\text{ V} > 0.2\text{ V}$  so, forward active mode  
Assumption correct!

$$I_B = I_E - I_C = 18.2\text{ uA}$$

## Example 8

Analyze the circuit above to find  $i_C$ ,  $i_E$ ,  $i_B$ , and  $v_{o1}$ .  
Here, use the Method of Assumed State.

**Sol<sup>n</sup>:**

Assuming forward active mode,

$$V_{BE} = 0.7 \text{ V} \Rightarrow V_B - V_E = 0.7 \text{ V} \therefore V_B = 0.7 \text{ V} = V_C$$

So,  $V_{CE} = V_C - V_E = 0.7 \text{ V} > 0.2 \text{ V}$  so, forward active mode

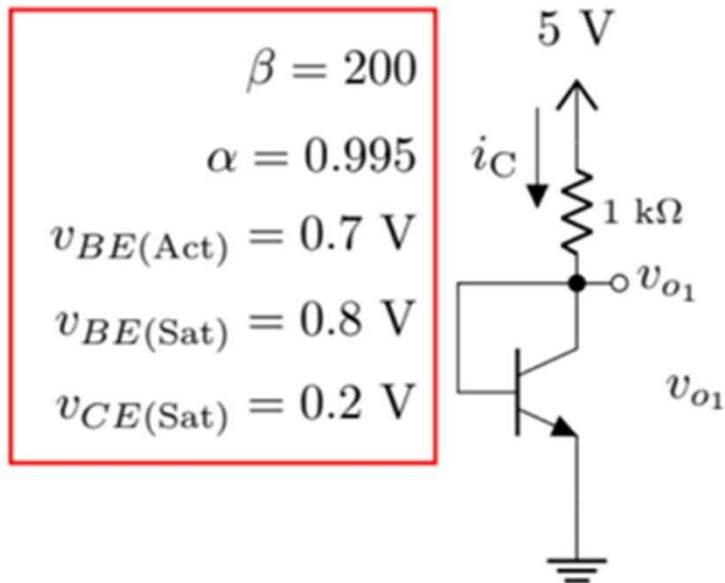
Assumption correct!

$$i_C = \frac{5 - V_C}{1 \text{ k}\Omega} = \frac{5 - 0.7}{1} = 4.3 \text{ mA}$$

$$I_C = \alpha I_E$$

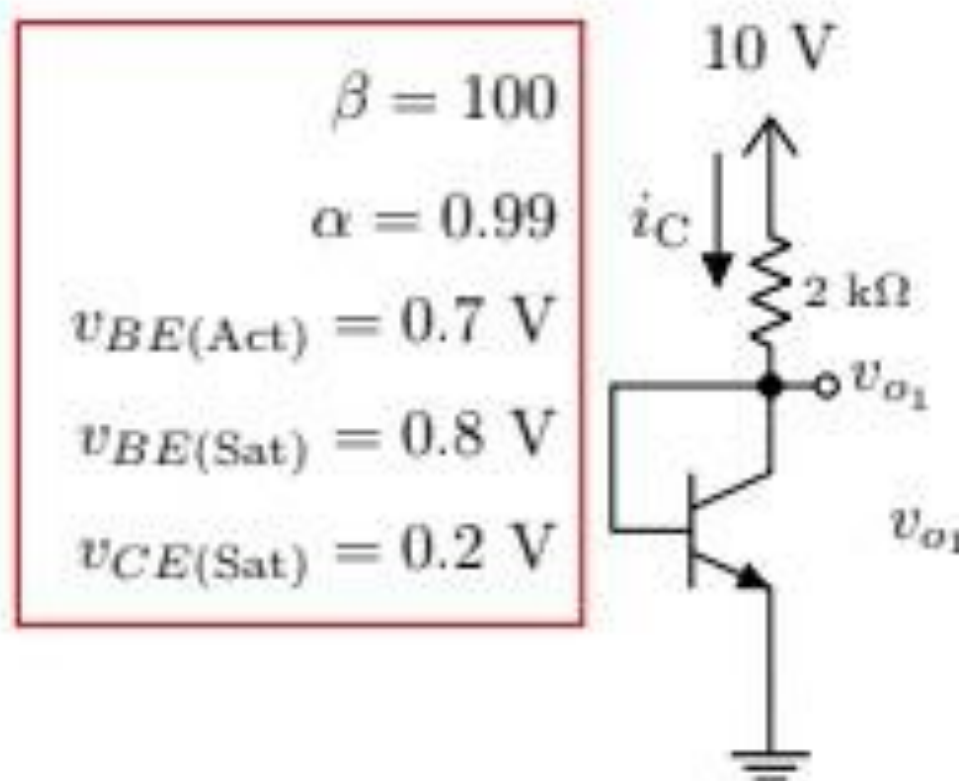
$$\therefore I_E = 4.3 / 0.995 = 4.3216 \text{ mA}$$

$$I_B = I_E - I_C = 21.6 \text{ }\mu\text{A}$$



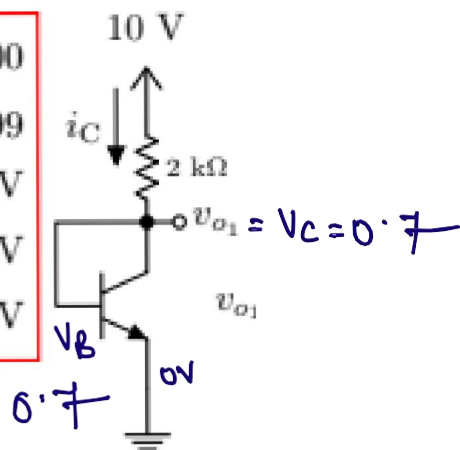


**Analyze** the Ckt - 2 to find  $i_C$  and  $v_{O_1}$  using the Method of Assumed State. **Validate** your assumptions.



Ckt - 2

$$\begin{aligned}\beta &= 100 \\ \alpha &= 0.99 \\ v_{BE}(\text{Act}) &= 0.7 \text{ V} \\ v_{BE}(\text{Sat}) &= 0.8 \text{ V} \\ v_{CE}(\text{Sat}) &= 0.2 \text{ V}\end{aligned}$$



$$V_E = 0 \text{ V}$$

$$V_B = V_C$$

Assuming active,

$$V_{BE} = 0.7$$

$$V_B - V_E = 0.7$$

$$\Rightarrow V_B = 0.7$$

$$V_C = 0.7$$

$$i_c = \frac{10 - 0.7}{2} = 4.65 \text{ mA}$$

$$V_{CE} = V_C - V_E = 0.7 - 0$$

$$= 0.7 > 0.3 \text{ V}$$

✓ Active

# Example 9

Sol<sup>n</sup>:

Assuming Active mode,

$$V_{BE} = 0.7 \text{ V} \Rightarrow V_B - V_E = 0.7 \text{ V} \therefore V_E = (-1) - 0.7 \text{ V} = -1.7 \text{ V}$$

$$I_B = \frac{0 - V_B}{R_B} = \frac{0 - (-1)}{500 \text{ k}\Omega} = 2 \text{ }\mu\text{A}$$

$$I_E = \frac{V_E - (-3)}{R_E} = \frac{-1.7 + 3}{4.8 \text{ k}\Omega} = 0.271 \text{ mA}$$

$$I_C = I_E - I_B = 0.269 \text{ mA}$$

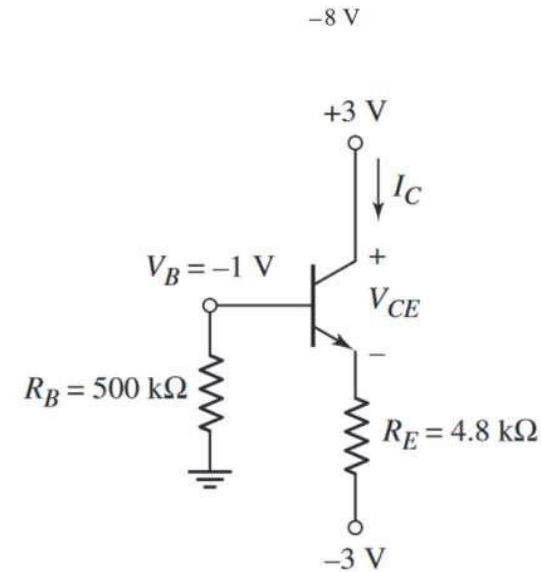
$$\beta = \frac{I_C}{I_B} = 134.5$$

$$\alpha = \frac{I_C}{I_E} = 0.9926$$

$$V_{CE} = V_C - V_E = 3 - (-1.7) = 4.7 \text{ V} > 0.2 \text{ V so, forward active mode}$$

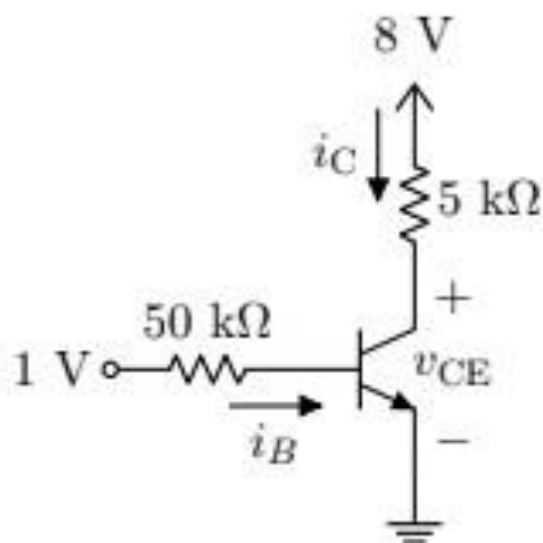
Assumption correct!

In the circuit shown in adjacent figure, the values of measured parameters are shown. Determine  $\beta$ ,  $\alpha$ , and the other labeled currents and voltages.



~~\*~~

Analyze the circuit below to find  $i_C$  and  $v_{CE}$ . Here, **use** the Method of Assumed State. You must **validate** your assumptions.



$$\beta = 100$$

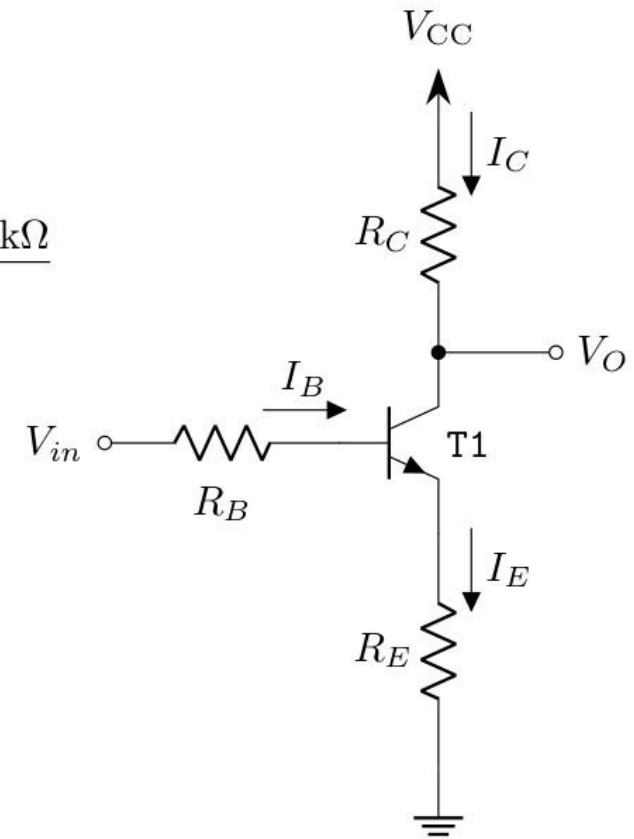
$$\alpha = 0.99$$

$$v_{BE(\text{Active})} = 0.7 \text{ V}$$

$$v_{BE(\text{Saturation})} = 0.8 \text{ V}$$

$$v_{CE(\text{Saturation})} = 0.2 \text{ V}$$

Andrew and Nicole found the adjacent circuit built in a trainer board. From the transistor model, they knew it had a gain of ~~[Set-A]~~  $\beta = 80$ . They also saw  $V_{CC} = 5\text{ V}$ ,  $R_B = 2\text{ k}\Omega$ , and  $R_C = 3\text{ k}\Omega$  or [Set-B]  $\beta = 60$ . They also saw  $V_{CC} = 6\text{ V}$ ,  $R_B = 3\text{ k}\Omega$ , and  $R_C = 4\text{ k}\Omega$ . However, the  $R_C$  resistor was an unknown one. So, they provided an input of  $V_{in} = 2\text{ V}$  and measured the output to be  $V_O = 2.2\text{ V}$ . Nicole said, "In this condition, the transistor is in **active** mode". But, Andrew disagreed.



- [CO1] **Illustrate** the Voltage Transfer Characteristic curve [1.5] of a BJT driven inverter with proper labeling.
- [CO3] **Design** the circuit, i.e., determine the value of  $R_E$ , [4] using what Nicole said about the mode of the transistor.
- [CO2] Use the calculations in (c), and **determine** who is right between Andrew and Nicole.
- [CO2] Using the value of  $R_E$  obtained from (b), **determine** who will be right if  $V_{in} = 4\text{ V}$ .

Solution: For active mode of operation:

$$V_{in} = V_{BE} + I_E R_E + V_{CE}$$

$$2 = 0.7 + I_E R_E + V_{CE}$$

$$I_E = \frac{2 - 0.7}{R_E + V_{CE}} \quad (3)$$

$$I_E = \frac{1.3}{3 + 61A\beta}$$

We can also write the equation of  $I_E$  from our knowledge of  $V_{CE}$ .

$$I_C = \beta I_B$$

$$\frac{V_{CE}}{R_C} = 0.95 = \frac{1.3 \times 60}{3 + 61A\beta} \quad (4)$$

$$R_C = \frac{0.95}{1.298 \text{ k}\Omega}$$

Solution: ANDREW WILL BE RIGHT THEN. Assuming saturation mode of operation and taking KVL along base-emitter we get:

$$V_{in} - R_B I_B - 0.7 - R_E I_E = 0$$

$$R_B I_B + R_E (I_C + I_B) = V_{in} - 0.7$$

$$(R_B + R_E) I_B + R_E I_C = V_{in} - 0.7$$

$$4.298 I_B + 1.298 I_C = 3.3$$

Taking KVL along collector-emitter junction, we get:

$$V_{CC} - R_C I_C - 0.2 - R_E I_E = 0$$

$$R_C I_C + R_E (I_C + I_B) = V_{CC} - 0.2$$

$$R_E I_B + (R_E + R_C) I_C = V_{CC} - 0.2$$

$$1.298 I_B + 5.298 I_C = 4.8$$

If  $V_{BE} = 0.7 \text{ V}$ , solving Eqn. 7 and 8 we get:

$$I_B = 0.534 \text{ mA}$$

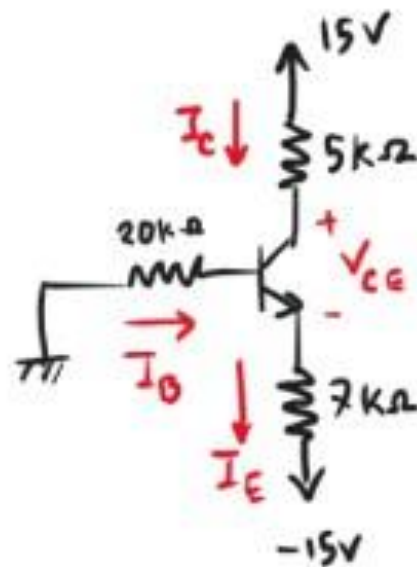
$$I_E = 0.775 \text{ mA}$$

If  $V_{CE} = 0.8 \text{ V}$ , solving above two equations, we get:

$$I_C = 0.509 \text{ mA}$$

$$I_E = 0.781 \text{ mA}$$

Analyze the following circuit to find the values of  $I_D$  and  $V_{DS}$ . Here, use the Method of Assumed State. You must **validate** your assumptions.



$$V_{BE(\text{ACTIVE})} = 0.7\text{V}$$

$$V_{BE(\text{SAT})} = 0.8\text{V}$$

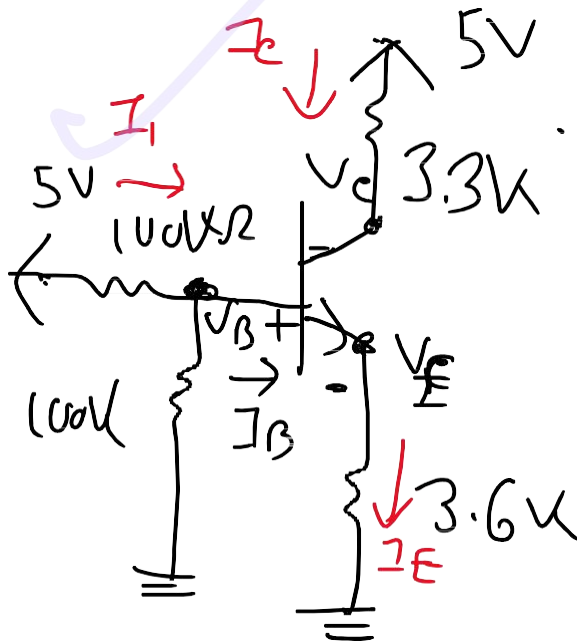
$$V_{CE(\text{SAT})} = 0.2\text{V}$$

$$\beta = 100$$

$$\alpha = 0.99$$

## Example 3

Analyze the circuit above to find  $i_B$ ,  $i_C$ ,  $i_E$  and  $v_{CE}$ . Here, use the Method of Assumed State. You must validate your assumptions.  $\beta = 100$ ,  $\alpha = (\beta)/(\beta+1) = 0.99$



Sol<sup>n</sup>:

Assume, Active mode

So,  $V_{BE} = 0.7 \text{ V}$  &  $I_C = \beta I_B = \alpha I_E$

Nodal analysis (at base terminal):

$$\frac{V_B - 5}{100 \text{ k}\Omega} + \frac{V_B}{100 \text{ k}\Omega} + I_B = 0 \text{ ---- (1)}$$

KVL:

$$5 - 0 = 100 I_1 + V_{BE} + 3.6 I_E$$

$$5 = 100 \frac{5 - V_B}{100 \text{ k}\Omega} + 0.7 + 3.6 I_B \text{ ---- (2)}$$

Solving, eq<sup>n</sup> 1 & 2,  $V_B = 2.28 \text{ V}$ ,  $I_B = 4.35 \text{ uA}$

$I_C = \beta I_B = 0.435 \text{ mA}$ ,  $I_E = I_C + I_B = 0.43935 \text{ mA}$

$$V_C = 5 - 3.3 I_C = 3.5645 \text{ V}$$

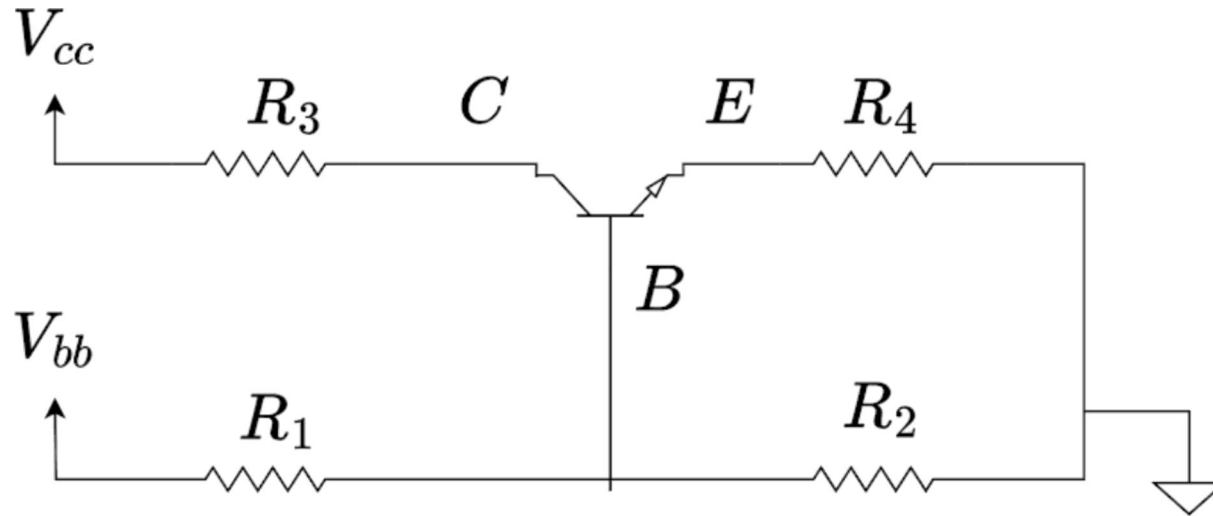
$$V_E = 3.6 I_E = 1.582 \text{ V}$$

$$V_{CE} = V_C - V_E = 1.983 \text{ V}$$

So,  $V_{CE} > 0.2 \text{ V}$

$\therefore$  Assumption Correct!

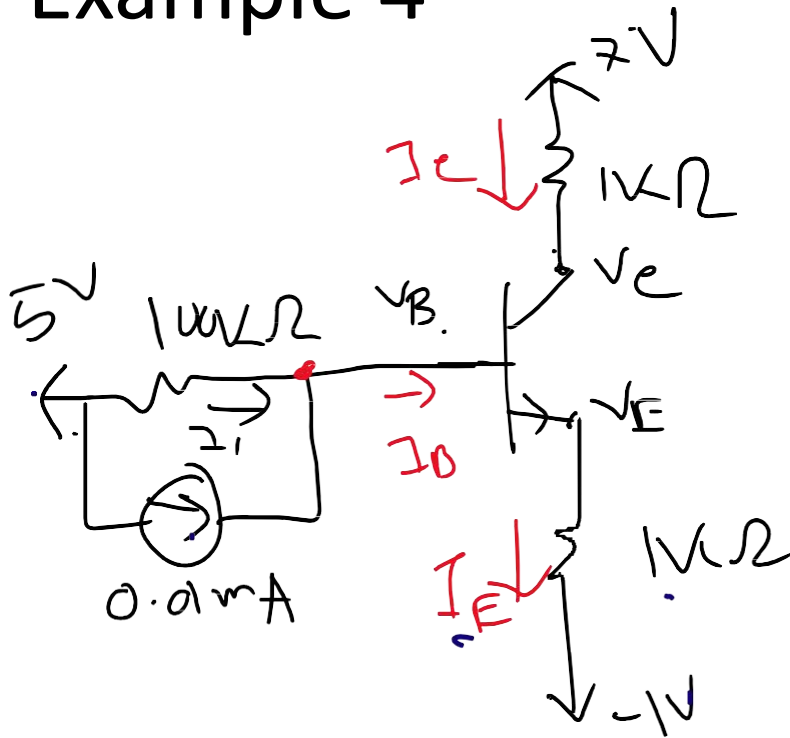




In the above circuit,  $V_{bb} = 5V$ ,  $V_{cc} = 15V$ ,  $R_1 = 20k\Omega$  ( $40k\Omega$ ),  $R_2 = 80k\Omega$  ( $60k\Omega$ ),  $R_3 = 2k\Omega$  and  $R_4 = 1k\Omega$ . Also, assume current gain,  $I_c/I_b = 100$ .

- Draw the equivalent circuit of BJT during saturation and active modes. [2]
- Solve the above circuit and calculate  $I_B$ ,  $I_C$ ,  $I_E$ ,  $V_{CE}$  and  $V_C$  using the method of assumed states. [Hint: try to find the Thevenin equivalent of the left hand side circuit from the B terminal and ground] [3]
- If  $V_{bb}$  is changed from 5V to 5.1V, what happens to the outputs of the circuits? Calculate  $I_B$ ,  $I_C$ ,  $I_E$ ,  $V_{CE}$  and  $V_C$  again. Now for a 0.1V increase in input  $V_{bb}$ , what is the change of  $I_n$ ? Use All  $I_{n,new} \wedge I_{n,old}$  [3+1]
- Explain any use case of the differences in voltage increase between input and output. What could the use case be to such a phenomenon? [1]

## Example 4



Analyze the circuit above to find  $v_{CE}$ . Here, use the Method of Assumed State. You must validate your assumptions.  $\beta = 100$ ,  $\alpha = (\beta)/(\beta+1) = 0.99$

Sol<sup>n</sup>:

Assume, Active mode

So,  $V_{BE} = 0.7 \text{ V}$  &  $I_C = \beta I_B = \alpha I_E$

KCL (at base terminal):

$$I_1 + 0.01 = I_B$$

$$\therefore I_1 = I_B - 0.01$$

KVL:

$$5 - (-1) = 100I_1 + V_{BE} + \frac{1I_E}{\alpha}$$

$$6 = 100(I_B - 0.01) + 0.7 + \frac{1}{\alpha} I_B \quad \text{--- (2)}$$

$$\therefore I_B = 0.0313 \text{ mA}$$

$$I_C = \beta I_B = 3.13 \text{ mA}, I_E = I_C + I_B = 3.1613 \text{ mA}$$

$$V_C = 7 - 1I_C = 3.87 \text{ V}$$

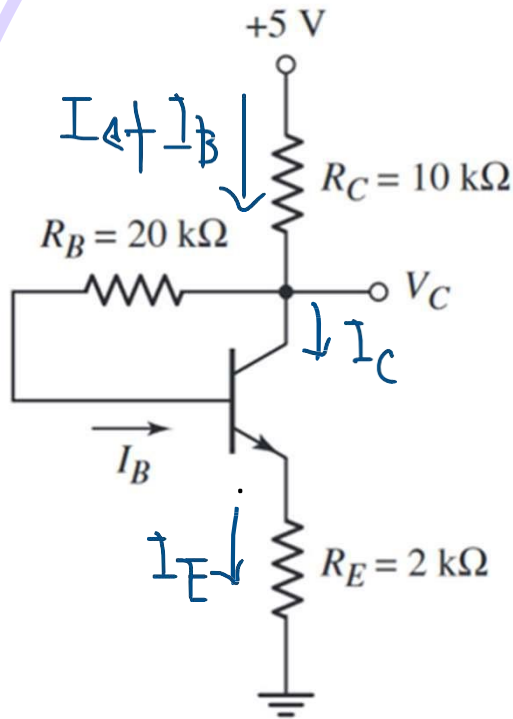
$$V_E = 1I_E - 1 = 2.16 \text{ V}$$

$$V_{CE} = V_C - V_E = 1.709 \text{ V}$$

$$\text{So, } V_{CE} > 0.2 \text{ V}$$

$\therefore$  Assumption Correct!

## Example 10



$\beta = 75$ . Find the labelled voltages and currents.

**Sol<sup>n</sup>:**

Assuming Active mode,

$$V_{BE} = 0.7 \text{ V}$$

$$5 - 0 = R_C(I_C + I_B) + R_B I_B + V_{BE} + R_E I_E$$

$$5 = 10(\beta I_B + I_B) + 20I_B + 0.7 + 2I_E$$

$$\therefore I_B = 4.604 \text{ uA}$$

$$I_C = \beta I_B = 0.345 \text{ mA}$$

$$V_C = 5 - 10(I_C + I_B) = 1.5 \text{ V}$$

$$V_E = 2I_E = 0.7 \text{ V}$$

$V_{CE} = V_C - V_E = 1.5 - 0.7 = 0.8 \text{ V} > 0.2 \text{ V}$  so, forward active mode  
Assumption correct!