

Chapter 1

Boolean Logic

These slides support chapter 1 of the book

The Elements of Computing Systems

By Noam Nisan and Shimon Schocken

MIT Press

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Happy teaching!

Noam Nisam / Shimon Schocken

Chapter 1: Boolean logic



Boolean logic

- Boolean function synthesis
- Hardware description language
- Hardware simulation
- Multi-bit buses
- Project 1 overview

Boolean Values





F

Τ

N

Y

0

1

Boolean Operations

x And y

 $x \wedge x$

х	у	And
0	0	0
0	1	0
1	0	0
1	1	1

Boolean Operations

x And y

 $x \wedge x$

x Or *y*

 $x \vee y$

x	у	And
0	0	0
0	1	0
1	0	0
1	1	1

X	y	Or
0	0	0
0	1	1
1	0	1
1	1	1

Boolean Operations

x And y

 $x \wedge x$

х	у	And
0	0	0
0	1	0
1	0	0
1	1	1

x Or y

 $x \vee y$

х	у	Or
0	0	0
0	1	1
1	0	1
1	1	1

Not(x)

 $\neg x$

х	Not
0	1
1	0

Boolean Expressions

Not(0 Or (1 And 1)) =

Not(0 Or 1) =

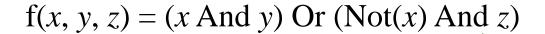
Not(1) =

0

f(x, y, z) = (x And y) Or (Not(x) And z)

f(x, y, z) = (x And y) Or (Not(x) And z)

X	у	Z	f
0	0	0	
0	0	1	
0	1	0	
0	1	1	
1	0	0	
1	0	1	
1	1	0	
1	1	1	

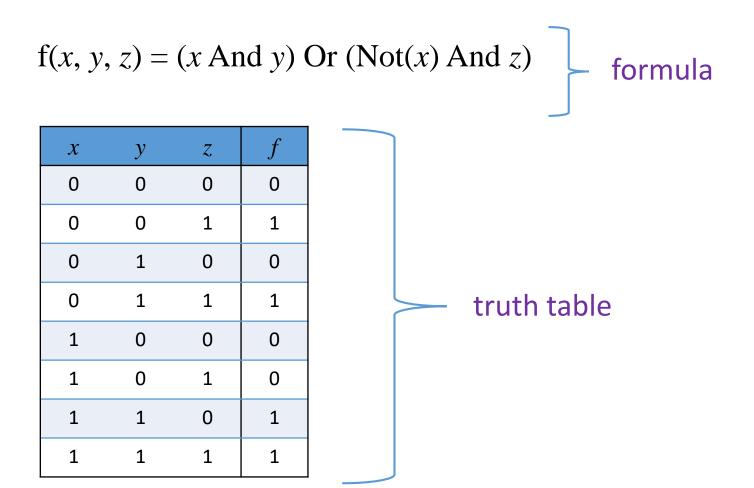


			•
X	y	Z	f
0	0	0	
0	0	1	1
0	1	0	
0	1	1	
1	0	0	
1	0	1	
1	1	0	
1	1	1	

(0 And 0) Or (Not(0) And 1) =
0 Or (1 And 1) =
0 Or 1 = 1

f(x, y, z) = (x And y) Or (Not(x) And z)

X	у	z	f
0	0	0	0
0	0	1	1
0	1	0	0
0	1	1	1
1	0	0	0
1	0	1	0
1	1	0	1
1	1	1	1



Boolean Identities

- (x And y) = (y And x)• (x Or y) = (y Or x) commutative laws
- $(x \operatorname{And} (y \operatorname{And} z)) = ((x \operatorname{And} y) \operatorname{And} z)$ $(x \operatorname{Or} (y \operatorname{Or} z)) = ((x \operatorname{Or} y) \operatorname{Or} z)$ associative laws

- (x And (y Or z)) = (x And y) Or (x And z)• (x Or (y And z)) = (x Or y) And (x Or z) distributive laws
- Not(x And y) = Not(x) Or Not(y)
 Not(x Or y) = Not(x) And Not(y)

 De Morgan laws

Not(Not(x) And Not(x Or y)) =

Not(Not(x) And Not(x Or y)) =

De Morgan law

Not(Not(x) And (Not(x) And Not(y))) =

Not(Not(x) And Not(x Or y)) =

Not(Not(x) And (Not(x) And Not(y))) =

associative law

Not((Not(x) And Not(x)) And Not(y)) =

Not(Not(x) And Not(x Or y)) =

Not(Not(x) And (Not(x) And Not(y))) =

Not((Not(x) And Not(x)) And Not(y)) = -

idempotence

Not(Not(x) And Not(y)) =

Not(Not(x) And Not(x Or y)) =

Not(Not(x) And (Not(x) And Not(y))) =

Not((Not(x) And Not(x)) And Not(y)) =

Not(Not(x) And Not(y)) =

De Morgan law

Not(Not(x)) Or Not(Not(y)) =

Not(Not(x) And Not(x Or y)) =

Not(Not(x) And (Not(x) And Not(y))) =

Not((Not(x) And Not(x)) And Not(y)) =

Not(Not(x) And Not(y)) =

Not(Not(x)) Or Not(Not(y)) =

double negation

x Or y

Not(Not(x) And Not(x Or y)) =

Not(Not(x) And Not(x Or y)) =



х	у	Or
0	0	0
0	1	1
1	0	1
1	1	1

Not(Not(x) And Not(x Or y)) =



X	y	Or
0	0	0
0	1	1
1	0	1
1	1	1



x Or y

Chapter 1: Boolean logic

- ✓ Boolean logic
- Boolean function synthesis
 - Hardware description language
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 - Project 1 overview

Boolean expression → truth table

f(x, y, z) = (x And y) Or (Not(x) And z)



X	y	Z	f
0	0	0	0
0	0	1	1
0	1	0	0
0	1	1	1
1	0	0	0
1	0	1	0
1	1	0	1
1	1	1	1

Boolean expression ← truth table

f(x, y, z) = (x And y) Or (Not(x) And z)



X	у	z	f
0	0	0	0
0	0	1	1
0	1	0	0
0	1	1	1
1	0	0	0
1	0	1	0
1	1	0	1
1	1	1	1

у	z	f
0	0	1
0	1	0
1	0	1
1	1	0
0	0	1
0	1	0
1	0	0
1	1	0
	0 0 1 1 0 0	0 0 0 1 1 0 1 1 0 0 0 1 1 1 0 0

y	z	f
0	0	1 1
0	1	0 0
1	0	1 0
1	1	0 0
0	0	1 0
0	1	0 0
1	0	0 0
1	1	0 0
	0 0 1 1 0 0	0 0 0 1 1 0 1 1 0 0 0 1 1 1 0 0

(Not(x) And Not(y) And Not(z))

X	у	z	f
0	0	0	1 0
0	0	1	0 0
0	1	0	1 1
0	1	1	0 0
1	0	0	1 0
1	0	1	0 0
1	1	0	0 0
1	1	1	0 0

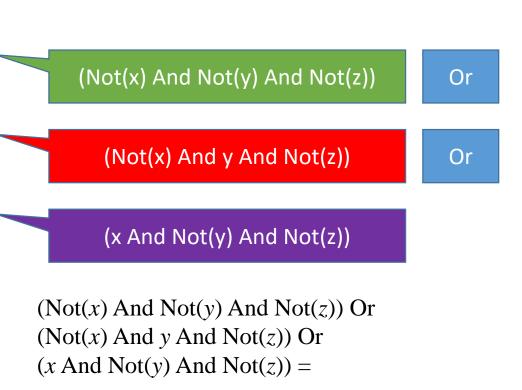
(Not(x) And y And Not(z))

X	у	z	f
0	0	0	1 0
0	0	1	0 0
0	1	0	1 1
0	1	1	0 0
1	0	0	1 1
1	0	1	0 0
1	1	0	0 0
1	1	1	0 0

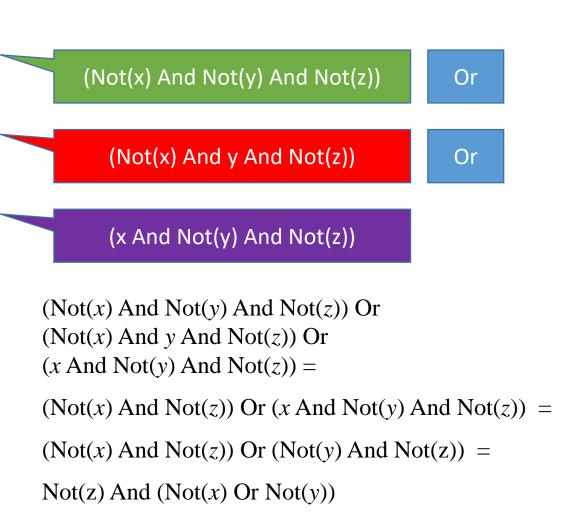
(x And Not(y) And Not(z))

X	у	z	f	
0	0	0	1 1	
0	0	1	0	(Not(x) And Not(y) And Not(z))
0	1	0	1 1	
0	1	1	0	(Not(x) And y And Not(z))
1	0	0	1 1	
1	0	1	0	(x And Not(y) And Not(z))
1	1	0	0	
1	1	1	0	

X	у	Z	f
0	0	0	1
0	0	1	0
0	1	0	1
0	1	1	0
1	0	0	1
1	0	1	0
1	1	0	0
1	1	1	0



X	у	Z	f
0	0	0	1
0	0	1	0
0	1	0	1
0	1	1	0
1	0	0	1
1	0	1	0
1	1	0	0
1	1	1	0



x	у	Nand
0	0	1
0	1	1
1	0	1
1	1	0

$$(x \text{ Nand } y) = \text{Not}(x \text{ And } y)$$

Theorem

<u>Theorem:</u> Any Boolean function can be represented using an expression containing Nand operations only.

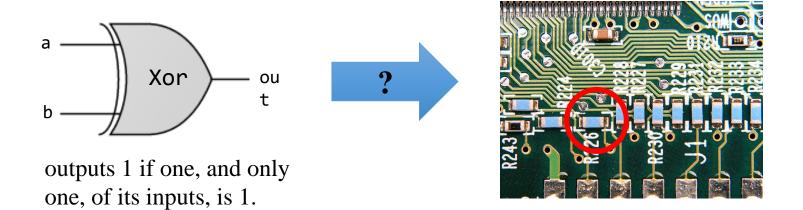
Proof:

- Not(x) = (x Nand x)
- (x And y) = Not(x Nand y)

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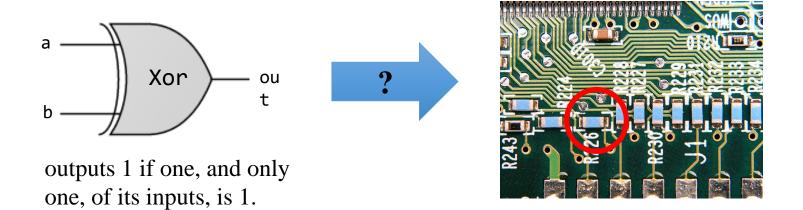
Building a logic gate



The Process:

- Design the gate architecture
- Specify the architecture in HDL
- Test the chip in a hardware simulator
- Optimize the design
- Realize the optimized design in silicon.

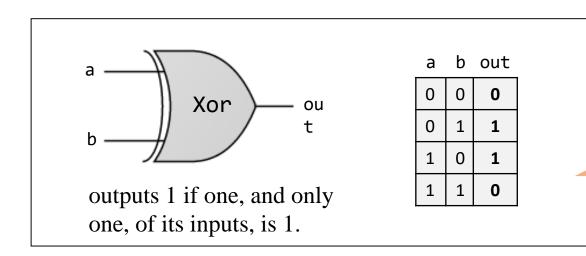
Building a logic gate



The Process:

- ✓ Design the gate architecture
- ✓ Specify the architecture in HDL
- ✓ Test the chip in a hardware simulator
- Optimize the design
- Realize the optimized design in silicon.

Design: from requirements to interface



Requirement:

Build a gate that delivers this functionality

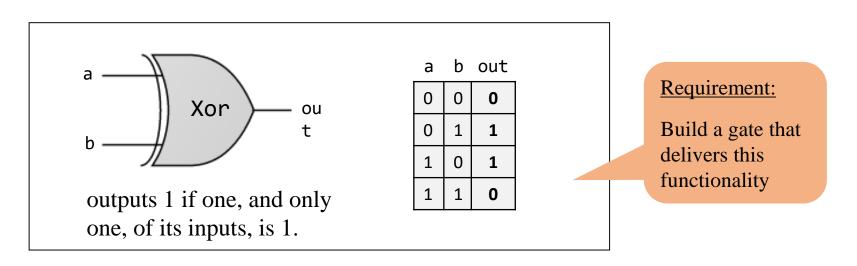
```
/** Xor gate: out = (a And Not(b)) Or (Not(a) And b)) */
CHIP Xor {
    IN a, b;
    OUT out;

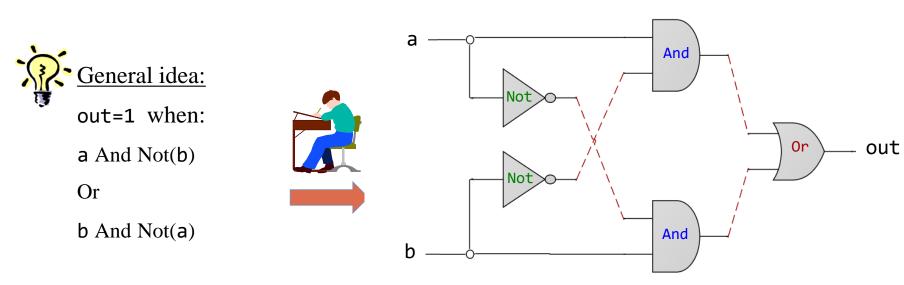
PARTS:
    // Implementation missing
}
```

Gate interface

Expressed as an HDL stub file

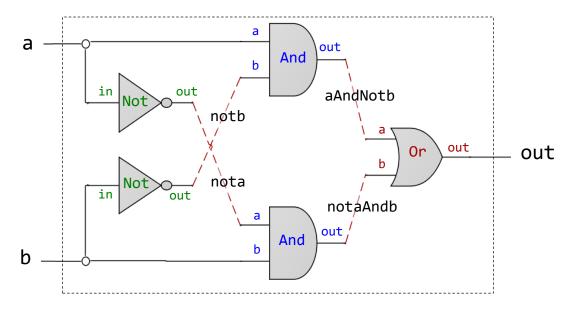
Design: from requirements to gate diagram





Design: from gate diagram to HDL

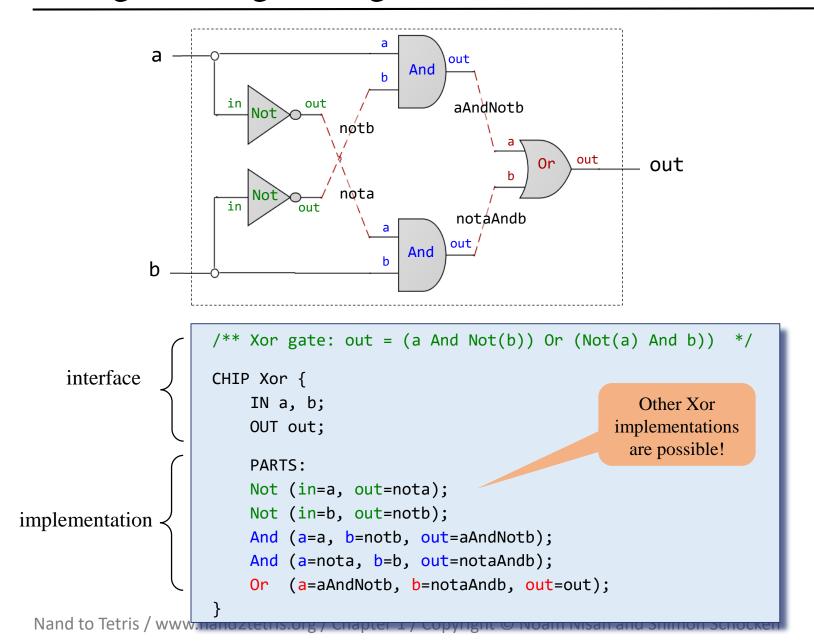
Nand to Tetris / www.manuztetris.org / chapter



```
/** Xor gate: out = (a And Not(b)) Or (Not(a) And b)) */
CHIP Xor {
    IN a, b;
    OUT out;

PARTS:
    // implementation missing
}
```

Design: from gate diagram to HDL



HDL: some comments

```
/** Xor gate: out = (a And Not(b)) Or (Not(a) And b)) */
CHIP Xor {
    IN a, b;
    OUT out;

PARTS:
    Not (in=a, out=nota);
    Not (in=b, out=notb);
    And (a=a, b=notb, out=aAndNotb);
    And (a=nota, b=b, out=notaAndb);
    Or (a=aAndNotb, b=notaAndb, out=out);
}
```

- HDL is a functional / declarative language
- The order of HDL statements is insignificant
- Before using a chip part, you must know its interface. For example:

```
Not(in= ,out=), And(a= ,b= ,out= ), Or(a= ,b= ,out= )
```

• Connection patterns like chipName(a=a,...) and chipName(...,out=out) are common

Hardware description languages

Common HDLs:

- VHDL
- Verilog
- Many more HDLs...

Our HDL

- Similar in spirit to other HDLs
- Minimal and simple
- Provides all you need for this course
- HDL Documentation:

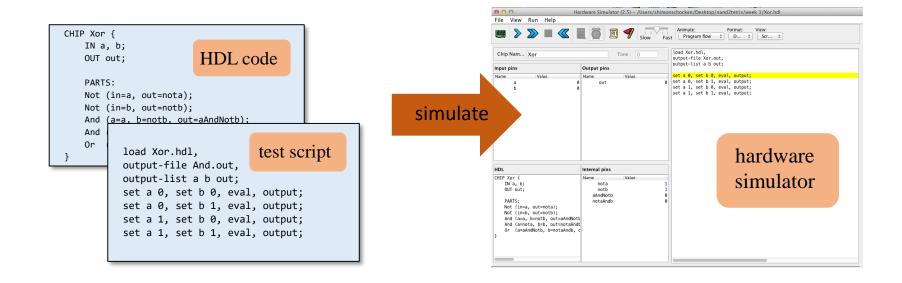


- □ Textbook / Appendix A
- www.nand2tetris.org / HDL Survival Guide

Chapter 1: Boolean logic

- ✓ Boolean logic
- **✓** Boolean function synthesis
- ✓ Hardware description language
- Hardware simulation
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Hardware simulation in a nutshell



Simulation options:

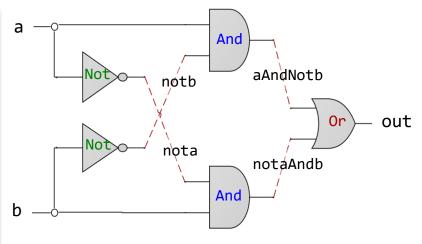
- Interactive
- Script-based
- With / without output and compare files

Interactive simulation (using Xor as an example)

Xor.hdl

```
CHIP Xor {
    IN a, b;
    OUT out;

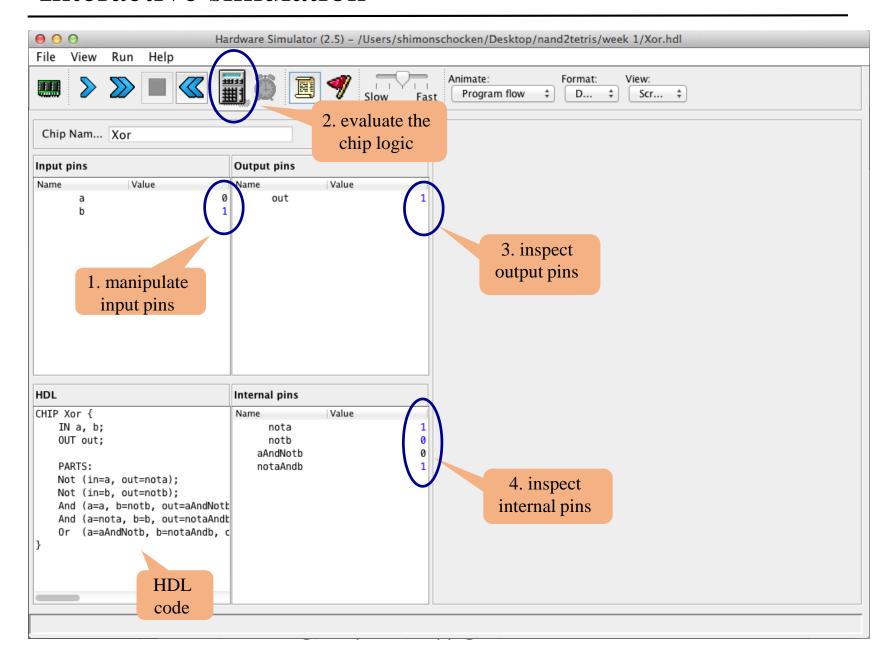
PARTS:
    Not (in=a, out=nota);
    Not (in=b, out=notb);
    And (a=a, b=notb, out=aAndNotb);
    And (a=nota, b=b, out=notaAndb);
    Or (a=aAndNotb, b=notaAndb, out=out);
}
```



Simulation process:

- Load the HDL file into the hardware simulator
- Enter values (0's and 1's) into the chip's input pins (e.g. a and b)
- Evaluate the chip's logic
- Inspect the resulting values of:
 - Output pins (e.g. out)
 - □ Internal pins (e.g. nota, notb, aAndNotb, notaAndb)

Interactive simulation



Script-based simulation

Xor.hdl

```
CHIP Xor {
    IN a, b;
    OUT out;

    PARTS:
    Not (in=a, out=nota);
    Not (in=b, out=notb);
    And (a=a, b=notb, out=aAndNotb);
    And (a=nota, b=b, out=notaAndb);
    Or (a=aAndNotb, b=notaAndb, out=out);
}
```

Xor.tst

```
load Xor.hdl;
set a 0, set b 0, eval;
set a 0, set b 1, eval;
set a 1, set b 0, eval;
set a 1, set b 1, eval;
```

<u>test script</u> = series of commands to the simulator

Benefits:

- "Automatic" testing
- Replicable testing

Script-based simulation, with an output file

Xor.hdl

```
CHIP Xor {
    IN a, b;
    OUT out;

    PARTS:
    Not (in=a, out=nota);
    Not (in=b, out=notb);
    And (a=a, b=notb, out=aAndNotb);
    And (a=nota, b=b, out=notaAndb);
    Or (a=aAndNotb, b=notaAndb, out=out);
}
```

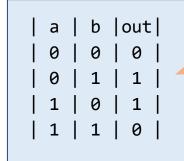
The logic of a typical test script

- Initialize:
 - Load an HDL file
 - Create an empty output file
 - List the names of the pins whose values will be written to the output file
- □ Repeat:
 - □ set eval output

Xor.tst

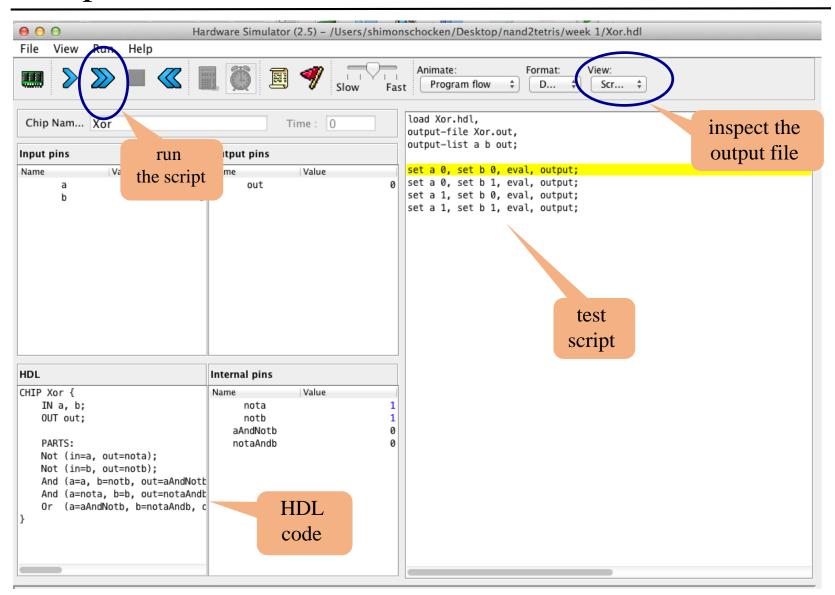
```
load Xor.hdl,
output-file Xor.out,
output-list a b out;
set a 0, set b 0, eval, output;
set a 0, set b 1, eval, output;
set a 1, set b 0, eval, output;
set a 1, set b 1, eval, output;
```

Xor.out



Output File, created by the test script as a side-effect of the simulation process

Script-based simulation



Hardware simulators

• There are many of them!

Our hardware simulator

- Minimal and simple
- Provides all you need for this course
- Hardware simulator documentation:



www.nand2tetris.org / Hardware Simulator Tutorial

Revisiting script-based simulation with output files

Xor.hdl

```
CHIP Xor {
    IN a, b;
    OUT out;

PARTS:
    Not (in=a, out=nota);
    Not (in=b, out=notb);
    And (a=a, b=notb, out=aAndNotb);
    And (a=nota, b=b, out=notaAndb);
    Or (a=aAndNotb, b=notaAndb, out=out);
}
```

Xor.tst

```
load Xor.hdl,

output-file Xor.out,

output-list a b out;

set a 0, set b 0, eval, output;

set a 0, set b 1, eval, output;

set a 1, set b 0, eval, output;

set a 1, set b 1, eval, output;
```

Xor.out

| a | b |out| | 0 | 0 | 0 | | 0 | 1 | 1 | | 1 | 0 | 1 | | 1 | 1 | 0 |

Output file, created by the test script as a side-effect of the simulation process

Script-based simulation, with compare files

Xor.hdl

```
CHIP Xor {
    IN a, b;
    OUT out;

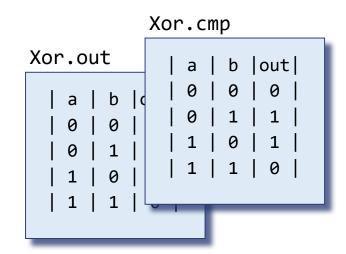
PARTS:
    Not (in=a, out=nota);
    Not (in=b, out=notb);
    And (a=a, b=notb, out=aAndNotb);
    And (a=nota, b=b, out=notaAndb);
    Or (a=aAndNotb, b=notaAndb, out=out);
}
```

Simulation-with-compare-file logic

- When each output command is executed, the outputted line is compared to the corresponding line in the compare file
- If the two lines are not the same, the simulator throws a comparison error.

Xor.tst

```
load Xor.hdl,
output-file Xor.out,
compare-to Xor.cmp,
output-list a b out;
set a 0, set b 0, eval, output;
set a 0, set b 1, eval, output;
set a 1, set b 0, eval, output;
set a 1, set b 1, eval, output;
```

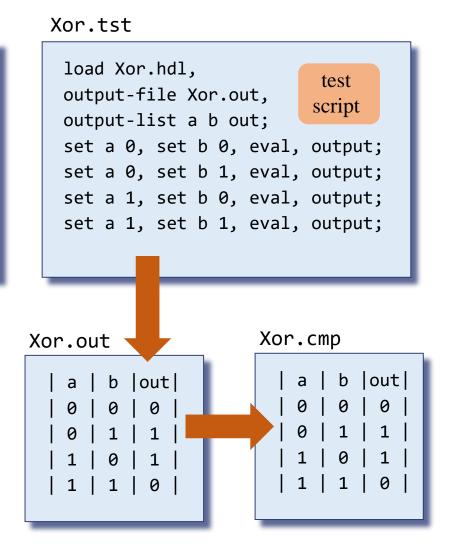


Behavioral simulation

Xor.hdl

Behavioral simulation:

- The chip logic (abstraction) can be implemented in some high-level language
- Enables high-level planning and testing of a hardware architecture before writing any HDL code.



Hardware construction projects

- The players (first approximation):
 - System architects
 - Developers
- The system architect decides which chips are needed
- For each chip, the architect creates
 - A chip API
 - A test script
 - A compare file
- Given these resources, the developers can build the chips.

The developer's view (of, say, a xor gate)

Xor.hdl

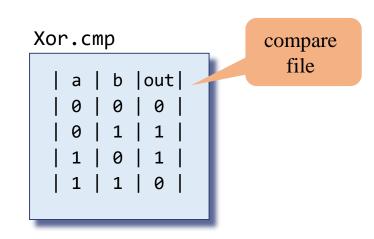
```
/** returns 1 if (a != b) */
CHIP Xor {
    IN a, b;
    OUT out;

PARTS:
    // Implementation missing
}
```

Xor.tst

```
load Xor.hdl,
output-file Xor.out,
compare-to Xor.cmp
output-list a b out;
set a 0, set b 0, eval, output;
set a 0, set b 1, eval, output;
set a 1, set b 0, eval, output;
set a 1, set b 1, eval, output;
```

- Taken together, the three files provide a convenient specification of:
 - □ The chip interface (.hdl)
 - □ What the chip is supposed to do (.cmp)
 - How to test the chip (.tst)
- The developer's task: implement the chip, using these resources.



Chapter 1: Boolean logic

- **✓** Boolean logic
- **✓** Boolean function synthesis
- ✓ Hardware description language
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Arrays of Bits

- Sometimes we wish to manipulate an array of bits as one group
- It's convenient to think about such a group of bits as a single entity, sometime termed "bus"
- HDLs usually provide notation and means for handling buses.

Example: adding 16-bit integers

```
/*
* Adds two 16-bit inputs.
                                                 16-bit
                                                 adder
CHIP Add16 {
  IN a[16], b[16];
  OUT out[16];
   PARTS:
                   /*
                    * Adds three 16-bit inputs.
                    */
                   CHIP Add3Way16 {
```

Example: adding 16-bit integers

```
/*
* Adds two 16-bit values.
                                                 16-bit
                                                 adder
CHIP Add16 {
  IN a[16], b[16];
  OUT out[16];
   PARTS:
                   /*
                    * Adds three 16-bit inputs.
                    */
                   CHIP Add3Way16 {
                      IN first[16], second[16], third[16];
                      OUT out[16];
                      PARTS:
                      Add16(a=first, b=second, out=temp);
                      Add16(a=temp, b=third, out=out);
```

```
* 4-way And: Ands 4 bits.
 */
CHIP And4Way {
```

```
* 4-way And: Ands 4 bits.
*/
CHIP And4Way {
  IN a[4];
  OUT out;
  PARTS:
  And(a=a[0], b=a[1], out=t01);
  And(a=t01, b=a[2], out=t012);
  And(a=t012, b=a[3], out=out);
```

```
* Bit-wise And of two 4-bit inputs
 */
CHIP And4 {
```

```
* Bit-wise And of two 4-bit inputs
*/
CHIP And4 {
  IN a[4], b[4];
  OUT out[4];
  PARTS:
  And(a=a[0], b=b[0], out=out[0]);
  And(a=a[1], b=b[1], out=out[1]);
  And(a=a[2], b=b[2], out=out[2]);
  And(a=a[3], b=b[3], out=out[3]);
```

Sub-buses

Buses can be composed from (and decomposed into) sub-buses

```
...
IN lsb[8], msb[8], ...
...
```

Sub-buses

Buses can be composed from (and decomposed into) sub-buses

```
...
IN lsb[8], msb[8], ...
...
Add16(a[0..7]=lsb, a[8..15]=msb, b=..., out=...);
Add16(..., out[0..3]=t1, out[4..15]=t2);
```

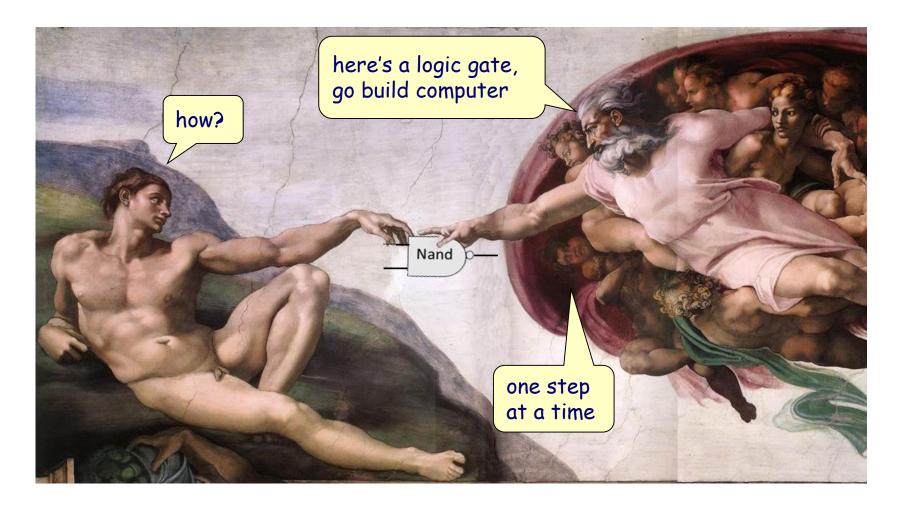
Some syntactic choices of our HDL

- buses are indexed right to left: if foo is a 16-bit bus, then foo[0] is the right-most bit, and foo[15] is the left-most bit
- overlaps of sub-buses are allowed in output buses of parts
- width of internal pin buses is deduced automatically
- The false and true constants may be used as buses of any width.

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Nand to Tetris course methodology

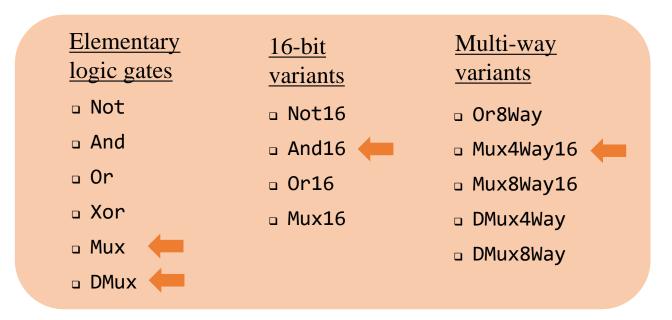


Project 1: the first step

Project 1

Given: Nand

Goal: Build the following gates:



Why these 15 particular gates?

- Commonly used gates
- Comprise all the elementary logic gates needed to build our computer.

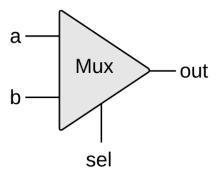
Project 1

Given: Nand

Goal: Build the following gates:

Elementary logic gates	<u>16-bit</u> <u>variants</u>	<u>Multi-way</u> <u>variants</u>
□ Not	□ Not16	□ Or8Way
□ And	□ And16	□ Mux4Way16
□ Or	or16	□ Mux8Way16
□ Xor	□ Mux16	□ DMux4Way
□ Mux		□ DMux8Way
□ DMux		

Multiplexor

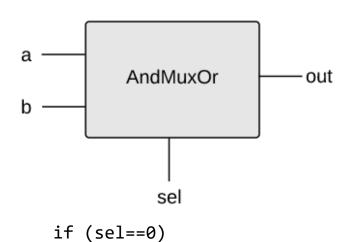


а	b	sel	out
0	0	0	0
0	1	0	0
1	0	0	1
1	1	0	1
0	0	1	0
0	1	1	1
1	0	1	0
1	1	1	1

	sel	out		
	0	а		
	1	b		
	abbreviated truth table			

- A 2-way multiplexor enables <u>selecting</u>, and outputting, one of two possible inputs
- Widely used in:
 - Digital design
 - Communications networks

Example: using mux logic to build a programmable gate



out = (a And b)

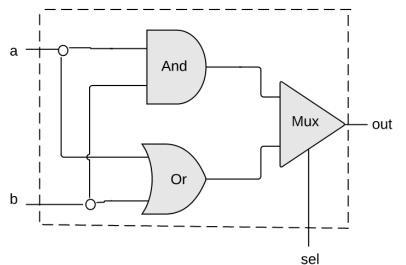
out = (a Or b)

else

a	b	sel	out	_
0	0	0	0	
0	1	0	0	
1	0	0	0	
1	1	0	1	ر ا
0	0	1	0	5
0	1	1	1	
1	0	1	1	
1	1	1	1	ر[

When sel==0 the gate acts like an And gate

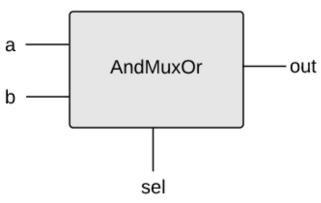
When sel==1
the gate acts like
an Or gate



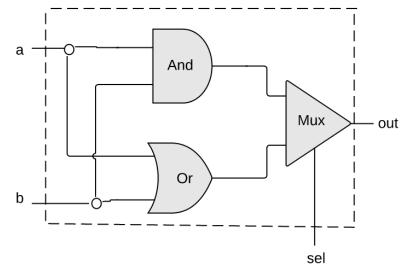
Mux.hdl

```
CHIP AndMuxOr {
   IN a, b, sel;
   OUT out;
```

Example: using mux logic to build a programmable gate



	361				
if	(se]	L==	: 0)		
	out	=	(a	And	b)
219	se				
	out	=	(a	Or b)



a	b	sel	out	_
0	0	0	0	
0	1	0	0	
1	0	0	0	
1	1	0	1	ر ا
0	0	1	0	[
0	1	1	1	
1	0	1	1	
1	1	1	1	ر[

When sel==0 the gate acts like an And gate

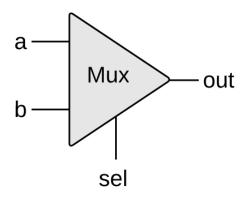
When sel==1
the gate acts like
an Or gate

Mux.hdl

```
CHIP AndMuxOr {
    IN a, b, sel;
    OUT out;

PARTS:
    And (a=a, b=b, out=andOut);
    Or (a=a, b=b, out=orOut);
    Mux (a=andOut, b=orOut, sel=sel, out=out);
}
```

Multiplexor implementation



if	(sel==0)
	out=a
els	se
	out=b

sel	out
0	а
1	b

Mux.hdl

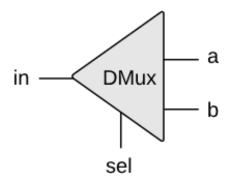
```
CHIP Mux {
    IN a, b, sel;
    OUT out;

PARTS:
    // Put your code here:
}
```

<u>Implementation tip:</u>

Can be implemented with And, Or, and Not gates

Demultiplexor



in	sel	a	b
0	0	0	0
0	1	0	0
1	0	1	0
1	1	0	1

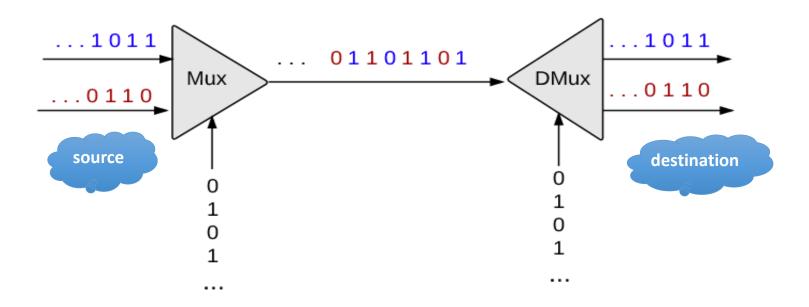
- Acts like the "inverse" of a multiplexor
- Distributes the single input value into one of two possible destinations

DMux.hdl

```
CHIP DMux {
    IN in, sel;
    OUT a, b;

PARTS:
    // Put your code here:
}
```

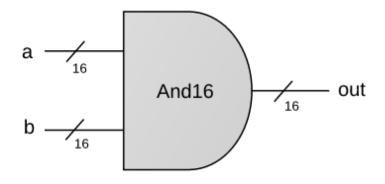
Example: Multiplexing / demultiplexing in communications networks



- Each sel bit is connected to an oscillator that produces a repetitive train of alternating 0 and 1 signals
- Enables transmitting multiple messages on a single, shared communications line
- A common use of multiplexing / demultiplexing logic
- Unrelated to this course.

Project 1

Elementary Multi-way <u>16-bit</u> logic gates variants variants Not □ Not16 □ Or8Way And □ And16 ← Mux4Way16 o Or □ 0r16 Mux8Way16 □ Xor Mux16 DMux4Way Mux DMux8Way DMux



```
a = 1 0 1 0 1 0 1 1 0 1 0 1 1 1 0 0
b = 0 0 1 0 1 1 0 1 0 0 1 0 1 0 1 0

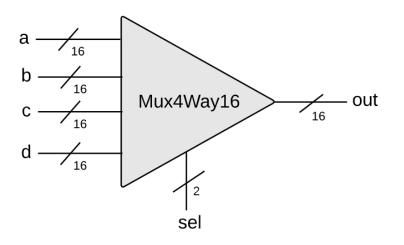
out = 0 0 1 0 1 0 0 1 0 0 0 0 0 0 0
```

• A straightforward 16-bit extension of the elementary And gate (See previous slides on working with multi-bit buses)

Project 1

Elementary logic gates	<u>16-bit</u> variants	<u>Multi-way</u> <u>variants</u>
□ Not	□ Not16	□ Or8Way
□ And	□ And16	□ Mux4Way16 🛑
o Or	o 0r16	□ Mux8Way16
□ Xor	□ Mux16	□ DMux4Way
□ Mux		□ DMux8Way
□ DMux		

16-bit, 4-way multiplexor



sel[1	sel[0]	out
0	0	а
0	1	b
1	0	С
1	1	d

Mux4Way16.hdl

```
CHIP Mux4Way16 {
    IN a[16], b[16], c[16], d[16],
        sel[2];
    OUT out[16];

    PARTS:
    // Put your code here:
}
```

<u>Implementation tip:</u>

Can be built from several Mux16 gates

Project 1

Given: Nand

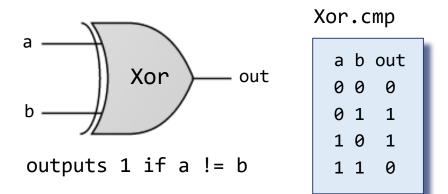
Goal: Build the following gates:

Elementary logic gates	<u>16-bit</u> variants	<u>Multi-way</u> <u>variants</u>
□ Not	 Not16	□ Or8Way
□ And	□ And16	□ Mux4Way16
or Or	□ 0r16	□ Mux8Way16
□ Xor	□ Mux16	□ DMux4Way
□ Mux		□ DMux8Way
□ DMux		



So how to actually <u>build</u> these gates?

Chip building materials (using xor as an example)



The contract:

When running your Xor.hdl on the supplied Xor.tst, your Xor.out should be the same as the supplied Xor.cmp

Xor.hdl

```
CHIP Xor {
    IN a, b;
    OUT out;

PARTS:
    // Put your code here.
}
```

Xor.tst

```
load Xor.hdl,
output-file Xor.out,
compare-to Xor.cmp,
output-list a b out;
set a 0, set b 0, eval, output;
set a 0, set b 1, eval, output;
set a 1, set b 0, eval, output;
set a 1, set b 1, eval, output;
```

Project 1 Resources



Home

Prerequisites

Syllabus

Course

Book

Software

Terms Papers

Talks

Cool Stuff

About Team

Q&A

Project 1: Elementary Logic Gates

Background

A typical computer architecture is based on a set of elementary logic gates like And, Or, Mux, etc., as well as their bit-wise versions And16, Or16, Mux16, etc. (assuming a 16-bit machine). This project engages you in the construction of a typical set of basic logic gates. These gates form the elementary building blocks from which more complex chips will be later constructed.

Objective

Build all the logic gates described in Chapter 1 (see list below), yielding a basic chip-set. The only building blocks that you can use in this project are primitive Nand gates and the composite gates that you will gradually build on top of them.

Chips

Chip (HDL)	Description	Test Script	Compare File
Nand	Nand gate (primitive)		
Not	Not gate	Not.tst	Not.cmp
And	And gate	And.tst	And.cmp
Or	Or gate	Or.tst	Or.cmp
Xor	Xor gate	Xor.tst	Xor.cmp
Mux	Mux gate	Mux.tst	Mux.cmp
DMux	DMux gate	DMux.tst	DMux.cmp
Not16	16-bit Not	Not16.tst	Not16.cmp
And16	16-bit And	And16.tst	And16.cmp
Or16	16-bit Or	Or16.tst	Or16.cmp
Mux16	16-bit multiplexor	Mux16.tst	Mux16.cmp

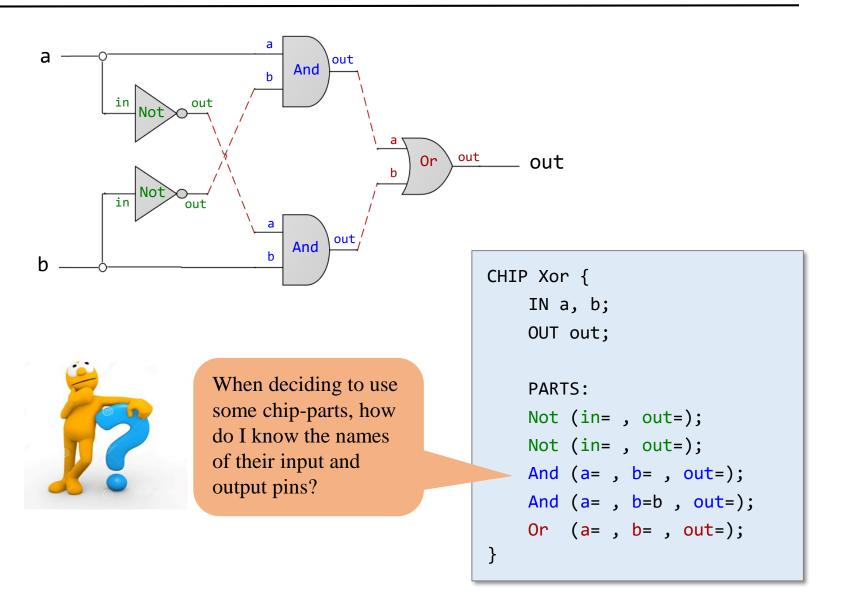
All the necessary project 1 files are available in:
nand2tetris/projects/01

More resources

- Text editor (for writing your HDL files)
- HDL Survival Guide
- Hardware Simulator Tutorial
- nand2tetris Q&A forum

All available in: www.nand2tetris.org

Hack chipset API



Hack chipset API

```
Add16 (a= ,b= ,out= );
ALU (x= ,y= ,zx= ,nx= ,zy= ,ny= ,f= ,no= ,out= ,zr= ,ng= );
And16 (a= ,b= ,out= );
                                        Mux8Way (a= ,b= ,c= ,d= ,e= ,f= ,g= ,h= ,sel= ,out= );
And (a= ,b= ,out= );
                                        Mux (a= ,b= ,sel= ,out= );
Aregister (in= ,load= ,out= );
                                        Nand (a= ,b= ,out= );
Bit (in= ,load= ,out= );
                                        Not16 (in= ,out= );
CPU (inM= ,instruction= ,reset= ,outN
                                        Not (in= ,out= );
DFF (in= ,out= );
                                        Or16 (a= ,b= ,out= );
DMux4Way (in= ,sel= ,a= ,b= ,c= ,d=
                                        Or8Way (in= ,out= );
DMux8Way (in= ,sel= ,a= ,b= ,c= ,d=
                                        Or (a= ,b= ,out= );
Dmux (in= ,sel= ,a= ,b= );
                                        PC (in= ,load= ,inc= ,reset= ,out= );
Dregister (in= ,load= ,out= );
                                        PCLoadLogic (cinstr= ,j1= ,j2= ,j3= ,load= ,inc= );
FullAdder (a= ,b= ,c= ,sum= ,carry=
                                        RAM16K (in= ,load= ,address= ,out= );
HalfAdder (a= ,b= ,sum= , carry= );
                                        RAM4K (in= ,load= ,address= ,out= );
Inc16 (in= ,out= );
                                        RAM512 (in= ,load= ,address= ,out= );
Keyboard (out= );
                                        RAM64 (in= ,load= ,address= ,out= );
Memory (in= ,load= ,address= ,out= );
                                        RAM8 (in= ,load= ,address= ,out= );
Mux16 (a= ,b= ,sel= ,out= );
                                        Register (in= ,load= ,out= );
Mux4Way16 (a= ,b= ,c= ,d= ,sel= ,out=
                                        ROM32K (address= ,out= );
Mux8Way16 (a= ,b= ,c= ,d= ,e= ,f= ,g=
                                        Screen (in= ,load= ,address= ,out= );
                                        Xor (a= ,b= ,out= );
```



(see HDL Survival Guide @ www.nand2tetris.org)

Built-in chips

```
CHIP Foo {
    IN ...;
    OUT ...;

PARTS:
    ...
    Mux16(...)
}
```

Q: What happens if there is no Mux16.hdl file in the current directory?

Built-in chips

```
CHIP Foo {
    IN ...;
    OUT ...;

PARTS:
    ...
    Mux16(...)
    ...
}
```

- Q: What happens if there is no Mux16.hdl file in the current directory?
- A: The simulator invokes, and evaluates, the built-in version of Mux16 (if such exists).

- The supplied simulator software features built-in chip implementations of all the chips in the Hack chip set
- If you don't implement some chips from the Hack chipset, you can still use them as chip-parts of other chips:
 - □ Just rename their given stub files to, say, Mux16.hdl1
 - □ This will cause the simulator to use the built-in chip implementation.

Best practice advice

- Try to implement the chips in the given order
- If you don't implement some chips, you can still use them as chip-parts in other chips (the built-in implementations will kick in)
- You can invent new, "helper chips"; however, this is not required: you can build any chip using previously-built chips only
- Strive to use as few chip-parts as possible.

Chapter 1: Boolean logic

- **✓** Boolean logic
- ✓ Boolean function synthesis
- ✓ Hardware description language
- ✓ Hardware simulation
- ✓ Multi-bit buses
- ✓ Project 1 overview



Chapter 1

Boolean Logic

These slides support chapter 1 of the book

The Elements of Computing Systems

By Noam Nisan and Shimon Schocken

MIT Press