

Important Questions for Class 12 Physics

Chapter 9 – Ray optics and Optical Instruments

Very Short Answer Questions

1 Mark

1. A person standing before a concave mirror cannot see his image, unless he is beyond the centre of curvature. Why?

Ans: Let a man stand beyond focus i.e., between focus and centre of curvature, then the image formed will be real and inverted and is formed beyond C (beyond him). Thus, he cannot see the image.

But if he stands beyond C, the image will be formed between focus and centre of curvature which is in front of him and thus he will be able to see his reflected image.

2. For what angle of incidence, the lateral shift produced by a parallel sided glass plate is maximum?

Ans: We know that lateral shift d is given as,

$$d = \frac{t}{\cos r} \sin (i - r)$$

For lateral shift d to be maximum, $\sin(i-r)$ must be maximum i.e., i-r must be minimum. This happens when $i = 90^{\circ}$.

$$\Rightarrow d = \frac{t}{\cos r} \sin(90^{\circ} - r)$$

$$\Rightarrow$$
 D = t

Then, we can say that lateral shift is maximum.

3. You read a newspaper, because of the light it reflects. Then why do you not see even a faint image of yourself in the newspaper?

Ans: We know that image is formed due to regular reflection of light.



However, when we read a newspaper, there is diffused (irregular) reflection of light, thus we are not able to see even a faint image of ourselves on the newspaper.

4. A substance has critical angle of 45° for yellow light, then what is its refractive index?

Ans: We know that refractive index is given as below

$$\mu = \frac{1}{\sin \mathbf{C}}$$

Substituting the values, we have

$$\mu = \frac{1}{\sin 45^\circ} = \frac{1}{\left(1/\sqrt{2}\right)}$$

$$\Rightarrow \mu = \sqrt{2}$$

5. An object is placed between the pole and focus of a concave mirror produces a virtual and enlarged image. Justify using mirror formula.

Ans: We know that the mirror formula is as given below,

$$\frac{1}{v} + \frac{1}{u} = \frac{1}{f}$$

$$\Rightarrow$$
 v = $\frac{uf}{u-f}$

Now magnification, $m = \frac{V}{U}$.

$$\Rightarrow m = \frac{\frac{uf}{u - f}}{u}$$

$$\Rightarrow$$
 m = $\frac{f}{u-f}$



For a concave mirror,

$$f = -ve$$

$$u = -ve$$

Given
$$u < f$$
;

 \therefore m = +ve, hence enlarged image is produced.

6. A converging and diverging lens of equal focal lengths are placed coaxially in contact. Find the focal length and power of the combination.

Ans: We know that the lens formula is as given below,

$$\frac{1}{F} = \frac{1}{f_1} + \frac{1}{f_2}$$

For converging lens $f_1 = +f$

For diverging lens $f_2 = -f$

$$\Rightarrow \frac{1}{F} = \frac{1}{f} - \frac{1}{f}$$

$$\Rightarrow F = \frac{1}{0} \Rightarrow F = \infty$$

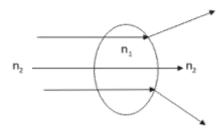
Since
$$P = \frac{1}{F} = \frac{1}{\infty} = 0$$

Hence, the power of the combination of the lens is P = 0.

7. The refractive index of a material of a convex lens is n_1 . It is immersed in a medium of refractive index n_2 . A parallel beam of light is incident on the lens. Trace the path of the emergent rays when $n_2 > n_1$.

Ans: We know that for $n_2 > n_1$ then the convex lens behaves as a concave lens as shown below.





8. In a telescope the focal length of the objective and the eye piece are 60 cm and 5 cm respectively. What is (1) its magnification power? (2) the tube length?

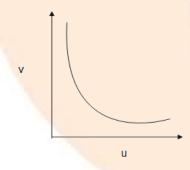
Ans:

1) We know that magnification
$$M = -\frac{f_o}{f_e} = \frac{-60}{5} = -12$$

2) The tube length we be $L = f_o + f_e = 60 + 5 = 65$ cm.

9. Show the variation of u and v in case of a convex mirror.

Ans: The variation of **u** and **v** in a convex mirror is as shown below.



10. Two lenses having focal length f_1 and f_2 are placed coaxially at a distance x from each other. What is the focal length of the combination?

Ans: The formula for the focal length of the combination of two lenses when placed coaxially at a distance x from each other is as given below:



$$\frac{1}{F} = \frac{1}{f_1} + \frac{1}{f_2} - \frac{x}{f_1 f_2}.$$

11. Does short-sightedness (myopia) or long-sightedness (hypermetropia) imply necessarily that the eye has partially lost its ability of accommodation? If not, what might cause these defects of vision?

Ans: Myopia and hypermetropia are common eye defects.

A myopic or hypermetropic person need not necessarily suffer a partial loss in their eyes' ability of accommodation.

Myopia occurs when the eye-balls engage in elongation from the front to the back whereas hypermetropia occurs when the eye-balls shorten themselves.

On the other hand, when the eye-lens completely loses its ability of adjusting itself, then the defect is called presbyopia.

Short Answer Questions

2 Mark

1. What are optical fibres? Give their one use.

Ans: Optical fibres are thin and long strands of fine quality glass or quartz coated with a thin layer of material with refractive index less than that of the strands.

They work on the principle of total internal reflection and thus, they avoid any loss in transfer of information.

<u>Uses</u>

Optical fibres are often used in medical investigations i.e., one can examine the inside view of stomach and intestine by a method called endoscopy.

2. How do the focal lengths of a lens change with increase in the wavelength of the light?

Ans: We know that
$$\frac{1}{f} = (\mu - 1) \left(\frac{1}{R_1} - \frac{1}{R_2} \right)$$
.



Also,
$$\mu \propto \frac{1}{\lambda}$$
.

Clearly, when wavelength (λ) increases, refractive index (μ) decreases.

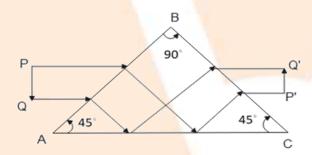
Similarly, $\mu \propto f$.

Clearly, as refractive index (µ) decreases, focal length (f) increases.

3. Show with a ray diagram, how an image is produced in a total reflecting prism?

Ans: Consider the two rays from the object PQ, as shown below.

They undergo total internal reflection firstly at the face AB and then at BC forming the final image P'Q' (real and inverted image).



4. The radii of the curvature of the two spherical surfaces which is a lens of required focal length are not same. It forms image of an object. The surfaces of the lens facing the object and the image are inter-changed. Will the position of the image change?

Ans: As we know that,

$$\frac{1}{f} = (\mu - 1) \left(\frac{1}{R_1} - \frac{1}{R_2} \right)$$

When the radii of curvature R_1 and R_2 are interchanged, the focal length of the lens also changes. Hence, the position of the image will reduce gradually.



5. A thin converging lens has focal length (f) when illuminated by violet light. State with reason how the focal length of the lens will change if violet light is replaced by red light.

Ans: We know that,

$$\frac{1}{f} = (n-1) \left(\frac{1}{R_1} - \frac{1}{R_2} \right)$$

Since, n for violet is more that n for red colour, and since $m \propto f$, we can say that the focal length of the lens will decrease when violet light is replaced by red light.

6. Thin prism of angle 60° gives a deviation of 30°. What is the refractive index of material of the prism?

Ans: We know that the refractive index of a thin prism is as follows

$$n = \frac{\sin\left(\frac{A + \delta_{m}}{2}\right)}{\sin\left(\frac{A}{2}\right)}$$

Substituting the given values, we have

$$n = \frac{\sin\left(\frac{60+30}{2}\right)}{\sin\frac{60}{2}} = \frac{\sin 45^{\circ}}{\sin 30^{\circ}}$$

 \Rightarrow n = 1.41, which is the refractive index of the given thin prism.

7. Although the surfaces of a goggle lens are curved it does not have any power. Why?

Ans: Since the two surfaces of a goggle lens are parallel i.e., one surface convex and the other concave, the resultant power of the two surfaces is zero as powers on both surfaces are equal but opposite in sign.

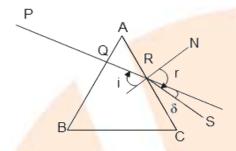
$$p = p_1 + p_2 = p + (-p) = 0$$



8. A ray of light is incident normally on one face of the prism of apex angle 30° and refractive index $\sqrt{2}$. Find the angle of deviation for the ray of light.

Ans: Let us assume that the ray PQ falls normally on AB.

Then, it goes straight to AC without any refraction (QR) as shown in the figure.



Also given that

$$n = \sqrt{2}$$
;

$$A = 30^{\circ};$$

$$i = 30^{\circ}$$

Applying Snell's law for face AC,

$$n = \frac{\sin r}{\sin 30^{\circ}}$$

$$\Rightarrow \sin r = \frac{1}{\sqrt{2}}$$

$$\Rightarrow$$
 r = 45°

Now angle of deviation

$$\delta\!=\!r\!-\!i$$

$$\Rightarrow \delta = 45^{\circ} - 30^{\circ}$$

 $\Rightarrow \delta = 15^{\circ}$, is the angle of deviation.

9. Following data was recorded for values of object distance and corresponding values of image distance in the experiment on study of real



image formation by a convex lens of power +5 D. One of the three observations is incorrect. Identify and give reason:

Sl. No:	1	2	3
Object distance (cm):	25	30	35
Image distance (cm):	97	60	37

Ans: Given that P = 5D

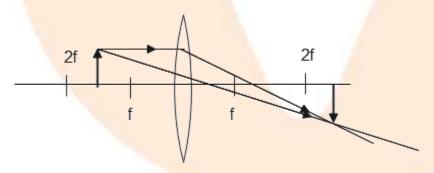
We know that $P = \frac{1}{f}$

$$\Rightarrow$$
 f = $\frac{1}{5}$ = 20cm

Then,

$$2f = 40cm$$

To find, which of the following observations are incorrect, consider the ray diagram as shown below, where it can be seen that when the object is placed between focus and twice the focus, the image is obtained after the measure if twice the focus.



1) u = 25 and v = 97 is correct.

When the object is placed between f = 20cm and 2f = 40cm, the image is obtained after 2f = 40cm.

2) u = 30 and v = 60 is also correct.

When the object is placed between f = 20cm and 2f = 40cm, the image is obtained after 2f = 40cm.



3) u = 30 and v = 37 is incorrect.

Here, when the object is placed between f = 20cm and 2f = 40cm, the image is obtained before 2f = 40cm.

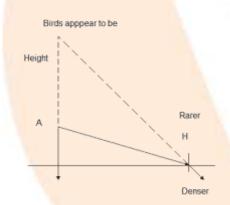
Clearly, we can conclude that observation (3) is incorrect because both object and the image here lie between f and 2 f.

10. Birds flying high in the air appear to be higher than in reality. Explain why?

Ans: Birds fly in air, which is a rarer medium when compared to the ground, which is denser.

The light from the birds when viewed will undergo refraction towards the normal. Thus, the birds appear to fly at a higher point. i.e.,

Apparent height > Real height



11. What is the focal length of a convex lens of focal length 30cm in contact with a concave lens of focal length 20cm? Is the system a converging or a diverging lens? Ignore thickness of the lenses.

Ans: Given that.

Focal length of the convex lens, $f_1 = 30$ cm

Focal length of the concave lens, $f_2 = -20$ cm

Focal length of the system of lenses = f



Then the equivalent focal length of a system of two lenses in contact is given as:

$$\frac{1}{f} = \frac{1}{f_1} + \frac{1}{f_2}$$

$$\Rightarrow \frac{1}{f} = \frac{1}{30} - \frac{1}{20} = \frac{2-3}{60} = -\frac{1}{60}$$

$$\therefore$$
 f = -60cm

Hence, the focal length of the combination of lenses is 60 cm. The negative sign indicates that the system of lenses acts as a diverging lens.

12. The image of a small electric bulb fixed on the wall of a room is to be obtained on the opposite wall 3m away by means of a large convex lens. What is the maximum possible focal length of the lens required for the purpose?

Ans: Given that,

Distance between the object and the image, d = 3 m

Maximum focal length of the convex lens = f_{max}

For real images, the maximum focal length is given as:

$$f_{max} = \frac{d}{4} = \frac{3}{4} = 0.75m$$

Hence, for the required purpose, the maximum possible focal length of the convex lens is 0.75 m.

13. A screen is placed 90cm from an object. The image of the object on the screen is formed by a convex lens at two different locations separated by 20cm. Determine the focal length of the lens.

Ans: Given that,

Distance between the image (screen) and the object, D = 90 cm

Distance between two locations of the convex lens, d = 20 cm



Focal length of the lens = f

Focal length is related to d and D as:

$$f = \frac{D^2 - d^2}{4D} = \frac{(90)^2 - (20)^2}{4 \times 90} = \frac{770}{36} = 21.39$$
cm

Therefore, the focal length of the convex lens is 21.39cm.

14. You are given prisms made of crown glass and flint glass with a wide variety of angles. Suggest a combination of prisms which will

a) deviate a pencil of white light without much dispersion,

Ans: Place the two given prisms next to each other.

Make sure that their bases are on the opposite sides of the incident white light, with their faces touching each other.

When the white light is incident on the first prism, it will get dispersed. This acts as the incident light for the second prism and the dispersed light this time will recombine to give white light as a result of the combination of the two prisms.

b) disperse (and displace) a pencil of white light without much deviation.

Ans: Take the system of the two prisms as suggested in answer (a).

Adjust (increase) the angle of the flint-glass-prism so that the deviations due to the combination of the prisms become equal.

This combination will now disperse the pencil of white light without much deviation.

15. A myopic person has been using spectacles of power -1.0 dioptre for distant vision. During old age he also needs to use separate reading glass of power +2.0 dioptres. Explain what may have happened.

Ans: Given that the power of the spectacles used by the myopic person is P = -1.0 D.

Focal length of the spectacles,



$$f = \frac{1}{P} = \frac{1}{-1 \times 10^{-2}} = -100cm$$

Hence, the far point of the person is 100cm. He might have a normal near point of 25 cm.

When he uses the spectacles, the objects placed at infinity produce virtual images at 100 cm.

He uses the ability of accommodation of the eye-lens to see the objects placed between 100 cm and 25 cm.

During old age, the person uses reading glasses of power, p' = +2D.

The ability of accommodation is lost in old age. This defect is called presbyopia. As a result, he is unable to see clearly the objects placed at 25 cm

16. A person looking at a person wearing a shirt with a pattern comprising vertical and horizontal lines is able to see the vertical lines more distinctly than the horizontal ones. What is this defect due to? How is such a defect of vision corrected?

Ans: In the given case, the person is able to see vertical lines more distinctly than horizontal lines.

This means that the refracting system (cornea and eye-lens) of the eye is not working effectively in different planes. This defect is called astigmatism.

The person's eye has enough curvature in the vertical plane. However, the curvature in the horizontal plane is insufficient.

Hence, sharp images of the vertical lines are formed on the retina, but horizontal lines appear blurred. This defect can be corrected by using cylindrical lenses.

- 17. A small telescope has an objective lens of focal length 140cm and an eyepiece of focal length 5.0cm. What is the magnifying power of the telescope for viewing distant objects when
- a) the telescope is in normal adjustment (i.e., when the final image is at infinity)?



Ans: Given that,

Focal length of the objective lens, $f_o = 140 \text{ cm}$

Focal length of the eyepiece, $f_e = 5$ cm

Least distance of distinct vision, d = 25 cm

When the telescope is in normal adjustment, its magnifying power is given as:

$$m = \frac{f_o}{f_e}$$

$$\Rightarrow$$
 m = $\frac{140}{5}$ = 28

Thus, the magnifying power is 28.

b) the final image is formed at the least distance of distinct vision 25cm?

Ans: When the final image is formed at d, the magnifying power of the telescope is given as:

$$\mathbf{m} = \frac{\mathbf{f}_{o}}{\mathbf{f}_{e}} \left[1 + \frac{\mathbf{f}_{e}}{\mathbf{d}} \right]$$

$$\Rightarrow m = \frac{140}{5} \left[1 + \frac{5}{25} \right]$$

$$\Rightarrow$$
 m = $28[1+0.2]$

$$\Rightarrow$$
 m = 28×1.2 = 33.6

Thus, the magnifying power is 33.6.

18. Light incident normally on a plane mirror attached to a galvanometer coil retraces backwards as shown in figure below. A current in the coil produces a deflection of 3.5° in the mirror. What is the displacement of the reflected spot of light on a screen placed 1.5 m away?

Ans: Given that,



Angle of deflection, $\theta = 3.5^{\circ}$

Distance of the screen from the mirror, D=1.5 m

The reflected rays get deflected by an amount twice the angle of deflection i.e., $2\theta = 7.0^{\circ}$

The displacement (d) of the reflected spot of light on the screen is given as:

$$\tan 2\theta = \frac{d}{1.5}$$

$$\therefore d = 1.5 \times \tan 7^{\circ} = 0.184 \text{m} = 18.4 \text{cm}$$

Hence, the displacement of the reflected spot of light is 18.4 cm.

Short Answer Questions

3 Marks

1. Find the radius of curvature of the convex surface of a plane convex lens, whose focal length is 0.3 m and the refractive index of the material of the lens is 1.5.

Ans: Given that,

$$\mu = 1.5$$

$$f = 0.3m$$

For plane convex lens,

$$R_2 = -\infty$$
 and let $R_1 = R$.

Substituting these values in the formula for focal length,

$$\frac{1}{f} = \left(\mu - 1\right) \left(\frac{1}{R_1} - \frac{1}{R_2}\right)$$

$$\Rightarrow \frac{1}{0.3} = (1.5 - 1) \left(\frac{1}{R} + \frac{1}{\infty} \right)$$

$$\Rightarrow \left(\frac{1}{R}\right)0.5 = \frac{1}{0.3}$$



$$\Rightarrow$$
 R = 0.15m

Thus, the radius of curvature is R = 0.15m.

2. Show that the limiting value of the angle of prism is twice its critical angle. Hence define critical angle.

Ans: We know that,

Angle of the prism is given by $A = r_1 + r_2$.

In a case of a triangular prism where $i_1 = i_2 = 90^\circ$, angle of refraction is given by $r_1 = r_2 = C$.

where, C is the critical angle.

Clearly,

$$\mathbf{A} = \mathbf{r}_1 + \mathbf{r}_2$$

$$\Rightarrow$$
 A = C + C

$$\Rightarrow$$
 A = 2C

Therefore, the angle of incidence for which angle of refraction is 90°, is called the critical angle.

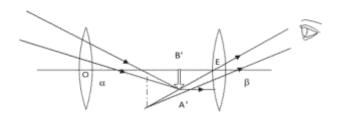
3. Draw a labelled diagram of telescope when the image is formed at the least distance of distinct vision? Hence derive the expression for its magnifying power.

Ans: We know that,

magnifying power =
$$\frac{\text{angle subtended by the image at the eye}}{\text{angle subtended by the object at the eye}}$$

$$MP = \frac{\tan \beta}{\tan \alpha} = \frac{\beta}{\alpha}$$
 (Since angles are very small)





$$\tan \beta = \frac{A'B'}{B'E}$$
 and $\tan \alpha = \frac{A'B'}{B'O}$

$$MP = \frac{A'B'}{B'E} \times \frac{A'B'}{B'O}$$

$$MP = \frac{B'O}{B'E} = \frac{f_o}{-v_e}$$

$$MP = \frac{-f_o}{-v_e}.....(i)$$

For eye piece,

$$\frac{1}{v} - \frac{1}{v} = \frac{1}{f_e}$$

$$-\frac{1}{D} - \frac{1}{-v_e} = \frac{1}{f_e}$$

Multiply by D,

$$-1 + \frac{D}{v_e} = \frac{D}{f_e}$$

$$\frac{D}{v_e} = \frac{D}{f_e} + 1$$

$$\frac{1}{v_e} = \frac{1}{f_e} + \frac{1}{D} = \frac{1}{f_e} \left(1 + \frac{f_e}{D} \right)$$

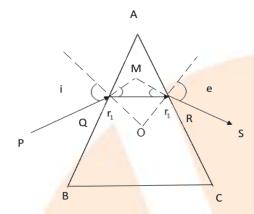
Substituting in (i),

$$MP = \frac{-f_o}{f_e} \left(1 + \frac{f_e}{D} \right)$$



4. Drive the expression for the angle of deviation for a ray of light passing through an equilateral prism of refracting angle A.

Ans: Consider the given diagram:



At the surface AB,

$$\delta_1 = i - r_1$$

At the surface AC,

$$\delta_2 = e - r_2$$

Thus,

$$\delta = \delta_1 + \delta_2$$

$$\delta = i + e - (r_1 + r_2)$$
(1)

Now, in quadrilateral AQOR,

$$\angle A + \angle Q + \angle O + \angle R = 360^{\circ}$$

$$\Rightarrow \angle A + \angle O = 180^{\circ} \dots (2)$$

Also, in $\triangle QOR$,

$$\angle Q + \angle O + \angle R = 180^{\circ}$$

Or

$$r_1 + r_2 + \angle O = 180^{\circ} \dots (3)$$

From (2) and (3),



$$r_1 + r_2 = A$$
(4)

Substituting equation (4) in equation (1)

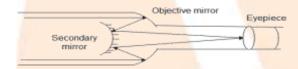
$$\delta = i + e - A$$

Or

$$A + \delta = i + e$$

5. Draw a ray diagram to illustrate image formation by a Newtonian type reflecting telescope. Hence state two advantages of it over refracting type telescopes.

Ans: The ray diagram of the Newtonian type reflecting telescope is as shown below.



Advantages

The image formed in a reflecting type telescope is free from chromatic aberrations.

The image formed is very bright due to its large light gathering power.

6. The magnifying power of an astronomical telescope in the normal adjustment position is 100. The distance between the objective and the eye

piece is 101 cm. Calculate the focal length of the objective and the eye piece.

Ans: Given that,

$$f_o + f_e = 101cm \dots (1)$$

$$M = \left| \frac{f_o}{f_e} \right| = 100$$

$$f_o = 100 f_e$$
(2)



Substituting equation (2) in equation (1),

$$f_e + 100 f_e = 101$$

$$\Rightarrow 101f_e = 101$$

$$\Rightarrow$$
 $f_e = 1cm$

Substituting f_e in equation (2),

$$f_o = 100 \times 1$$

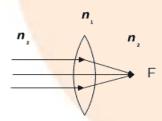
$$f_0 = 100cm$$

Thus, the focal length of the eye-piece is 1cm whereas the focal length of the objective is 100cm.

7. A convex lens made up of refractive index n_1 is kept in a medium of refractive index n_2 . Parallel rays of light are incident on the lens. Complete the path of rays of light emerging from the convex lens if

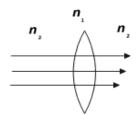
a)
$$n_1 > n_2$$

Ans: When $n_1 > n_2$, the lens behaves as a convex lens.



b)
$$n_1 = n_2$$

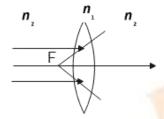
Ans: When $n_1 = n_2$, the lens behaves as a plane plate and thus, no refraction takes place.





c)
$$n_1 < n_2$$

Ans: When $n_1 < n_2$, the lens behaves as a convex lens.



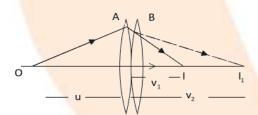
8. Derive the relation $\frac{1}{f} = \frac{1}{f_1} + \frac{1}{f_2}$, where f_1 and f_2 are focal lengths of two thin lenses and F is the focal length of the combination in contact.

Ans: Consider two thin lenses in contact having focal length f_1 and f_2 .

For the first lens,

$$\frac{1}{v_1} - \frac{1}{u} = \frac{1}{f_1}$$
(1)

For the second lens, I_1 acts as an object which forms the final image I.



Clearly,
$$\frac{1}{v} - \frac{1}{v_1} = \frac{1}{f_2}$$
(2)

Adding equations (1) & (2)

$$\frac{1}{f_1} + \frac{1}{f_2} = \frac{1}{v} - \frac{1}{u} + \frac{1}{v_1} - \frac{1}{v_1}$$

$$\Rightarrow \frac{1}{f_1} + \frac{1}{f_2} = \frac{1}{v} - \frac{1}{u}$$



Using lens formula $\left(\frac{1}{v} - \frac{1}{u} = \frac{1}{F}\right)$,

$$\frac{1}{f_1} + \frac{1}{f_2} = \frac{1}{F}$$

For n number of thin lenses in contact,

$$\frac{1}{F} = \frac{1}{f_1} + \frac{1}{f_2} + \frac{1}{f_3} + \dots + \frac{1}{f_n}$$

Hence the derivation.

9. A convex lens has a focal length 0.2 m and made of glass ($\mu = 1.50$) is immersed in water ($\mu = 1.33$). Find the change in focal length of the lens.

Ans: Given,

$$f_a = 0.2m$$
; $^a\mu_g = 1.50$

It is known that

$$\frac{1}{f_a} = {\binom{a}{\mu_g} - 1} \left(\frac{1}{R_1} - \frac{1}{R_2} \right)$$

$$\Rightarrow \frac{1}{0.2} = (1.50 - 1) \left(\frac{1}{R_1} - \frac{1}{R_2} \right)$$

$$\Rightarrow \frac{1}{R_1} - \frac{1}{R_2} = 10 \dots (1)$$

Now,

$$^{\mathrm{w}}\mu_{\mathrm{g}} = \frac{^{\mathrm{a}}\mu_{\mathrm{g}}}{^{\mathrm{a}}\mu_{\mathrm{w}}} = \frac{1.50}{1.33} = 1.128$$

Also, the focal length of the lens when immersed in water would be



$$\frac{1}{f_{w}} = {w \mu_{g} - 1} \left(\frac{1}{R_{1}} - \frac{1}{R_{2}} \right)$$

$$\Rightarrow \frac{1}{f_w} = (1.128 - 1) \left(\frac{1}{R_1} - \frac{1}{R_2} \right)$$

$$\Rightarrow \frac{1}{f_w} = (0.128) = \times 10 = 1.28$$

$$\Rightarrow f_{\rm w} = \frac{1}{1.28}$$

$$\Rightarrow$$
 f_w = 0.78m

Thus, the change in focal length is given by

$$f_w - f_a = 0.78 - 0.20 = 0.58m$$

10. A reflecting type telescope has a concave reflector of radius of curvature 120 cm. Calculate the focal length of eye piece to achieve a magnification of 20.

Ans: Given that

$$M = 20$$

R = 120cm (Concave reflector)

$$f_o = \frac{R}{2} = \frac{-120}{2} = -60cm$$

$$M = \frac{f_o}{f_e} \Rightarrow \frac{-60}{f_e} = -20$$

$$\Rightarrow$$
 $f_e = 3cm$

Thus, the focal length of the eye-piece is 3cm.



11. Show that a convex lens produces an N time magnified image, when the object distances from the lens have magnitude $\left(f\pm\frac{f}{N}\right)$. Here f is the magnitude of the focal length of the lens. Hence find two values of object distance u, for which convex lens of power 2.5 D will produce an image that is four times as large as the object?

Ans: We know that the magnifying power is given by

$$M = \frac{f}{v + f}$$

For real image m = -N;

$$\Rightarrow -N = \frac{f}{u+f} \Rightarrow u+f = \frac{-f}{N}$$

$$\Rightarrow$$
 u = $-\left(f + \frac{f}{N}\right)$ (1)

For virtual image m = N;

$$\Rightarrow N = \frac{f}{u+f}$$

$$\Rightarrow$$
 u + f = -f + $\frac{f}{N}$

$$\Rightarrow$$
 u = $-\left(f - \frac{f}{N}\right)$ (2)

From equation (1) & (2) we can say that magnification produced by a lens can be N if

$$u = -\left(f \pm \frac{f}{N}\right).$$

Now, power of the lens P = 2.5 D.

$$f = \frac{1}{P} = \frac{1}{2.5}m$$



$$\Rightarrow$$
 f = $\frac{1}{2.5} \times 100 = 40$ cm

It is given that

$$M = \pm 4$$

$$\Rightarrow \pm 4 = \frac{40}{u + 40}$$

$$\Rightarrow$$
 u + 40 = \pm 10

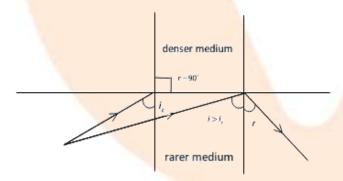
$$\Rightarrow$$
 u = -40 ± 10

$$\Rightarrow$$
 u = 30cm or -50cm

These are the two values of object distances.

12. Define total internal reflection of light. Hence write two advantages of total reflecting prisms over a plane mirror.

Ans: The phenomenon of reflection of light when a ray of light traveling from a denser medium getting reflected back into the same denser medium provided the angle of incidence is greater than the angle called critical angle is called total internal reflection.



Advantages

- a) It does require silvering.
- b) Multiple reflections do not take place in a reflecting prism. Due to this, only one image is formed, which is very bright.



13. An equiconvex lens of radius of curvature R is cut into two equal parts by a vertical plane, so it becomes a plano-convex lens. If f is the focal length of equiconvex lens, then what will be focal length of the planoconvex lens?

Ans: We know that

$$\frac{1}{f} = (n-1)\left(\frac{1}{R_1} - \frac{1}{R_2}\right)$$

For equiconvex lens $R_1 = R_2 = R$

$$\frac{1}{f} = \left(n - 1\right) \left(\frac{1}{R} - \frac{1}{-R}\right)$$

$$\Rightarrow \frac{1}{f} = (n-1)\left(\frac{1}{R} + \frac{1}{R}\right)$$

$$\Rightarrow \frac{1}{f} = \frac{2(n-1)}{R} \quad(1)$$

For plano-convex lens,

$$R_1 = R$$
 and $R_2 = \infty$

Clearly,

$$\frac{1}{\mathbf{f'}} = \left(\mathbf{n} - 1\right) \left(\frac{1}{\mathbf{R}_1} - \frac{1}{\mathbf{R}_2}\right)$$

$$\Rightarrow \frac{1}{f'} = (n-1)\left(\frac{1}{R} - \frac{1}{\infty}\right)$$

$$\Rightarrow \frac{1}{f'} = \frac{(n-1)}{R} \dots (2)$$

From (1) & (2)

$$\frac{f'}{f} = 2 \Longrightarrow f' = 2f$$



14. A converging lens of focal length 6.25 cm is used as a magnifying glass if near point of the observer is 25 cm from the eye and the lens is held close to the eye. Calculate

a) distance of object from the lens.

Ans: It is known that,

$$\frac{1}{f} = \frac{1}{v} - \frac{1}{u}$$

Given,

$$f = 6.25$$
cm

$$v = -25cm$$

Substituting these values in the first expression,

$$\frac{1}{u} = \frac{-1}{25} - \frac{1}{6.25} = \frac{-1}{5}$$

$$\Rightarrow$$
 u = -5cm

b) angular magnification

Ans: Angular magnification is given by

$$m=1+\frac{D}{F}=1+\frac{25}{6.25}$$

$$\Rightarrow$$
 m=1+4=5

c) angular magnification when final image is formed at infinity.

Ans: When the image is formed at infinity,

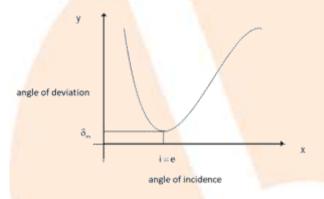
$$m = \frac{D}{F} = \frac{25}{6.25} = 4$$



15. Draw a graph to show that variation of angle of deviation δ_m with that of angle of incidence i for a monochromatic ray of light passing through a glass prism of refracting angle A. Hence deduce the relation.

$$\mu = \frac{sin\left(\frac{A + \delta_m}{2}\right)}{sin\left(\frac{A}{2}\right)}$$

Ans: For the minimum deviation position, $i = \frac{\delta_m + A}{2}$.



Also, $\angle i = \angle e$.

Now,
$$r_1 = r_2 = r$$
 (say).

We know that:

$$\angle i = \angle e = \delta_m + A$$
(1)

Also,

$$\mathbf{r}_1 + \mathbf{r}_2 = \mathbf{A}$$

$$\Rightarrow$$
 2r = A

$$\Rightarrow r = \frac{A}{2}$$

Applying minimum deviation condition is equation (1);

$$2i = \delta_m + A$$



$$\Rightarrow i = \frac{\delta_m + A}{2}$$

Applying Snell's law,

$$\mu = \frac{\sin i}{\sin r}$$

$$\Rightarrow \mu = \frac{\sin\left(\frac{A + \delta_{m}}{2}\right)}{\sin\left(\frac{A}{2}\right)}$$

16. An object of size 3.0 cm is placed 14 cm in front of a concave lens of focal length 21 cm. Describe the image produced by the lens. What happens if the object is moved further away from the lens?

Ans: Given that,

Size of the object, $h_1 = 3$ cm

Object distance, u = -14 cm

Focal length of the concave lens, f = -21 cm

Let image distance = v

According to the lens formula, we have the relation:

$$\frac{1}{v} - \frac{1}{u} = \frac{1}{f}$$

Substituting the given values,

$$\Rightarrow \frac{1}{v} = -\frac{1}{21} - \frac{1}{14} = \frac{-2 - 3}{42} = \frac{-5}{42}$$

$$v = -\frac{42}{5} = -8.4$$
cm

Hence, the image is formed on the other side of the lens, 8.4 cm away from it. The negative sign shows that the image is erect and virtual.



The magnification of the image is given as:

$$m = \frac{Im \, age \, height(h_2)}{Object \, height(h_1)} = \frac{v}{u}$$

$$\Rightarrow$$
 h₂ = $\frac{-8.4}{-14} \times 3 = 0.6 \times 3 = 1.8$ cm

Hence, the height of the image is 1.8cm.

If the object is moved further away from the lens, then the virtual image will move toward the focus of the lens, but not beyond it. Also, the size of the image will decrease with the increase in the object distance.

17. A beam of light converges at a point P. Now a lens is placed in the path of the convergent beam 12 cm from P. At what point does the beam converge if the lens is

a) a convex lens of focal length 20 cm

Ans: In the given situation, the object is virtual and the image formed is real.

Object distance, u = +12 cm

Focal length of the convex lens, f = 20 cm

Image distance = v

According to the lens formula, we have the relation:

$$\frac{1}{v} - \frac{1}{u} = \frac{1}{f}$$

$$\Rightarrow \frac{1}{v} - \frac{1}{12} = \frac{1}{20}$$

$$\Rightarrow \frac{1}{v} = \frac{1}{20} + \frac{1}{12} = \frac{3+5}{60} = \frac{8}{60}$$

$$\therefore v = \frac{60}{8} = 7.5cm$$

Hence, the image is formed 7.5cm away from the lens, toward its right.



b) a concave lens of focal length 16 cm.

Ans: Focal length of the concave lens, f = -16 cm

Image distance = v

Object distance, u = +12 cm

According to the lens formula, we have the relation:

$$\frac{1}{v} - \frac{1}{u} = \frac{1}{f}$$

$$\Rightarrow \frac{1}{y} = -\frac{1}{16} + \frac{1}{12} = \frac{-3+4}{48} = \frac{1}{48}$$

$$\therefore$$
 v = 48cm

Hence, the image is formed 48cm away from the lens, toward its right.

18. Double-convex lenses are to be manufactured from a glass of refractive index 1.55, with both faces of the same radius of curvature. What is the radius of curvature required if the focal length is to be 20cm?

Ans: Given that,

Refractive index of glass, $\mu = 1.55$

Focal length of the double-convex lens, f = 20 cm

Radius of curvature of one face of the lens $= R_1 = R$

Radius of curvature of the other face of the lens = $R_2 = -R$

Let radius of curvature of the double-convex lens = R

The value of R can be calculated as:

$$\frac{1}{f} = \left(\mu - 1\right) \left[\frac{1}{R_1} - \frac{1}{R_2} \right]$$

$$\Rightarrow \frac{1}{20} = (1.55 - 1) \left[\frac{1}{R} + \frac{1}{R} \right]$$



$$\Rightarrow \frac{1}{20} = 0.55 \times \frac{2}{R}$$

$$\Rightarrow$$
 R = 0.55 × 2 × 20 = 22cm

Hence, the radius of curvature of the double-convex lens is 22cm.

19. A small telescope has an objective lens of focal length 144 cm and an eyepiece of focal length 6.0 cm. What is the magnifying power of the telescope? What is the separation between the objective and the eyepiece?

Ans: Given,

Focal length of the objective lens, $f_0 = 144$ cm

Focal length of the eyepiece, $f_e = 6.0$ cm

The magnifying power of the telescope is given as:

$$m = \frac{f_o}{f_o} = \frac{144}{6} = 24$$

The separation between the objective lens and the eyepiece is calculated as:

$$D = f_0 + f_e = 144 + 6 = 150cm$$

Hence, the magnifying power of the telescope is 24 and the separation between the objective lens and the eyepiece is 150 cm.

20.

a) A giant refracting telescope at an observatory has an objective lens of focal length 15 m. If an eyepiece of focal length 1.0 cm is used, what is the angular magnification of the telescope?

Ans: Given that,

Focal length of the objective lens,

$$f_o = 15m = 15 \times 10^2 cm$$



Focal length of the eyepiece,

$$f_{e} = 1.0 cm$$

The angular magnification of a telescope is given as:

$$\alpha = \frac{f_o}{f_c} = \frac{15 \times 10^2}{1.0} = 1500$$

Hence, the angular magnification of the given refracting telescope is 1500.

b) If this telescope is used to view the moon, what is the diameter of the image of the moon formed by the objective lens? The diameter of the moon is 3.48×10^6 m, and the radius of lunar orbit is 3.8×10^8 m.

Ans: Given that,

Diameter of the moon, $d = 3.48 \times 10^6 \text{ m}$

Radius of the lunar orbit, $r_0 = 3.8 \times 10^8 \text{ m}$

Let d' be the diameter of the image of the moon formed by the objective lens.

The angle subtended by the diameter of the moon is equal to the angle subtended by the image.

$$\Rightarrow \frac{d}{r_0} = \frac{d'}{d_0}$$

$$\Rightarrow \frac{3.48 \times 10^6}{3.8 \times 10^8} = \frac{d'}{15}$$

$$\Rightarrow d' = \frac{3.48}{3.8} \times 10^{-2} \times 15$$

$$\Rightarrow$$
 d'=13.74×10⁻² m=13.74cm

Hence, the diameter of the moon's image formed by the objective lens is 13.74cm.



21. A small pin fixed on a table top is viewed from above from a distance of 50 cm. By what distance would the pin appear to be raised if it is viewed from the same point through a 15 cm thick glass slab held parallel to the table? Refractive index of glass $\mu = 1.5$. Does the answer depend on the location of the slab?

Ans: Given that, actual depth of the pin, d = 15 cm.

Refractive index of glass, $\mu = 1.5$

Let the apparent depth of the pin = d'.

Ratio of actual depth to the apparent depth is equal to the refractive index of glass, i.e.,

$$\mu = \frac{d}{d'}$$

$$\Rightarrow$$
 d' = $\frac{d}{\mu}$

$$\Rightarrow$$
 d' = $\frac{15}{1.5}$ = 10cm

Now, the distance by which the pin appears to be raised = d - d' = 15 - 10 = 5cm.

For a small angle of incidence, this distance does not depend upon the location of the slab.

- 22. A man with normal near point (25 cm) reads a book with small print using a magnifying glass: a thin convex lens of focal length 5 cm.
- a) What is the closest and the farthest distance at which he should keep the lens from the page so that he can read the book when viewing through the magnifying glass?

Ans: Given that,

Focal length of the magnifying glass, f = 5 cm

Least distance of distance vision, d = 25 cm

Let the object distance = u



Image distance, v = -d = -25 cm

According to the lens formula, we have:

$$\frac{1}{f} = \frac{1}{v} - \frac{1}{u}$$

$$\Rightarrow \frac{1}{u} = \frac{1}{v} - \frac{1}{f}$$

$$\Rightarrow \frac{1}{u} = \frac{1}{-25} - \frac{1}{5} = \frac{-5 - 1}{25} = \frac{-6}{25}$$

$$\Rightarrow$$
 u = $-\frac{25}{6}$ = -4.167cm

Hence, the closest distance at which the person can read the book is 4.167cm.

For the object at the farthest possible distance, the image distance $(v') = \infty$

According to the lens formula, we have:

$$\frac{1}{f} = \frac{1}{v'} - \frac{1}{u'}$$

$$\Rightarrow \frac{1}{u'} = \frac{1}{\infty} - \frac{1}{5} = -\frac{1}{5}$$

$$\therefore u' = -5cm$$

Hence, the farthest distance at which the person can read the book is 5cm.

b) What is the maximum and the minimum angular magnification (magnifying power) possible using the above simple microscope?

Ans: Maximum angular magnification is given by the relation:

$$\alpha_{\text{max}} = \frac{d}{|\mathbf{u}|} = \frac{25}{\left|\frac{25}{6}\right|} = 6$$

Minimum angular magnification is given by the relation:

$$\alpha_{\min} = \frac{\mathrm{d}}{|\mathbf{u'}|} = \frac{25}{5} = 5$$



- 23. A card sheet divided into squares each of size 1mm² is being viewed at a distance of 9 cm through a magnifying glass (a converging lens of focal length 9 cm) held close to the eye.
- a) What is the magnification produced by the lens? How much is the area of each square in the virtual image?

Ans: Given that,

Size of each square, $a = 1 \text{ mm}^2$

Object distance, u = -9 cm

Focal length of a converging lens, f = 10 cm

For image distance v, the lens formula can be written as:

$$\frac{1}{f} = \frac{1}{v} - \frac{1}{u}$$

$$\Rightarrow \frac{1}{10} = \frac{1}{v} + \frac{1}{9}$$

$$\Rightarrow \frac{1}{v} = -\frac{1}{90}$$

$$\therefore v = -90cm$$

Magnification,
$$m = \frac{v}{u}$$

$$\Rightarrow m = \frac{-90}{-9} = 10$$

 \therefore Area of each square in the virtual image = $10^2 \times a$

$$\Rightarrow$$
 A = $10^2 \times 1 = 100 \text{mm}^2$

$$\Rightarrow$$
 A = 1cm²

b) What is the angular magnification (magnifying power) of the lens?

Ans: Magnifying power of the lens $=\frac{d}{|u|} = \frac{25}{9} = 2.8$



c) Is the magnification in (a) equal to the magnifying power in (b)? Explain.

Ans: The magnification in (a) is not the same as the magnifying power in (b). The magnification magnitude is $\left(\frac{|v|}{|u|} \right)$ and the magnifying power is $\left(\frac{d}{|u|} \right)$. The two quantities will be equal only when the image is formed at the near point.

24.

a) At what distance should the lens be held from the figure in Exercise 9.29 in order to view the squares distinctly with the maximum possible magnifying power?

Ans: The maximum possible magnification is obtained when the image is formed at the near point (d = 25 cm).

Here,

Image distance, v = -d = -25 cm

Focal length, f = 10cm

Object distance = u

According to the lens formula, we have:

$$\frac{1}{f} = \frac{1}{v} - \frac{1}{u}$$

$$\Rightarrow \frac{1}{u} = \frac{1}{v} - \frac{1}{f}$$

$$\Rightarrow \frac{1}{u} = \frac{1}{-25} - \frac{1}{10} = \frac{-2 - 5}{50} = -\frac{7}{50}$$

$$u = -\frac{50}{7} = -7.14$$
cm

Hence, to view the squares distinctly, the lens should be kept 7.14cm away from them.



b) What is the magnification in this case?

Ans: Magnification =
$$\left| \frac{\mathbf{v}}{\mathbf{u}} \right| = \frac{25}{7.14} = 3.5$$

c) Is the magnification equal to the magnifying power in this case? Explain.

Ans: Here,

Magnifying power =
$$\frac{d}{|u|} = \frac{25}{7.14} = 3.5$$

Thus, it can be concluded that since the image is formed at the near point (25 cm), the magnifying power is equal to the magnitude of magnification.

25. What should be the distance between the object in Exercise 9.30 and the magnifying glass if the virtual image of each square in the figure is to have an area of 6.25mm²? Would you be able to see the squares distinctly with your eyes very close to the magnifier? [Note: Exercises 9.29 to 9.31 will help you clearly understand the difference between magnification in absolute size and the angular magnification (or magnifying power) of an instrument.]

Ans: Given,

Area of the virtual image of each square, $A = \frac{6.25 \text{mm}^2}{1}$

Area of each square, $A_0 = 6.25 \text{mm}^2$

The linear magnification of the object can be calculated as:

$$m = \sqrt{\frac{A}{A_0}} = \sqrt{\frac{6.25}{1}} = 2.5$$

However,

$$m = \frac{v}{u}$$

$$\Rightarrow$$
 v = mu = 2.5u(1)



Now,

Focal length of the magnifying glass, f = 10 cm.

According to the lens formula, we have the relation:

$$\frac{1}{f} = \frac{1}{v} - \frac{1}{u}$$

$$\Rightarrow \frac{1}{10} = \frac{1}{2.5u} - \frac{1}{u} = \frac{1}{u} \left(\frac{1}{2.5} - \frac{1}{1} \right) = \frac{1}{u} \left(\frac{1 - 2.5}{2.5} \right)$$

$$u = -\frac{1.5 \times 10}{2.5} = -6$$
cm

and

$$v = 2.5u = 2.5 \times 6 = -15cm$$

The virtual image is formed at a distance of 15cm, which is less than the near point (i.e., 25 cm) of a normal eye. Thus, it cannot be seen distinctly with the help of eyes.

26.

a) For the telescope described in Exercise 9.34 (a), what is the separation between the objective lens and the eyepiece?

Ans: Given,

Focal length of the objective lens, $f_0 = 140$ cm.

Focal length of the eyepiece, $f_e = 5$ cm.

In normal adjustment, the separation between the objective lens and the eyepiece is the sum of focal length of the objective lens and that of the eye piece.

$$\Rightarrow$$
 D = $f_0 + f_e = 140 + 5 = 145 \text{ cm}$

b) If this telescope is used to vie a 100m tall tower 3km away, what is the height of the image of the tower by the objective lens?

Ans: Given,



Height of the tower, $h_1 = 100 \text{ m}$

Distance of the tower (object) from the telescope, u = 3 km = 3000 m

The angle subtended by the tower at the telescope is given as:

$$\theta = \frac{h_1}{u} = \frac{100}{3000} = \frac{1}{30} \text{ rad}$$

The angle subtended by the image produced by the objective lens is given as:

$$\theta = \frac{h_2}{f_0} = \frac{h_2}{140} \text{ rad}$$

Where,

 h_2 = Height of the image of the tower formed by the objective lens.

$$\Rightarrow \frac{1}{30} = \frac{h_2}{140}$$

$$\Rightarrow h_2 = \frac{140}{30} = 4.7 \text{cm}$$

Therefore, the objective lens forms a 4.7cm tall image of the tower.

c) What is the height of the final image of the tower if it is formed at 25cm?

Ans: Given, the image is formed at a distance, d = 25 cm.

The magnification of the eyepiece is given by the relation:

$$m = 1 + \frac{d}{f_e}$$

$$\Rightarrow m = 1 + \frac{25}{5} = 1 + 5 = 6$$

Height of the final image = $mh_2 = 6 \times 4.7 = 28.2$ cm

Therefore, the height of the final image of the tower is 28.2cm.



Long Answer Questins

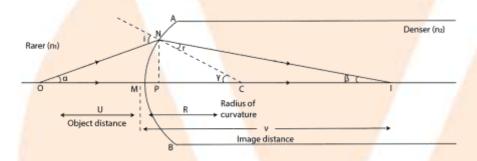
5 Marks

1. Prove that

$$\frac{n_2}{v} - \frac{n_1}{u} = \frac{n_2 - n_1}{R}$$

When refraction occurs of a convex spherical refracting surface and the ray travels from rarer to denser medium.

Ans: The ray is travelling from rarer medium to denser medium as shown in figure.



Now, we have $\triangle NOC$,

We get,

$$i = \alpha + \gamma \dots (1)$$

From figure,

$$\tan \alpha = \frac{MN}{OM}$$

$$\tan \beta = \frac{MN}{MI}$$

$$\tan \gamma = \frac{MN}{MC}$$

For small angle,
$$\alpha = \frac{MN}{OM}$$
, $\beta = \frac{MN}{MI}$, $\gamma = \frac{MN}{MC}$

Now equation (1) becomes,



$$\Rightarrow i = \frac{MN}{OM} + \frac{MN}{MC}$$

Similarly, $r = \gamma - \beta$

$$\Rightarrow r = \frac{MN}{MC} - \frac{MN}{MI}$$

Using Snell's Law,

$$n_1 \sin i = n_2 \sin r$$

For small angle,

$$n_1 i = n_2 r$$

Now, we put the value of i and r in the above equation,

$$n_1 \left[\frac{MN}{OM} + \frac{MN}{MC} \right] = n_2 \left[\frac{MN}{MC} - \frac{MN}{MI} \right] \dots (2)$$

Put OM = -u, MI = v, MC = R in equation (2),

$$\Rightarrow n_1 \left[\frac{1}{OM} + \frac{1}{MC} \right] = n_2 \left[\frac{1}{MC} - \frac{1}{MI} \right]$$

$$\Rightarrow \frac{n_2}{MI} + \frac{n_1}{OM} = \frac{n_2 - n_1}{MC}$$

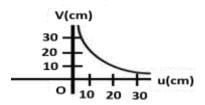
$$\Rightarrow \frac{\mathbf{n}_2}{\mathbf{v}} + \frac{\mathbf{n}_1}{-\mathbf{n}} = \frac{\mathbf{n}_2 - \mathbf{n}_1}{\mathbf{R}}$$

$$\Rightarrow \frac{\mathbf{n}_2}{\mathbf{v}} - \frac{\mathbf{n}_1}{\mathbf{u}} = \frac{\mathbf{n}_2 - \mathbf{n}_1}{\mathbf{R}}$$

Hence, Proved.

2. A lens forms a real image of an object. The distance of the object. From the lens is u cm and the distance of the image from the lens is v cm. The given graph shows the variation of v and u





a) What is the nature of the lens?

Ans: The lens is convex lens.

b) Using the graph find the focal length of the lens?

Ans: We use lens formula,

$$\frac{1}{f} = \frac{1}{v} - \frac{1}{u}$$

When $u \rightarrow \infty$, v = 10cm

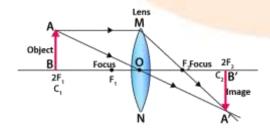
$$\Rightarrow \frac{1}{f} = \frac{1}{10} - \frac{1}{\infty}$$

$$\Rightarrow \frac{1}{f} = \frac{1}{10}$$

$$\Rightarrow$$
 f = 10cm

c) Draw a ray diagram to show the formation of image of same size as that of object in case of converging lens hence derive lens equation?

Ans: The below figure shows the formation of same size of image as that of object.



From above figure, $\triangle ABO \& \triangle A'B'O$ are similar.



$$\frac{B'O}{BO} = \frac{A'B'}{AB} \dots (1)$$

 $\Delta MOF_2 \& \Delta A'B'F_2$ are similar.

$$\frac{MO}{OF_2} = \frac{A'B'}{B'F_2}$$

And, we know,

$$MO = AB$$

$$\Rightarrow \frac{AB}{OF_2} = \frac{A'B'}{B'F_2}$$

$$\Rightarrow \frac{B'F_2}{OF_2} = \frac{A'B'}{AB} \dots (2)$$

From (1) & (2),

$$\frac{B'F_2}{OF_2} = \frac{B'O}{BO}$$

Put BO = -u, B'O = v, $OF_2 = f$, $B'F_2 = v - f$ in above equation,

$$\Rightarrow \frac{v-f}{f} = \frac{v}{-u}$$

$$\Rightarrow$$
 -uv + fu = vf

Divide by uvf

$$\Rightarrow -\frac{1}{f} + \frac{1}{v} = \frac{1}{u}$$

$$\Rightarrow \frac{1}{v} - \frac{1}{u} = \frac{1}{f}$$

This is derived.

3. By stating sign conventions and assumptions used derive the relation between u, v & f in case of a concave mirror?



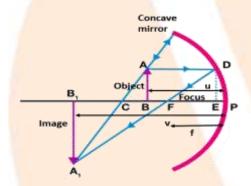
Ans: Sign conventions:

- 1) All distances are estimated from the mirror's pole.
- 2) Distance measured in the incident light direction is positive, and those measured in the direction reverse to the incident light are negative.
- 3) Height estimated upwards is positive and height estimated downwards is negative.

Assumptions:

- 1) Spherical mirror's aperture is supposed to be very small.
- 2) The incident and refracted rays form small angles with the principal axis.

This figure shows image produced by the concave mirror.



$$\angle ACB = \angle A_1CB_1$$
 [opposite angles]

$$\angle ABC = \angle A_1B_1C$$
 [right angles]

This gives,
$$\angle BAC = \angle CA_1B_1$$

$$\frac{AB}{A_1B_1} = \frac{BC}{B_1C} \quad \dots (1)$$

$$\Delta FED \sim \Delta FA_1B_1$$

$$\frac{ED}{A_1B_1} = \frac{EF}{FB_1}$$

Also,
$$ED = AB$$



$$\frac{AB}{A_1B_1} = \frac{EF}{FB_1}$$

Combining (1) and (2),

$$\frac{BC}{B_1C} = \frac{EF}{FB_1}$$

We are considering that E is close to P, so, EF=PF

$$\frac{BC}{B_1C} = \frac{PF}{FB_1}$$

From figure,

$$BC = -R - (-u), B_1C = -v - (-R), PF = -f, FB_1 = -v - (-f)$$

Now,

$$\Rightarrow \frac{-R+u}{-v+R} = \frac{-f}{-v+f}$$

$$\Rightarrow$$
 uv - uf - Rv + Rf = Rf - vf

$$\Rightarrow$$
 uv - uf - Rv = -vf

Put
$$R = 2f$$

$$\Rightarrow$$
 uv - uf - 2fv = -vf

$$\Rightarrow$$
 uv – uf – fv = 0

Dividing by uvf

$$\frac{1}{f} = \frac{1}{u} + \frac{1}{v}$$

Hence, derived.

4.

a) A person looking at a mesh of crossed wires is able to see the vertical lines more distinctly than the horizontal wires. What is the effect due to? How is such a defect of vision corrected?



Ans: In the given case, the person can see vertical lines more precisely than horizontal lines.

This means that the eye's refracting system (cornea and eye-lens) is not working similarly in different planes. This defect is named astigmatism.

The person's eye has sufficient curvature in the vertical plane. However, the horizontal plane's curvature is insufficient. Hence, sharp vertical lines are made on the retina, but horizontal lines seem blurred.

This defect can be fixed by using cylindrical lenses.

- b) A man with normal near point (25cm) reads a book with small print using a magnifying glass: a thin convex lens of focal length 5cm.
 - i) What is the closest and the farthest distance at which he can read the book when viewing through the magnifying glass?

Ans: Given that,

Focal length of the magnifying glass, f = 5 cm

Least distance of distance vision, d = 25 cm

Closest Object distance = u

Image distance, v = -d = -25cm

Using lens formula,

$$\frac{1}{f} = \frac{1}{v} - \frac{1}{u}$$

$$\Rightarrow \frac{1}{5} = \frac{1}{-25} - \frac{1}{u}$$

$$\Rightarrow u = \frac{-25}{6} \text{cm} = -4.167 \text{cm}$$

Hence, the nearest distance at which the person can read the book is 4.167 cm.

For the object at the farthest distance (u'), the image distance (v') = ∞

Using lens formula,



$$\frac{1}{f} = \frac{1}{v'} - \frac{1}{u'}$$

$$\Rightarrow \frac{1}{5} = \frac{1}{\infty} - \frac{1}{\mathbf{u}'}$$

$$\Rightarrow$$
 u' = -5cm

Hence, the farthest distance at which the person can read the book is 5cm.

ii) What is the maximum and minimum angular magnificent (magnifying power) possible using the above simple microscope?

Ans: The formula for maximum angular magnification is given by:

$$a_{\text{max}} = \frac{d}{|u|}$$

$$\Rightarrow$$
 $a_{\text{max}} = \frac{25}{\frac{25}{6}} = 6$

The formula for minimum angular magnification is given by:

$$a_{\min} = \frac{d}{|u'|}$$

$$\Rightarrow$$
 $a_{min} = \frac{25}{5} = 5$

Thus, the maximum and the minimum angular magnification (magnifying power) possible using the given simple microscope are 6 and 5 respectively.

5. Four double convex lens with following specification are available.

	Lens focal	Aperture
	length	
A	100 cm	10 cm
В	100 cm	5 cm
C	10 cm	2 cm
D	5 cm	2 cm



a) Which of the given four lenses should be selected as objective and eyepiece to construct an astronomical telescope and why? What will be the magnifying power and length of the tube of this telescope?

Ans: The telescope's objective should be of large aperture so that it can receive maximum light and should be of large focal length so that it can produce maximum magnification.

From table, we choose lens A as objective and lens D as eyepiece due to small aperture and small focal length.

$$f_0 = 100 \text{cm}, f_e = 5 \text{cm}$$

Magnification,

$$m = \frac{f_o}{f_e}$$

$$m = \frac{100}{5} = 20$$

Normal length, $L = f_0 + f_e = 100 + 5 = 105$ cm

The magnification is 20 and the length of telescope's tube is 105cm.

b) An object is seen with the help of a simple microscope, firstly in red light and then is blue light. Will the magnification be same in both the cases? Why?

Ans: The focal length of lens is small for violet light than red light and magnifying power is inversely dependent on the focal length. So, magnification for violet light will be larger.

6. A small candle, 2.5 cm in size is placed at 27 cm in front of a concave mirror of radius of curvature 36cm. At what distance from the mirror should a screen be placed in order to obtain a sharp image? Describe the nature and size of the image. If the candle is moved closer to the mirror, how would the screen have to be moved?

Ans: We have,

Size of the candle, h = 2.5cm



Let image size = h'

Object distance, u = -27cm

concave mirror's curvature radius, R = -36cm

Focal length of the concave mirror, $f = \frac{R}{2} = -18cm$

Using mirror formula,

$$\frac{1}{u} + \frac{1}{v} = \frac{1}{f}$$

$$\Rightarrow \frac{1}{v} = \frac{1}{f} - \frac{1}{u}$$

Where, u is the object distance,

v is the image distance and

f is the focal length.

Now, we put given values,

$$\Rightarrow \frac{1}{v} = \frac{1}{-18} - \frac{1}{-27}$$

$$\Rightarrow \frac{1}{y} = \frac{-3+2}{54}$$

$$\Rightarrow \frac{1}{v} = \frac{-1}{54}$$

$$\Rightarrow$$
 v = -54cm

Therefore, the screen should be 54 cm away from the mirror to get a sharp image.

The formula for magnification of image is given by:

$$m = \frac{h'}{h} = -\frac{v}{u}$$



$$\therefore h' = -\frac{v}{u} \times h$$

$$\Rightarrow$$
 h' = $-\frac{-54}{-27} \times 2.5$

$$\Rightarrow$$
 h' = -5cm

The height of the image of the candle is 5 cm. The negative sign shows that the image is inverted and real.

If the candle is moved nearer to the mirror, then the screen will have to be moved far from the mirror in order to get the image.

7. A 4.5 cm needle is placed 12cm away from a convex mirror of focal length 15cm. Give the location of the image and the magnification. Describe what happens as the needle is moved farther from the mirror.

Ans: Given that,

Height of the needle, $h_1 = 4.5 \text{cm}$

Object distance, u = -12cm

Focal length of the convex mirror, f = 15cm

Image distance = v

Using mirror formula,

$$\frac{1}{u} + \frac{1}{v} = \frac{1}{f}$$

$$\Rightarrow \frac{1}{v} = \frac{1}{f} - \frac{1}{u}$$

Now, we put given values,

$$\Rightarrow \frac{1}{v} = \frac{1}{15} - \frac{1}{-12}$$

$$\Rightarrow \frac{1}{v} = \frac{4+5}{60}$$



$$\Rightarrow \frac{1}{v} = \frac{9}{60}$$

$$\Rightarrow$$
 v = 6.7cm

Hence, the needle's image is 6.7 cm away from the mirror and it is on the mirror's other side.

The formula for magnification of image is given by:

$$\mathbf{m} = \frac{\mathbf{h}_2}{\mathbf{h}_1} = -\frac{\mathbf{v}}{\mathbf{u}}$$

$$\therefore \mathbf{h}_2 = -\frac{\mathbf{v}}{\mathbf{u}} \times \mathbf{h}_1$$

$$\Rightarrow h_2 = -\frac{6.7}{-12} \times 4.5$$

$$\Rightarrow$$
 h₂ = 2.5cm

Hence, magnification,

$$m = \frac{2.5}{4.5} = 0.56$$

The image's height is 2.5cm. The positive sign shows that the image is virtual, erect, and diminished.

If the needle is moved away from the mirror, the image will also move farther from the mirror, and the size of the image will decrease gradually.

8. A tank is filled with water to a height of 12.5 cm. The apparent depth of a needle lying at the bottom of the tank is measured by a microscope to be 9.4cm. What is the refractive index of water? If water is replaced by a liquid of refractive index 1.63 up to the same height, by what distance would the microscope have to be moved to focus on the needle again?

Ans: Given that,

Actual depth of the needle in water, $h_1 = 12.5$ cm

Apparent depth of the needle in water, $h_2 = 9.4$ cm



Refractive index of water $=\mu$

The formula for refractive index is given by:

$$\mu = \frac{h_1}{h_2}$$

Put the given values,

$$\mu = \frac{12.5}{9.4}$$

$$\mu \approx 1.33$$

Hence, the water's refractive index is about 1.33.

When water is replaced by a liquid of refractive index, $\mu'=1.63$.

The actual depth of the needle will be the same, but it's apparent depth will vary.

Let y be the new apparent depth of the needle.

We will use the relation given below:

$$\mu' = \frac{h_1}{y}$$

$$\therefore y = \frac{h_1}{\mu'}$$

$$\Rightarrow y = \frac{12.5}{1.63}$$

$$\Rightarrow$$
 y = 7.67cm

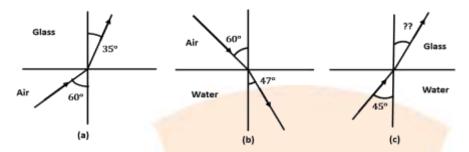
We get the new apparent depth of the needle to be 7.67cm. It is less than h_2 . Therefore, the microscope should be moved up to focus the needle again.

The distance by which the microscope would be moved up = 9.4 - 7.67 = 1.73cm.

9. Figures (a) and (b) show refraction of a ray in air incident at 60° with the normal to a glass-air and water air interface, respectively. Predict the



angle of refraction in glass when the angle of incidence in water is 45° with the normal to a water-glass interface [figure (c)].



Ans: Given that,

For the glass -air interface,

Angle of incidence, $i = 60^{\circ}$

Angle of refraction, $r = 35^{\circ}$

We can use Snell's law,

$$\mu_g^a = \frac{\sin i}{\sin r}$$

$$\Rightarrow \mu_g^a = \frac{\sin 60^\circ}{\sin 35^\circ}$$

$$\Rightarrow \mu_g^a = 1.51....(i)$$

For the air-water interface,

Angle of incidence, $i = 60^{\circ}$

Angle of refraction, $r = 47^{\circ}$

We can use Snell's law,

$$\mu_{\rm w}^{\rm a} = \frac{\sin i}{\sin r}$$

$$\Rightarrow \mu_{\rm w}^{\rm a} = \frac{\sin 60^{\circ}}{\sin 47^{\circ}}$$

$$\Rightarrow \mu_w^a = 1.184 \dots (ii)$$



Using (i) and (ii), the relative refractive index of glass with respect to water can be derived as:

$$\mu_g^w = \frac{\mu_g^a}{\mu_w^a}$$

$$\Longrightarrow \mu_g^{\rm w} = \frac{1.51}{1.184}$$

$$\Rightarrow \mu_g^w = 1.275$$

For the glass - water interface,

Angle of incidence, $i = 45^{\circ}$

Angle of refraction, = r

We can use Snell's law,

$$\mu_{\rm g}^{\rm w} = \frac{\sin i}{\sin r}$$

$$\Rightarrow 1.275 = \frac{\sin 45^{\circ}}{\sin r}$$

$$\Rightarrow$$
 sin r = 0.5546

$$\Rightarrow r = \sin^{-1}(0.5546)$$

$$\Rightarrow$$
 r = 38.68°

Hence, the angle of refraction at the water – glass interface is 38.68°.

10. A small bulb is placed at the bottom of a tank containing water to a depth of 80 cm. What is the area of the surface of water through which light from the bulb can emerge out? Refractive index of water is 1.33. (Consider the bulb to be a point source.)

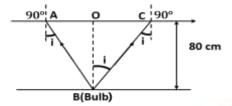
Ans: Provided that,

Bulb's actual depth in water, $d_1 = 80 \text{cm} = 0.8 \text{m}$

Water's refractive index, $\mu = 1.33$



The following diagram represents the given setup:



Where, i is the Angle of incidence

r is the Angle of refraction, $r = 90^{\circ}$

As the bulb acts as a point source, the emergent light would be considered as a circle of radius, $R = \frac{AC}{2} = AO = OB$

Snell's law may be used as follows:

$$\mu = \frac{\sin r}{\sin i}$$

$$\Rightarrow 1.33 = \frac{\sin 90^{\circ}}{\sin i}$$

$$\Rightarrow \sin i = \frac{1}{1.33}$$

$$\Rightarrow$$
 i = 48.75°

Considering the given diagram, we have the relation:

$$tan i = \frac{OC}{OB} = \frac{R}{d_1}$$

$$\Rightarrow$$
 R = tan 48.75°×0.8

$$\Rightarrow$$
 R = 0.91m

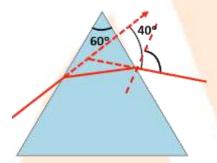
Area of the surface of water = $\pi R^2 = \pi (0.91)^2 = 2.61 \text{m}^2$

Clearly, the area of the water surface through which the light from the bulb could project is about 2.61m^2 .



11. A prism is made of glass of unknown refractive index. A parallel beam of light is incident on a face of the prism. The angle of minimum deviation is measured to be 40° . What is the refractive index of the material of the prism? The refracting angle of the prism is 60° . If the prism is placed in water (refractive index 1.33), predict the new angle of minimum deviation of a parallel beam of light.

Ans: The minimum deviation angle and the angle of prism is as shown in figure given below:



Angle of minimum deviation, $\delta_{\rm m} = 40^{\circ}$

Angle of the prism, $A = 60^{\circ}$

Refractive index of water, $\mu = 1.33$

Refractive index of the material of the prism = μ '

The relation between angle of deviation with refractive index is given by:

$$\mu' = \frac{\sin\left(\frac{A + \delta_{m}}{2}\right)}{\sin\left(\frac{A}{2}\right)}$$

$$\Rightarrow \mu' = \frac{\sin\left(\frac{60^{\circ} + 40^{\circ}}{2}\right)}{\sin\left(\frac{60^{\circ}}{2}\right)} = \frac{\sin 50^{\circ}}{\sin 30^{\circ}}$$

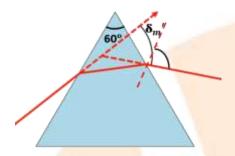
$$\Rightarrow \mu' = 1.532$$

Hence, the refractive index of the prism is 1.532.



Since the prism is placed in water, let δ'_m be the new angle of minimum deviation for the same prism.

The below figure shows the angle of prism and the unknown minimum deviation angle.



The refractive index of glass with respect to water is given by the relation:

$$\mu_{g}^{w} = \frac{\mu'}{\mu} = \frac{\sin\left(\frac{A + \delta'_{m}}{2}\right)}{\sin\left(\frac{A}{2}\right)}$$

$$\Rightarrow \frac{\mu'}{\mu}\sin\left(\frac{A}{2}\right) = \sin\left(\frac{A + \delta'_{m}}{2}\right)$$

$$\therefore (A + \delta'_{m}) \quad 1.532 \quad . \quad ($$

$$\Rightarrow \sin\left(\frac{A + \delta'_{m}}{2}\right) = \frac{1.532}{1.33}\sin\left(\frac{60^{\circ}}{2}\right) = 0.5759$$

$$\Rightarrow \frac{A + \delta'_{m}}{2} = \sin^{-1}(0.5759) = 35.16^{\circ}$$

$$\Rightarrow$$
 60° + $\delta'_{\rm m}$ = 70.32°

$$\Rightarrow \delta'_{\rm m} = 10.32^{\circ}$$

Hence, the new minimum angle of deviation is 10.32°.

12. A compound microscope consists of an objective lens of focal length 2.0 cm and an eyepiece of focal length 6.25 cm separated by a distance of 15 cm. How far from the objective should an object be placed in order to obtain the final image at:



a) the least distance of distinct vision $(25\ cm)$? What is the magnifying power of the microscope?

Ans: Given that,

Focal length of the objective lens, $f_1 = 2.0$ cm

Focal length of the eyepiece, $f_2 = 6.25$ cm

Distance between the objective lens and the eyepiece, d = 15 cm

Least distance of distinct vision, d' = 25 cm

lmage distance for the eyepiece, $v_2 = -25$ cm

Object distance for the eyepiece = u_2

Using lens formula,

$$\frac{1}{v_2} - \frac{1}{u_2} = \frac{1}{f_2}$$

$$\Rightarrow \frac{1}{\mathbf{u}_2} = \frac{1}{\mathbf{v}_2} - \frac{1}{\mathbf{f}_2}$$

$$\Rightarrow \frac{1}{u_2} = \frac{1}{-25} - \frac{1}{6.25}$$

$$\Rightarrow \frac{1}{u_2} = \frac{-5}{25}$$

$$\Rightarrow$$
 u₂ = -5cm

The distance of image for the objective lens, $v_1 = d + u_2 = 15 - 5 = 10 \text{cm}$.

The distance of object for the objective lens = u_1

Using lens formula,

$$\frac{1}{v_1} - \frac{1}{u_1} = \frac{1}{f_1}$$



$$\Rightarrow \frac{1}{u_1} = \frac{1}{v_1} - \frac{1}{f_1}$$

$$\Rightarrow \frac{1}{u_1} = \frac{1}{10} - \frac{1}{2}$$

$$\Rightarrow \frac{1}{u_1} = \frac{-4}{10}$$

$$\Rightarrow$$
 $u_1 = -2.5cm$

Magnitude of the object distance, $|u_1| = 2.5 \text{cm}$.

The compound microscope's magnifying power is given by the relation:

$$m = \frac{V_1}{|u_1|} \left(1 + \frac{d'}{f_2} \right)$$

$$\Rightarrow m = \frac{10}{2.5} \left(1 + \frac{25}{6.25} \right)$$

$$\Rightarrow$$
 m = 4(1+4) = 20

Hence, the magnifying power of the microscope is 20.

b) at infinity? What is the magnifying power of the microscope?

Ans: Given that, the final image is formed at infinity.

The distance of image of the eyepiece, $v_2 = \infty$

The distance of object of the eyepiece = u_2

Using lens formula,

$$\frac{1}{v_2} - \frac{1}{u_2} = \frac{1}{f_2}$$

$$\Rightarrow \frac{1}{\mathbf{u}_2} = \frac{1}{\mathbf{v}_2} - \frac{1}{\mathbf{f}_2}$$



$$\Rightarrow \frac{1}{\mathbf{u}_2} = \frac{1}{\infty} - \frac{1}{6.25}$$

$$\Rightarrow$$
 u₂ = -6.25cm

The distance of image for the objective lens, $v_1 = d + u_2 = 15 - 6.25 = 8.75$ cm

The distance of object for the objective lens = u_1

Using lens formula,

$$\frac{1}{v_1} - \frac{1}{u_1} = \frac{1}{f_1}$$

$$\Rightarrow \frac{1}{\mathbf{u}_1} = \frac{1}{\mathbf{v}_1} - \frac{1}{\mathbf{f}_1}$$

$$\Rightarrow \frac{1}{u_1} = \frac{1}{8.75} - \frac{1}{2}$$

$$\Rightarrow$$
 u₁ = -2.59cm

Magnitude of the object distance, $|u_1| = 2.59 \text{cm}$.

The compound microscope's magnifying power is given by the relation:

$$\mathbf{m} = \frac{\mathbf{v}_1}{|\mathbf{u}_1|} \left(\frac{\mathbf{d'}}{|\mathbf{u}_2|} \right)$$

$$\Rightarrow m = \frac{8.75}{2.59} \left(\frac{25}{6.25} \right)$$

$$\Rightarrow$$
 m = 13.51

Hence, the magnifying power of the microscope is 13.51.

13. A person with a normal near point (25 cm) using a compound microscope with objective of focal length 8.0 mm and an eyepiece of focal length 2.5 cm can bring an object placed at 9.0 mm from the objective in sharp focus. What is the separation between the two lenses? Calculate the magnifying power of the microscope.



Ans: Given that,

Focal length of the objective lens, $f_0 = 8 \text{ mm} = 0.8 \text{ cm}$

Focal length of the eyepiece, $f_e = 2.5$ cm

The distance of the object for the Objective lens, $u_0 = -9.0 \text{ mm} = -0.9 \text{ cm}$

Least distance of distant vision, d = 25 cm

Image distance for the eyepiece, $v_e = -d = -25$ cm

Object distance for the eyepiece, u_e

Using lens formula,

$$\frac{1}{v_e} - \frac{1}{u_e} = \frac{1}{f_e}$$

$$\Rightarrow \frac{1}{u_e} = \frac{1}{v_e} - \frac{1}{f_e}$$

$$\Rightarrow \frac{1}{u_e} = \frac{1}{-25} - \frac{1}{2.5}$$

$$\Rightarrow \frac{1}{u_e} = \frac{-11}{25}$$

$$\Rightarrow$$
 u_e = -2.27 cm

Using lens formula, we can obtain image distance for the objective lens, $v_{\rm o}$, is given by:

$$\frac{1}{v_0} - \frac{1}{u_0} = \frac{1}{f_0}$$

$$\Rightarrow \frac{1}{v_o} = \frac{1}{u_o} + \frac{1}{f_o}$$

$$\Rightarrow \frac{1}{v_o} = \frac{1}{0.8} - \frac{1}{0.9}$$



$$\Rightarrow \frac{1}{v_0} = \frac{0.1}{0.72}$$

$$\Rightarrow$$
 $v_0 = 7.2$ cm

The distance between the objective lens and the eyepiece, $|\mathbf{u}_e| + \mathbf{v}_o = 2.27 + 7.2 = 9.47 \text{cm}$

The microscope's magnifying power is given by the relation:

$$m = \frac{v_o}{|u_o|} \left(1 + \frac{d}{f_e} \right)$$

$$\Rightarrow m = \frac{7.2}{0.9} \left(1 + \frac{25}{2.5} \right)$$

$$\Rightarrow$$
 m = 8(1+10) = 88

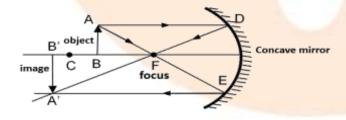
Hence, the magnifying power of the microscope is 88.

14. Use the mirror equation to deduce that:

a) an object placed between f and 2f of a concave mirror produces a real image beyond 2f.

Ans: For a concave mirror, f < 0.

When the object is placed on the left side of the mirror, then u < 0.



Using mirror formula,

$$\frac{1}{u} + \frac{1}{v} = \frac{1}{f}$$



$$\Rightarrow \frac{1}{v} = \frac{1}{f} - \frac{1}{u} \dots (1)$$

If the object placed between f and 2f i.e., 2f < u < f:

$$\Rightarrow \frac{1}{2f} > \frac{1}{u} > \frac{1}{f}$$

$$\Rightarrow -\frac{1}{2f} < -\frac{1}{u} < -\frac{1}{f}$$

$$\Rightarrow \frac{1}{f} - \frac{1}{2f} < \frac{1}{f} - \frac{1}{u} < 0 \dots (2)$$

Using equation (1), we get

$$\Rightarrow \frac{1}{2f} < \frac{1}{v} < 0$$

Since $\frac{1}{v}$ is negative, v is negative.

$$\Rightarrow \frac{1}{2f} < \frac{1}{v}$$

$$\Rightarrow 2f > v$$

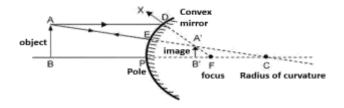
$$\Rightarrow -v > -2f$$

Therefore, image will lie beyond 2f.

b) a convex mirror always produces a virtual image independent of the location of the object.

Ans: For a convex mirror, f > 0.

When the object is placed on the left side of the mirror, then u < 0.





Using mirror formula,

$$\frac{1}{u} + \frac{1}{v} = \frac{1}{f}$$

$$\Rightarrow \frac{1}{v} = \frac{1}{f} - \frac{1}{u}$$

Using equation (2), we get:

$$\frac{1}{v} < 0$$

$$\Rightarrow$$
 v > 0

Thus, the image is formed on the mirror's back side.

Hence, a convex mirror always gives a virtual image, regardless of the object distance.

c) the virtual image produced by a convex mirror is always diminished in size and is located between the focus and the pole.

Ans: For a convex mirror, f > 0.

Using mirror formula,

$$\frac{1}{u} + \frac{1}{v} = \frac{1}{f}$$

$$\Rightarrow \frac{1}{v} = \frac{1}{f} - \frac{1}{u}$$

But we have, u < 0

$$\therefore \frac{1}{v} > \frac{1}{f}$$

$$\Rightarrow$$
 v < f

Hence, the image formed is diminished and is located between the focus and the pole.



d) An object placed between the pole and focus of a concave mirror produces a virtual and enlarged image.

Ans: For a concave mirror, f < 0.

When the object is placed on the left side of the mirror, then u < 0.

The object is placed between the focus and the pole.

$$\therefore f > u > 0$$

$$\Rightarrow \frac{1}{f} < \frac{1}{u} < 0$$

$$\Rightarrow \frac{1}{f} - \frac{1}{u} < 0$$

$$\therefore \frac{1}{v} < 0$$

$$\Rightarrow$$
 v > 0

The image is formed on the mirror's right side. Hence, it is a virtual image.

For u < 0, v > 0

$$\Rightarrow \frac{1}{11} > \frac{1}{V}$$

$$\Rightarrow$$
 v > u

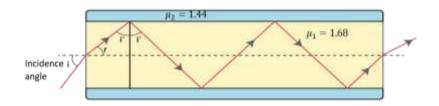
Magnification,
$$m = \frac{v}{u} > 1$$

Hence, the formed image is enlarged.

15.

a) Figure shows a cross-section of a 'light pipe' made of a glass fibre of refractive index 1.68. The outer covering of the pipe is made of a material of refractive index 1.44. What is the range of the angles of the incident rays with the axis of the pipe for which total reflections inside the pipe take place, as shown in the figure?





Ans: Given that,

Refractive index of the glass fibre, $\mu_1 = 1.68$

Refractive index of the outer covering of the pipe, $\mu_2 = 1.44$

Angle of incidence = i

Angle Of refraction = r

Angle of incidence at the interface = i'

The refractive index (μ) of the inner core - outer core interface is given as:

$$\mu = \frac{\mu_2}{\mu_1} = \frac{1}{\sin i}$$

$$\Rightarrow \sin i' = \frac{\mu_1}{\mu_2}$$

$$\Rightarrow \sin i' = \frac{1.44}{1.68} = 0.8571$$

For the critical angle, total internal reflection (TIR) takes place only when i > i'.

That is, when $i > 59^{\circ}$.

Maximum angle of reflection, $r_{max} = 90^{\circ} - i' = 90^{\circ} - 59^{\circ} = 31^{\circ}$.

Let i_{max} be the maximum incidence angle.

The refractive index at the air – glass interface, $\mu_1 = 1.68$.

We can use the relation for the maximum angles of incidence and reflection as:

$$\mu_1 = \frac{\sin i_{\text{max}}}{\sin r_{\text{max}}}$$

$$\Rightarrow \sin i_{\max} = \mu_1 \times \sin r_{\max}$$



$$\Rightarrow \sin i_{\text{max}} = 1.68 \times \sin 31^{\circ}$$

$$\Rightarrow \sin i_{max} = 0.8652$$

$$\Rightarrow i_{max} \approx 60^{\circ}$$

Thus, all the ray's incident at angles lying in the range $0 < i < 60^{\circ}$ will suffer total internal reflection.

b) What is the answer if there is no outer covering of the pipe?

Ans: If the outer covering of the pipe is not present, then:

Refractive index of the outer pipe = μ_1

Refractive index of air = 1

For the angle of incidence $i = 90^{\circ}$, we can use Snell's law at the air – pipe interface as

$$\mu_2 = \frac{\sin i}{\sin r}$$

$$\Rightarrow 1.68 = \frac{\sin 90^{\circ}}{\sin r}$$

$$\Rightarrow \sin r = \frac{1}{1.68}$$

$$\Rightarrow$$
 r = 36.5°

$$\therefore i' = 90^{\circ} - 36.5^{\circ} = 53.5^{\circ}$$

Since, i'>r, all incident rays will suffer total internal reflection.

16. Answer the following questions:

a) You have learnt that plane and convex mirrors produce virtual images of objects. Can they produce real images under some circumstances? Explain.

Ans: Yes. Plane and convex mirrors can provide real images as well.



If the light rays converging at a point behind a plane mirror (or a convex mirror) are reflected on a screen placed in front of the mirror, then an actual image will be formed.

b) A Virtual image, we always say, cannot be caught on a screen. Yet when we 'see' a virtual image, we are obviously bringing it on to the 'screen' (i.e., the retina) of our eye. Is there a contradiction?

Ans: No. A virtual image is made when light rays diverge.

The convex lens of the eye makes these divergent rays converge at the retina. The virtual image works as an object for the lens to provide an actual image in this situation.

c) A diver underwater, looks obliquely at a fisherman standing on the bank of a lake. Would the fisherman look taller or shorter to the diver than what he actually is?

Ans: The diver is in the water, and the fisherman is on the land. Water is a denser medium than air.

It is provided that the diver is viewing the fisherman. This shows that the light rays are traveling from a denser medium to a rarer medium.

Hence, the refracted rays will go away from the normal. As a result, the fisherman will seem to be taller.

d) Does the apparent depth of a tank of water change if viewed obliquely? If so, does the apparent depth increase or decrease?

Ans: Yes, the apparent depth decreases. The tank's apparent depth of water varies when viewed obliquely.

This is because the light deviates on traveling from one medium to another. The tank's apparent depth, when viewed obliquely, is less than the near-normal viewing.

e) The refractive index of diamond is much greater than that of ordinary glass. Is this fact of some use to a diamond cutter?



Ans: The diamond's refractive index is more than that of ordinary glass.

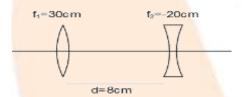
The critical angle for diamond is smaller than that for glass.

A diamond cutter utilizes a large angle of incidence to guarantee that the light entering the diamond is totally reflected from its face. This is the cause for the sparkling effect of a diamond.

17.

a) Determine the 'effective focal length' of the combination of the two lenses in Exercise 9.10, if they are placed 8.0 cm apart with their principal axes coincident. Does the answer depend on which side of the combination a beam of parallel light is incident? Is the notion of effective focal length of this system useful at all?

Ans: Consider the diagram below which represents the combination of two lenses.



Here,

Focal length of the convex lens, $f_1 = 30$ cm

Focal length of the concave lens, $f_2 = -20$ cm

Distance between the two lenses, d = 8.0 cm

First, consider the case when the parallel beam of light falls on the convex lens.

Using lens formula,

$$\frac{1}{v_1} - \frac{1}{u_1} = \frac{1}{f_1}$$

Where, object distance, $u_1 = \infty$

Image distance = v_1



$$\Rightarrow \frac{1}{v_1} = \frac{1}{30} - \frac{1}{\infty} = \frac{1}{30}$$

$$\Rightarrow$$
 v₁ = 30cm

The image will serve as a virtual object for the concave lens.

Using lens formula,

$$\frac{1}{v_2} - \frac{1}{u_2} = \frac{1}{f_2}$$

Where, object distance = u_2 .

$$u_2 = 30 - 8 = 22cm$$

Image distance = v_2 .

$$\Rightarrow \frac{1}{v_2} = \frac{1}{22} - \frac{1}{20} = \frac{-1}{220}$$

$$\Rightarrow$$
 $v_2 = -220$ cm

The parallel incident beam seems to diverge from a point, that is, $220 - \frac{d}{2} = 220 - 4 = 216$ cm from the centre of the combination of the two lenses.

Secondly, when the parallel beam of light falls, from the left, on the concave lens;

Using lens formula,

$$\frac{1}{v_2} - \frac{1}{u_2} = \frac{1}{f_2}$$

Where, object distance, $u_2 = -\infty$.

Image distance = v_2 .

$$\Rightarrow \frac{1}{v_2} = \frac{1}{-20} - \frac{1}{\infty} = \frac{1}{-20}$$

$$\Rightarrow$$
 $v_2 = -20cm$



The image will serve as a real object for the convex lens.

Using lens formula,

$$\frac{1}{v_1} - \frac{1}{u_1} = \frac{1}{f_1}$$

Where, object distance, $= u_1$.

$$u_1 = -(20 + 8) = -28cm$$
.

Image distance = v_1 .

$$\Rightarrow \frac{1}{v_1} = \frac{1}{30} + \frac{1}{-28} = \frac{-1}{420}$$

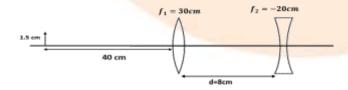
$$\Rightarrow$$
 $v_1 = -420$ cm

Hence, the parallel incident beam seems to diverge from a point, that is =420-4=416cm from the left of the centre of the combination of the two lenses.

Thus, the answer does depend on the combination side at which the parallel beam of light is incident. The notion of effective focal length does not appear to be useful for this combination.

b) An object 1.5 cm in size is placed on the side of the convex lens in the arrangement (a) above. The distance between the object and the convex lens is 40cm. Determine the magnification produced by the two-lens system, and the size of the image.

Ans: Consider the given diagram of the previous arrangement as follows:



Here, it is said that,

Height of the image, $h_1 = 1.5$ cm

Object distance from the side of the convex lens, $u_1 = -40$ cm



 $|u_1| = 40cm$

Using lens formula,

$$\frac{1}{v_1} - \frac{1}{u_1} = \frac{1}{f_1}$$

$$\Rightarrow \frac{1}{v_1} = \frac{1}{30} + \frac{1}{-40} = \frac{1}{120}$$

$$\Rightarrow$$
 v₁ = 120cm

Magnification, $m = \frac{v_1}{|u_1|}$

$$\Rightarrow$$
 m = $\frac{120}{40}$ = 3

Hence, the magnification due to the convex lens is 3.

The image made by the convex lens acts as an object for the concave lens.

Using lens formula,

$$\frac{1}{v_2} - \frac{1}{u_2} = \frac{1}{f_2}$$

Where, object distance = u_2 .

$$u_2 = 120 - 8 = 112 \text{cm}$$
.

Image distance = v_2 .

$$\Rightarrow \frac{1}{v_2} = \frac{1}{-20} + \frac{1}{112} = \frac{-92}{2240}$$

$$\Rightarrow v_2 = -\frac{2240}{92} \text{cm}$$

Magnification, m' = $\frac{|v_1|}{|u_1|}$



$$\Rightarrow \text{m'} = \frac{2240}{92} \times \frac{1}{112} = \frac{20}{92}$$

Hence, the magnification due to the concave lens is $\frac{20}{92}$.

The magnification due to the combination of the two lenses is calculated as:

$$m \times m' = 3 \times \frac{20}{92} = 0.652$$

Thus,

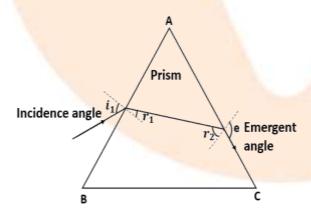
$$\frac{h_2}{h_1} = 0.652$$

$$\Rightarrow$$
 h₂ = 0.652 × 1.5 = 0.98cm

Clearly, the height of the image is 0.98cm.

18. At what angle should a ray of light be incident on the face of a prism of refracting angle 60° so that it just suffers total internal reflection at the other face? The refractive index of the material of the prism is 1.524.

Ans: Consider the given figure below:



Angle of prism, $A = 60^{\circ}$

i, is the incidence angle.

 $\mathbf{r}_{2} \ \mathbf{r}_{1}$ is the refracted angle.



is the angle of incidence at the face AC.

e is the emergent angle, $e = 90^{\circ}$.

Using Snell's law,

$$\mu = \frac{\sin e}{\sin r_2}$$

$$\Rightarrow 1.524 = \frac{\sin 90^{\circ}}{\sin r_2}$$

$$\Rightarrow \sin r_2 = 0.6562$$

$$\Rightarrow$$
 r₂ $\approx 41^{\circ}$

For refraction through prism, angle $A = r_1 + r_2$.

We get,

$$r_1 = A - r_2 = 60^{\circ} - 41^{\circ}$$

$$\therefore r_1 = 19^{\circ}$$

Using Snell's law,

$$\mu = \frac{\sin i_1}{\sin r_1}$$

$$\Rightarrow 1.524 = \frac{\sin i_1}{\sin 19^\circ}$$

$$\Rightarrow \sin i_1 = 0.496$$

$$\Rightarrow$$
 $i_1 = 29.75^{\circ}$

Hence, the incidence angle is 29.75°.

19. For a normal eye, the far point is at infinity and the near point of distinct vision is about 25cm in front of the eye. The cornea of the eye provides a converging power of about 40 dioptres, and the least converging power of the eye-lens behind the cornea is about 20 dioptres. From this



rough data estimate the range of accommodation (i.e., the range of converging power of the eye-lens) of a normal eye.

Ans: Given that,

Least distance of distinct vision, d = 25 cm

Far point of a normal eye, $d' = \infty$

Converging power of the cornea, $P_c = 40D$

Least converging power of the eye-lens, $P_e = 20D$

To see the objects at infinity, the eye uses its least converging power.

Power of the eye-lens, $P = P_c + P_e = 40 + 20 = 60D$

Power of the eye-lens is given as:

$$P = \frac{1}{f}$$

$$\Rightarrow f = \frac{1}{P}$$

$$\Rightarrow$$
 f = $\frac{1}{60}$ m = $\frac{5}{3}$ cm

Object distance, u = -d = -25cm

Image distance, $v = f = \frac{5}{3}$ cm

Using lens formula,

$$\frac{1}{f'} = \frac{1}{v} - \frac{1}{u}$$

$$\Rightarrow \frac{1}{f'} = \frac{3}{5} - \frac{1}{-25} = \frac{16}{25} \text{cm}^{-1}$$

Power,
$$P = \frac{1}{f'} \times 100$$



$$\Rightarrow P = \frac{16}{25} \times 100 = 64D$$

Power of the eye lens = 64 - 40 = 24D

Hence, the range of accommodation of the eye-lens is from 20 D to 24 D.

20.

a) The angle subtended at the eye by an object is equal to the angle subtended at the eye by the virtual image produced by a magnifying glass. In what sense then does a magnifying glass provide angular magnification?

Ans: Though the image size is larger than the object, the angular size of the image is equivalent to the angular size of the object.

A magnifying glass supports one seeing the objects closer than the least distance of distinct vision. A closer object produces a larger angular size.

A magnifying glass gives angular magnification. Without magnification, the object cannot be located closer to the eye. With magnification, the object can be set much closer to the eye.

b) In viewing through a magnifying glass, one usually positions one's eyes very close to the lens. Does angular magnification change if the eye is moved back?

Ans: Yes, the angular magnification varies.

When the length between the eye and a magnifying glass rises, the angular magnification reduces slightly because the subtended angle at the eye is imperceptibly less than the lenses.

Image distance does not have any impact on angular magnification.

c) Magnifying power of a simple microscope is inversely proportional to the focal length of the lens. What then stops us from using a convex lens of smaller and smaller focal length and achieving greater and greater magnifying power?



Ans: The convex lens's focal length cannot be reduced by a more significant amount.

This is because making lenses having tiny focal lengths is not easy.

Spherical and chromatic aberrations are created by a convex lens having a petite focal length.

d) Why must both the objective and the eyepiece of a compound microscope have short focal lengths?

Ans: The angular magnification produced by the compound microscope's eyepiece is:

$$\left[\left(\frac{25}{f_e} \right) + 1 \right]$$

Where, f_e is the eyepiece's focal length.

It can be seen that if f_e is small, then angular magnification of the eyepiece will be great.

The angular magnification of the compound microscope's objective lens is given as $\frac{f_o}{u_o}$.

u_o: Object distance for the objective lens

f_o: Objective's focal length

The magnification is large when $u_o > f_o$.

In the case of a microscope, the object is placed close to the objective lens. Hence, the object distance is tiny.

Since u_o is small, f_o will be smaller. Therefore, f_e and f_o are both small for the given condition.

e) When viewing through a compound microscope, our eyes should be positioned not on the eyepiece but a short distance away from it for best



viewing. Why? How much should be that short distance between the eye and eyepiece?

Ans: We cannot collect much-refracted light when we put our eyes too close to the compound microscope's eyepiece.

As a result, the field view reduces substantially. Hence, the image's clarity gets blurred.

The best view of the eye for seeing through a compound microscope is at the eye-ring connected to the eyepiece. The exact location of the eye depends on the separation between the objective lens and the eyepiece.

21. An angular magnification (magnifying power) of 30X is desired using an objective of focal length 1.25 cm and an eyepiece of focal length 5 cm. How will you set up the compound microscope?

Ans: Given that,

Focal length of the objective lens, $f_0 = 1.25$ cm

Focal length of the eyepiece, $f_e = 5$ cm

Least distance of distinct vision, d = 25 cm

Angular magnification of the compound microscope = 30X

Total magnifying power of the compound microscope, m = 30

The eyepiece's angular magnification is given by:

$$m_e = 1 + \frac{d}{f_e}$$

$$\Rightarrow$$
 $m_e = 1 + \frac{25}{5}$

$$\Rightarrow$$
 m_e = 6

The objective lens angular magnification is given by:

$$m = m_0 m_e$$



$$\Rightarrow m_{o} = \frac{m}{m_{e}}$$

$$\Rightarrow$$
 m_o = $\frac{30}{6}$ = 5

We have,

$$m_o = \frac{v_o}{-u_o}$$

$$\Rightarrow 5 = \frac{v_o}{-u_o}$$

$$\Rightarrow v_o = -5u_o \dots (1)$$

Using lens formula,

$$\frac{1}{f_0} = \frac{1}{v_0} - \frac{1}{u_0}$$

$$\Rightarrow \frac{1}{1.25} = \frac{1}{-5u_0} - \frac{1}{u_0}$$

$$\Rightarrow$$
 $u_o = -1.5$ cm

And,
$$v_o = -5u_o = -5 \times -1.5 = 7.5$$
cm

The object should be placed 1.5cm away from the objective lens to get the desired magnification.

Using lens formula,

$$\frac{1}{f_e} = \frac{1}{v_e} - \frac{1}{u_e}$$

Where, $v_e = -d = -25$ cm

$$\Rightarrow \frac{1}{5} = \frac{1}{-25} - \frac{1}{u_e}$$

$$\Rightarrow$$
 $u_e = -4.17$ cm

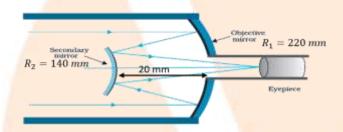


Separation between the eyepiece and the objective lens $= |\mathbf{u}_e| + |\mathbf{v}_o|$

$$|u_e| + |v_o| = 4.17 + 7.5 = 11.67$$
cm

Therefore, the separation between the eyepiece and the objective lens should be 11.67cm.

22. A Cassegrain telescope uses two mirrors as shown in figure. Such a telescope is built with the mirrors 20 mm apart. If the radius of curvature of the large mirror is 220 mm and these all mirror is 140mm, where will the final image of an object at infinity be?



Ans: A Cassegrain telescope contains two mirrors, one is objective mirror and second one is secondary mirror. We need to find the distance of final image from secondary mirror.

Given: distance between the objective mirror and the secondary mirror, d = 20mm

Radius of curvature of the objective mirror, $R_1 = 220 \text{ mm}$

Hence, objective mirror's focal length,
$$f_1 = \frac{R_1}{2} = 110 \text{mm}$$

Secondary mirror's radius of curvature, $R_2 = 140 \text{ mm}$

Secondary mirror's focal length,
$$f_2 = \frac{R_2}{2} = 70 \text{mm}$$

The image of an object set at infinity, made by the objective mirror, will serve as a virtual object for the secondary mirror.

Hence, the secondary mirror's virtual object distance, $u = f_1 - d$

$$\Rightarrow$$
 u = 110 – 20 = 90mm



Using mirror formula,

$$\frac{1}{u} + \frac{1}{v} = \frac{1}{f_2}$$

$$\Rightarrow \frac{1}{v} = \frac{1}{f_2} - \frac{1}{u}$$

Now, we put given values,

$$\Rightarrow \frac{1}{v} = \frac{1}{70} - \frac{1}{90}$$

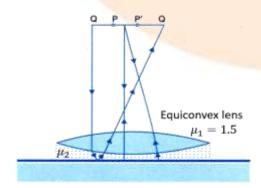
$$\Rightarrow \frac{1}{v} = \frac{9-7}{630}$$

$$\Rightarrow \frac{1}{v} = \frac{2}{630}$$

$$\Rightarrow$$
 v = 315mm

Clearly, the final image will be made 315 mm away from the secondary mirror.

23. Figure shows an equiconvex lens (of refractive index 1.50) in contact with a liquid layer on top of a plane mirror. A small needle with its tip on the principal axis is moved along the axis until its inverted image is found at the position of the needle. The distance of the needle from the lens is measured to be 45.0 cm. The liquid is removed and the experiment is repeated. The new distance is measured to be 30.0 cm. What is the refractive index of the liquid?





Ans: An equiconvex lens is in touch with a liquid layer on a plane mirror top. A small needle placed on the principal axis is moved along the axis until its inverted image will be at the position of the needle.

Convex lens' focal length, $f_1 = 30$ cm

The liquid will behave as a mirror.

Liquid's focal length = f_2

System's focal length, f = 45 cm

The equivalent focal length is given as:

$$\frac{1}{f} = \frac{1}{f_1} + \frac{1}{f_2}$$

$$\Rightarrow \frac{1}{f_2} = \frac{1}{f} - \frac{1}{f_1}$$

$$\Rightarrow \frac{1}{f_2} = \frac{1}{45} - \frac{1}{30} = -\frac{1}{90}$$

$$\therefore f_2 = -90cm$$

Let the lens's refractive index be μ_1 and curvature radius of one surface be R.

Hence, the curvature radius of the other surface is -R.

We use,

$$\frac{1}{f_1} = (\mu_1 - 1) \left[\frac{1}{R} - \frac{1}{-R} \right]$$

$$\Rightarrow \frac{1}{30} = (1.5 - 1) \left\lceil \frac{2}{R} \right\rceil$$

$$\therefore R = 30cm$$

Let μ_2 be the liquid's refractive index.

Liquid's curvature radius on the side of the plane mirror $=\infty$.

Curvature radius of the liquid on the side of the lens, R = -30 cm.



We use,

$$\frac{1}{f_2} = (\mu_2 - 1) \left[\frac{1}{R} - \frac{1}{\infty} \right]$$

$$\Rightarrow \frac{-1}{90} = (\mu_2 - 1) \left[\frac{1}{-30} - 0 \right]$$

$$\Rightarrow (\mu_2 - 1) = \frac{1}{3}$$

$$\Rightarrow \mu_2 = 1.33$$

Clearly, the liquid's refractive index is 1.33.