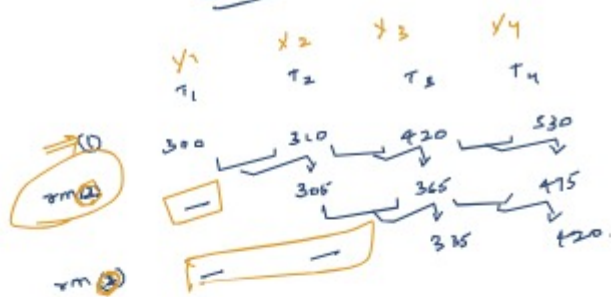


Time series = signal + noise  
trend or error/noise

① Remove trend

$$y(t) = y(t) - y(t-1)$$

moving average / rolling mean



$\frac{300 + 310}{2}$   
month → 30 days  
year → 12 months  
week → 7 days

AR model → autoregressive model

MA model → moving average model

ARMA model → autoregressive moving avg model

ARIMA model → autoregressive integrated moving average

AR model

$$y_t = \beta_0 + \beta_1 y_{t-1} + \beta_2 y_{t-2} + \dots + \beta_p y_{t-p} + \epsilon_t$$

constant past value error

MA model

$$y_t = \theta_0 + \theta_1 \epsilon_{t-1} + \dots + \theta_q \epsilon_{t-q}$$

constant error

ARMA

$$y_t = \beta_0 + \beta_1 y_{t-1} + \dots + \beta_p y_{t-p} + \epsilon_t + \theta_1 \epsilon_{t-1} + \dots + \theta_q \epsilon_{t-q}$$

ARMA (order, order = (0,1))

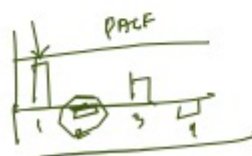
$$\frac{AR}{0} \frac{MA}{1}$$

ARIMA  
p d q { 1 0 1 = ARMA  
1 1 0 = AR1

ACF → MA  
PACF → AR



MA = 1/2



AR = 1