

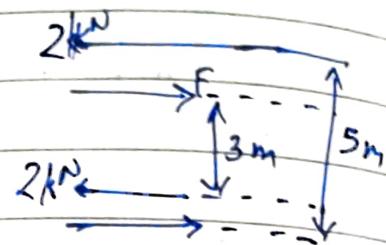
21st October, 2022

Couple

2/63. $M = 2(5) = 10$

~~$10 = F(3)$~~

$F = 3 \cdot 3 \text{ kN}$



$$\sum M = 0$$

$$2(5) - F(3) = 0$$

$$F = 3 \cdot 3$$

2/64. ~~Skew~~

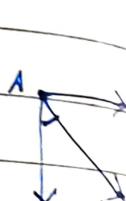
$$M = 8 (\sin 30)(0.32) - 8 \cos 30 (3)$$

$$= +1.28 - 20.78$$

$$= -22.064 \text{ kNm}$$

$$= -19.5 \text{ kNm}$$

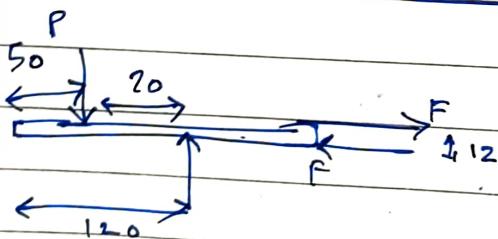
$$= 19.5 \text{ Nm c.w}$$



2/65. $\sum M = 0$

$$300(12) - P(50) - P(120) = 0$$

$$3600 = 120P$$



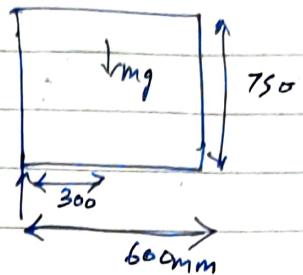
$$300(12) - P(70) = 0$$

$$\frac{300 \times 12}{70} = P$$

$$P = 51.42 \text{ kN}$$

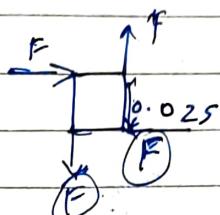
$$2/66. M = \cancel{5} (0.3)(9.81) \\ \text{couple} = 1.5 \text{ Nm}$$

$\text{mg } (0.3)$



$$2/67. \cancel{M = 250(0.7)} \\ = 175.0$$

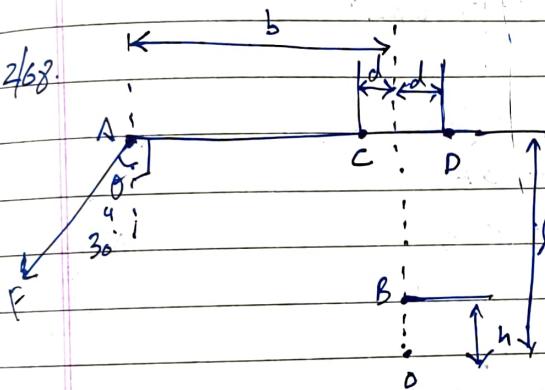
$$\cancel{F \left(\frac{0.350 + 0.350}{2} \right) = 175} \\ \cancel{F (0.35) = 175} \\ F = 500 \text{ N}$$



$$2F(0.025) = 175$$

$$F = 3500$$

2/68.



$$F = 425 \\ \theta = 30^\circ \\ b = 1.9 \\ d = 0.2 \\ h = 0.8 \\ l = 2.75$$

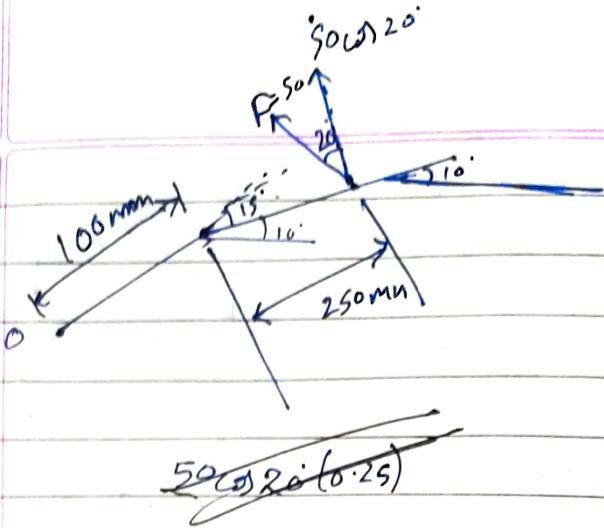
Force couple at B: $F = 425 \text{ N}$ @ 120° below Horizontal

$$\begin{aligned} M_B &= F \cos \theta (b) + F \sin \theta (l - b) \\ &= 425 \cos 30 (1.9) + 425 \sin 30 (2.75 - 0.8) \\ &= 699.31 + 1862.5 \\ &= 829.935 \text{ Nm CCW} \quad = 1114 \text{ Nm CCW} \end{aligned}$$

Now replacing F by two forces such that the resultant is in direction of F one at C & one at D

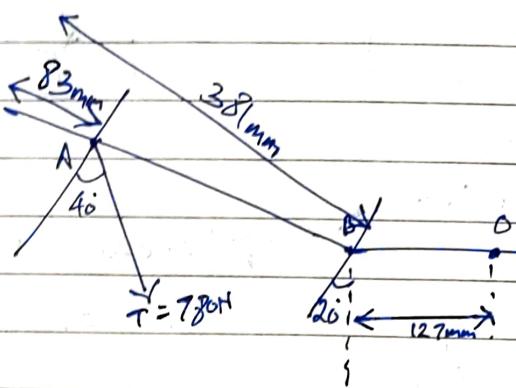
$$\begin{aligned} F_C &> F_D \\ F_C - F_D &= 425 \\ M_A \Rightarrow F_C \cos \theta (b - d) &= F_D \cos \theta (b + d) \\ F_C \cos 30 (1.7) &= F_D \cos 30 (2.1) \\ F_C &= 1.235 F_D \\ F_D &= 1808 \text{ N} @ 60^\circ \text{ above Horizontal} \quad | \quad F_C = 2230 \text{ N} @ 60^\circ \text{ below Horizontal} \end{aligned}$$

2/69.



$$250 \cos 20^\circ (0.25)$$

2/70.

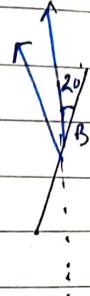


$$T = 780 \cos 40^\circ (-1) + 780 \sin 40^\circ (1)$$

$$M_B = \cancel{780 \cos 40^\circ (3.81 - 2.3)}$$

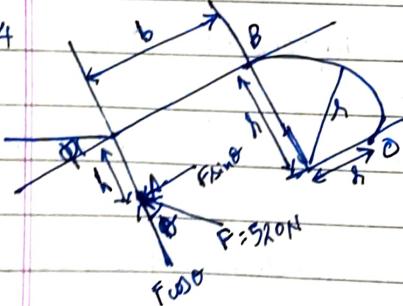
$$= 780 \cos 40^\circ (0.381 - 0.083)$$

$$= 178.05 \text{ kNm CCW}$$

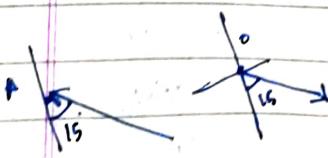


$$M_D = M_B + \cancel{28T \cos 20^\circ (0.127)} \\ = 271 \text{ kNm}$$

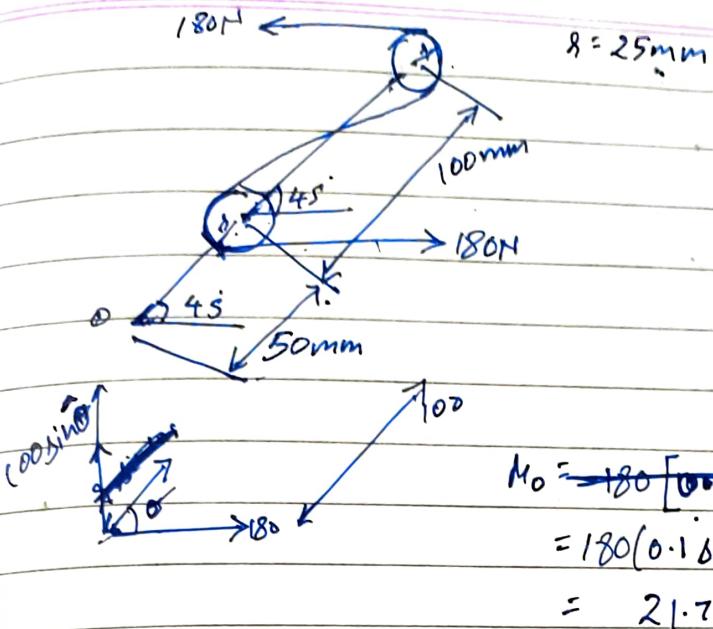
2/74



$$M_D = -F \cos \theta (b + h) + F \sin \theta (h - h) \\ = -520 \cos 15^\circ (0.45 + 0.325) \\ + 520 \sin 15^\circ (0.325 - 0.25) \\ = -389.26 + 14.80 \\ = -374.45 \text{ Nm} \\ = 374.45 \text{ Nm CW}$$



2/25.

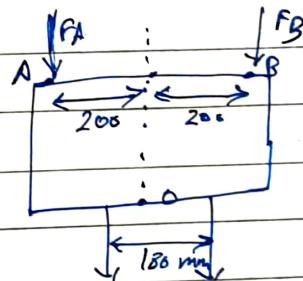


2/26.

$$\begin{aligned} M_o &= +6.3(10^3)(90)(10^{-3}) - 4.1(10^3)(90)(10^{-3}) \\ &= 567.0 - 369 \\ &= 198 \text{ Nm ccw} \end{aligned}$$

~~$$P(400)10^3 = 198$$

$$F = \frac{198}{0.4} = 472.5 \text{ N}$$~~



Replacing $6.3 \text{ kN} 4.1 \text{ kN}$ with F_A & F_B

$$\begin{aligned} \Rightarrow F_A + F_B &= 6.3 + 4.1 \text{ kN} \\ F_A + F_B &= 10.4 \text{ kN} = 10400 \text{ N} \end{aligned}$$

$$6.3 \text{ kN} \quad 4.1 \text{ kN}$$

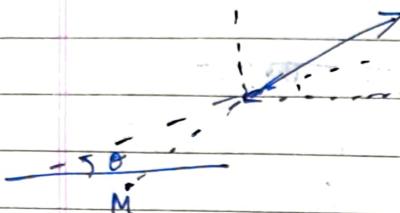
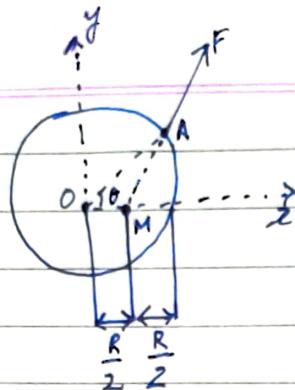
$$\begin{aligned} \text{Eq. } F_A(0.2) - F_B(0.2) &= 198 \\ F_A - F_B &= 990 \text{ N} \end{aligned}$$

$$2F_A = 11390$$

$$F_A = 5695 \text{ N}$$

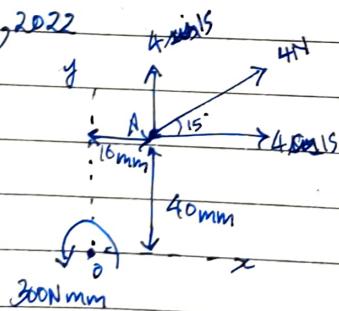
$$F_B = 4705 \text{ N} \quad //$$

2/18



1st November, 2022

2/26.

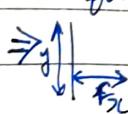


$$M_b = 300 - 4 \cos 15 + 4 \sin 15 (10)$$

$$= 300 - 154.54 + 10 \cdot 3.5$$

$$= 155.81 \text{ N mm}$$

to find y-intercept of line of action of force
for single equivalent force



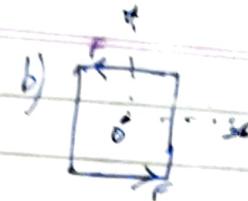
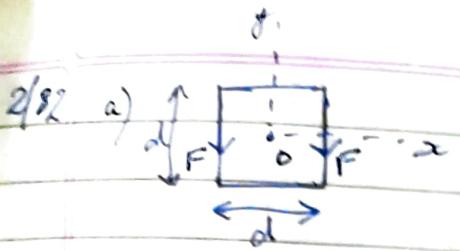
$$F_x(y) = M_b$$

$$\Rightarrow 4 \cos 15(y) = 155.81$$

$$3.86 y = 155.81$$

$$y = 40.36$$

$$y = -40.36$$



$$M_o = \frac{Fd}{2} - \frac{Fd}{2}$$

$$R = 0$$

$$M_o = 0$$

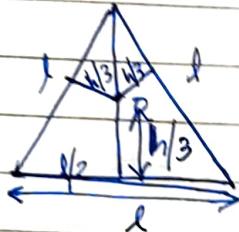
$$Fq = R = -2F\hat{j}$$

$$M_o = F(d)\hat{k}$$

$$R = -F\hat{i} + F\hat{j}$$

$$M_o = -F\left(\frac{d}{2}\right) + F\frac{d}{2} = 0$$

2/83.

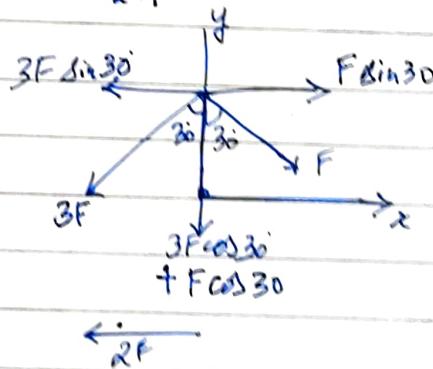
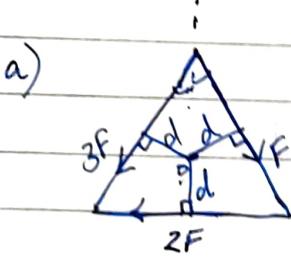


$$h = \sqrt{\frac{l^2 + l^2}{4}} = \frac{l\sqrt{3}}{2} = h \Rightarrow \frac{h}{3} = \frac{l\sqrt{3}}{6}$$

$$\text{let } \frac{h}{3} = d$$

equilateral Δ centroid divides

2:1



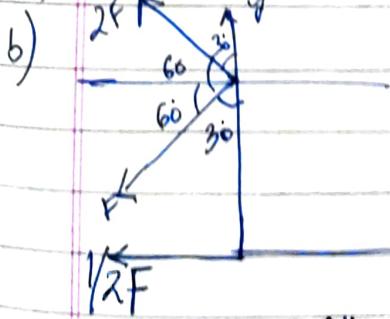
$$R = (-3F \sin 30 - 2F + F \sin 30)\hat{i} + (-3F \cos 30 - F \cos 30)\hat{j}$$

$$= (-3F\hat{i}) + \left(-\frac{2F\sqrt{3}}{2}\hat{j}\right) = -3F\hat{i} - 2F\sqrt{3}\hat{j}$$

at y = 0

$$M_o = 3F(d) - F(d) - 2F(d) = 0$$

as q. from poly

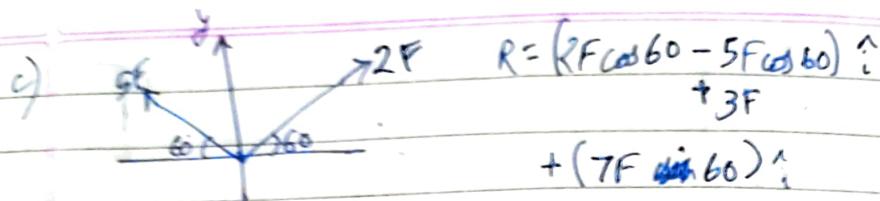


$$R = (-2F \cos 60 - F \cos 60 - \frac{1}{2}F)\hat{i} + (2F \cos 30 - F \cos 30)\hat{j}$$

$$= -2F\hat{i} + F\frac{\sqrt{3}}{2}\hat{j}$$

$$\frac{2F\sqrt{3}}{2} \cos 60$$

$$M_o = F(d) + 2F(d) - \frac{1}{2}F(d) = +\frac{5}{2}Fd = \boxed{\frac{5}{2}Fd}$$



$$R = (2F \cos 60^\circ - 5F \cos 60^\circ) \hat{i} + (7F \sin 60^\circ) \hat{j}$$

$$R = \left(F - \frac{5F}{2} + 3F \right) \hat{i} + \frac{7F \sqrt{3}}{2} \hat{j}$$

$$= \frac{3F \hat{i}}{2} + \frac{7\sqrt{3}F \hat{j}}{2}$$

$$M_0 = -2F(d) + 5Fd + 3F(d)$$

$$= F \cancel{Fd} = F \frac{l\sqrt{3}}{8} \text{ CCW}$$

Specify the location of force along y -axis
(F_y)

\Rightarrow dist along y -axis needed

b)

$$\begin{array}{l} R_x \leftarrow \\ (z) \end{array} \Rightarrow R_x \text{ should be above } 0$$

we got M_0 as CCW
 $\Rightarrow R_x(y) = M_0$

$$2F(y) = \frac{5\sqrt{3}F}{12} \Rightarrow y = \frac{5\sqrt{3}}{24}$$

c)

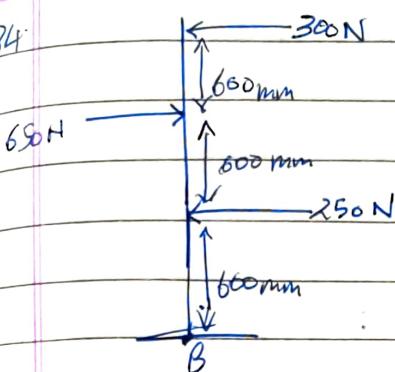
$R_x \rightarrow$ To produce CCW moment
 R_x should be below 0

$$R_x(y) > M_0$$

$$\frac{3F}{2}(y) = F l \sqrt{3}$$

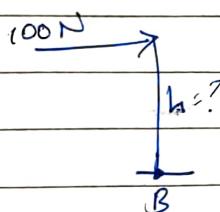
$$y = \frac{2l}{\sqrt{3}}$$

2/84



Find h above B where Res. of three forces act

$$\begin{aligned} R &= 680 - 300 - 250 \\ &= 350 - 250 \\ &= 100 \text{ N} \end{aligned}$$



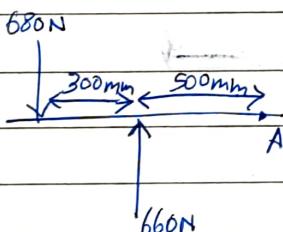
$$\begin{aligned} M_o &= 300(1.8) + 250(0.6) \\ &\quad - 680(1.2) \\ &= 540 + 150 - 780 \\ &= -90 \text{ Nm} \end{aligned}$$

$$10\phi(h) = 9\phi$$

$$h = 0.9 \text{ m}$$

= 90 Nm CW

2/85.

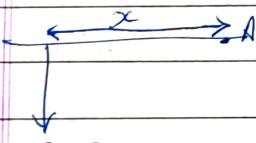


$$R = -680 + 660 = -20$$

$R = 20 \text{ N}$ below A

$$\begin{aligned} M_A &= +680(0.8) - 660(0.5) \\ &= 544 - 330 \end{aligned}$$

= 214 Nm CCW

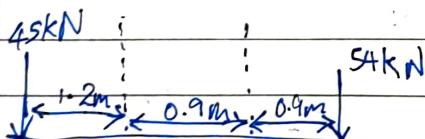


$$R(x) = M_A$$

$$20(x) = 214$$

$$x = 10.7 \text{ m} \text{ left of A}$$

2/86.

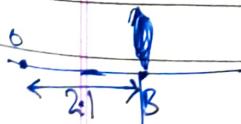


R passes through B

$$\begin{aligned} R &= 18 - 45 - 54 = \\ &= -81 \text{ kN} \end{aligned}$$

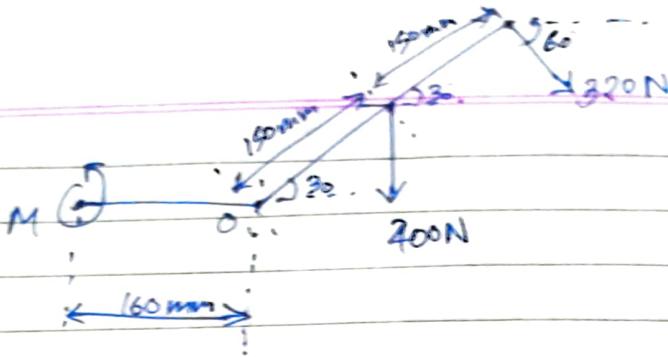
$$M_o = 81(2.1) \text{ Nm CCW}$$

$$= 170.1 \text{ kNm CW}$$



$$R = 81 \text{ kN (downwards)}$$

2/87



$R \rightarrow$ passes through O $M = ?$
~~9 complete M~~

$$R_y = 400 + 320 \sin 60 \\ = 677.128 \text{ N}$$

~~$M = 677.128(0.16) \\ = 108.34 \text{ Nm } \text{ cw}$~~

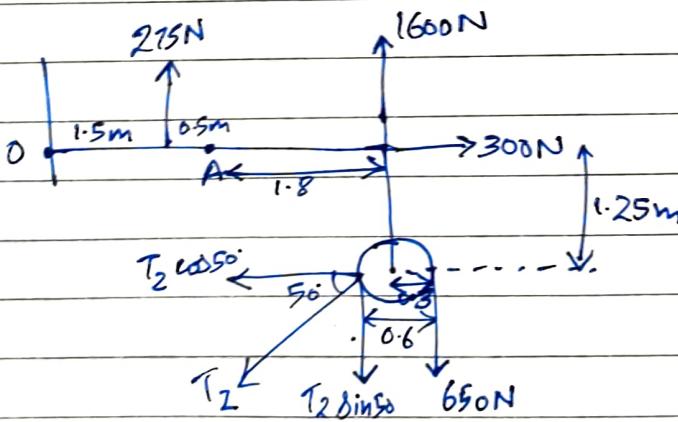
$\Rightarrow M_o = 0$

$M - 400(0.15 \cos 30) - 320(0.3) = 0$

$M - 91.96 - 96 = 0$

$M = 147.96 \text{ Nm}$

2/88



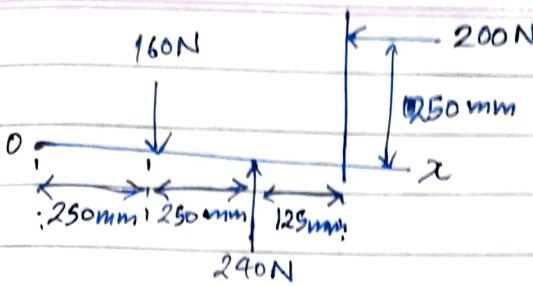
R passes through A $\Rightarrow \sum M_A = 0$

$\times T_2(0.3) ?$

$\sum M_A = 0 \Rightarrow -275(0.5) + 1600(1.8) - T_2 \cos 50(1.25) - T_2 \sin 50(1.8) \\ - 650(2.4) = 0$

$-137.5 + 2880 - 1365 = T_2(0.8) + T_2(1.378) \\ 1377.5 = T_2(2.178)$

2/89.



$$R = (240 - 160)\hat{j} - 200\hat{i}$$

$$= 80\hat{j} - 200\hat{i}$$

$$M_o = -160(0.25) + 240(0.5) + 200(0.25)$$

$$= 10 + 120$$

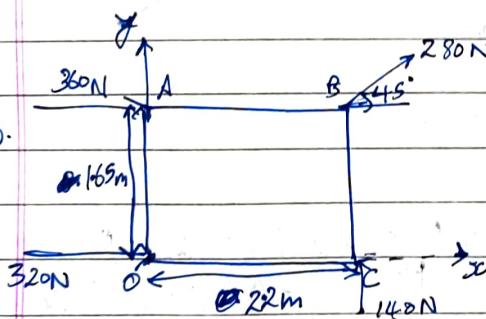
$$= 130 \text{ Nm CCW}$$

dist from O to point on x-axis $\Rightarrow R_y(x) = 130$

$$\text{at } x = 130$$

$x = 1.625 \text{ m}$ from O towards right
(off pipe)

2/90.



$$R = (360 + 320 + 280 \cos 45)\hat{i} + (140 + 280 \sin 45)\hat{j}$$

$$= 877.98\hat{i} + 337.98\hat{j}$$

$$M_o = -360(0.165) + 140(0.22) - 280 \cos 45(0.165) + 280 \sin 45(0.22)$$

$$= -59.4 + 30.8 - 32.66 + 43.55$$

$$= -17.702 \text{ Nm} = 17.702 \text{ Nm CW}$$

points on x-axis & y-axis through which COA of single R passes:

$$R_x(y) = 17.702$$

$$y = -0.02 \text{ or } 0.2$$

$$R_y(x) = 17.702$$

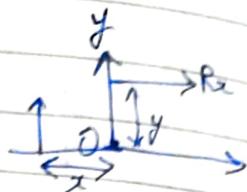
$$x = -0.05 \text{ or } 0.5$$

$$\text{Now } M_o = 177.02 \text{ Nm } \text{ C.W}$$

for M_o to be CW

R_x should be above O

$$\Rightarrow y = 0.2 \text{ m above O}$$

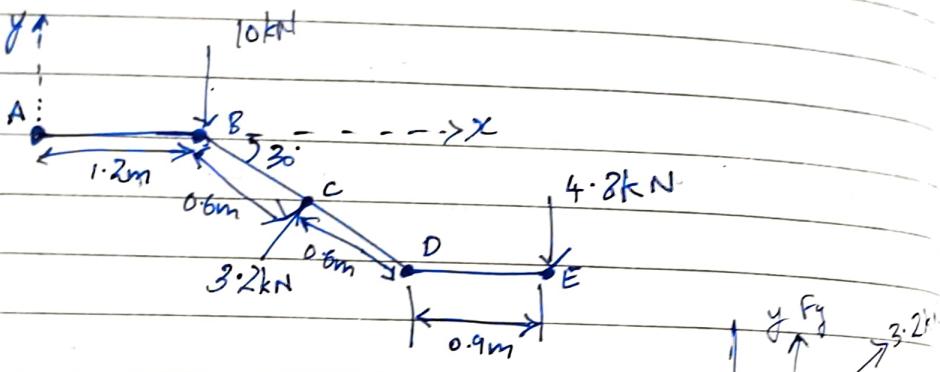
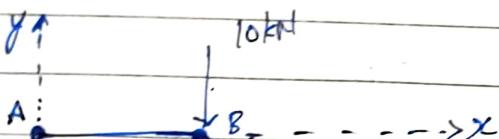


R_y should be left of O

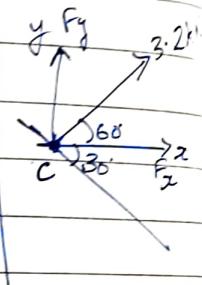
$$x = 0.5 \text{ m left of O}$$

$$\Rightarrow x = -0.5 \text{ m}$$

2/91



$$\begin{aligned} R &= [10\hat{j} - 4.8\hat{j} + 3.2 \sin 60\hat{i}] \\ &\quad + 3.2 \cos 60\hat{i} \\ &= -12.028\hat{j} + 1.6\hat{i} \end{aligned}$$



$$M_A = -10(1.2) + 3.2 \sin 60(0.6 \cos 30) + 3.2 \cos 60(0.6 \sin 30) + 1.2 - 4.8(0.9 + 1.2 \cos 30 + 1.2)$$

$$= -12 + 4.765 + 0.48 - 15.06$$

$$= -21.815 \text{ kNm}$$

$$= 21.815 \text{ kNm CW}$$

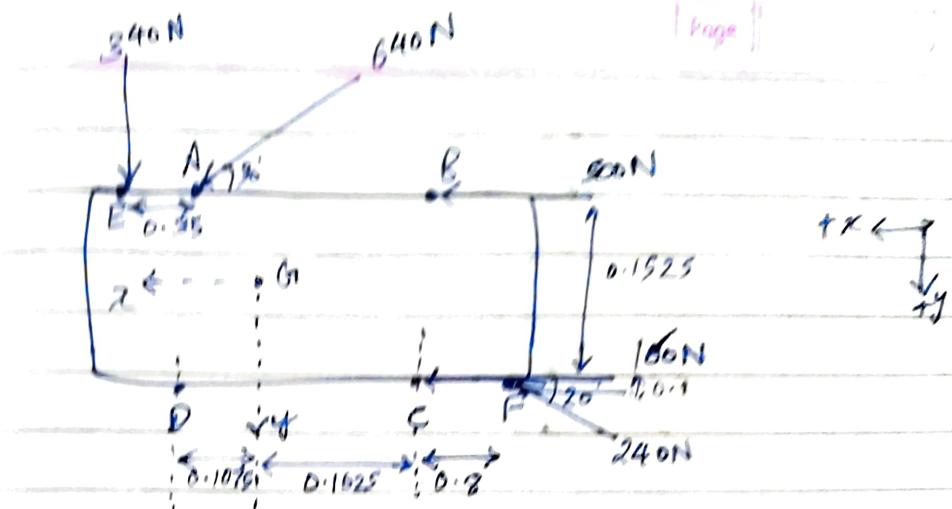
x-intercept of MoA of R

$$R_y(x) = M_A$$

$$12.028(x) = 21.815$$

$$x = 1.813 \text{ m}$$

2/92

(late
page)

$$\begin{aligned}
 R &= (4500 + 160 + 240 \cos 20 + 640 \cos 30) \hat{i} \\
 &\quad (+340 + 640 \sin 30 + 240 \sin 20) \hat{j} \\
 &= -1439.78 \hat{i} + 577.91 \hat{j}
 \end{aligned}$$

$$\begin{aligned}
 \sum M_G &= 340(0.35 + 0.1075) + (640 \cos 30 + 500 + 240 \cos 20) \frac{0.1525}{2} \\
 &\quad + 340(0.35 + 0.1075) + 640 \cos 30 \left(\frac{0.1525}{2}\right) + 500 \left(\frac{0.1525}{2}\right) \\
 &\quad - 160 \left(\frac{0.1525}{2}\right) - 240 \cos 20 \left(0.1 + \frac{0.1525}{2}\right) \\
 &\quad + 240 \sin 20 (0.1525 + 0.8) + 640 \sin 60 (0.1075) \\
 &= 1515 \text{ Nm CCW}
 \end{aligned}$$

2 copy-intercepts = ?

$$R_x(y) = M_{G_1} \quad +x \leftarrow \begin{matrix} G \\ \downarrow y \end{matrix}$$

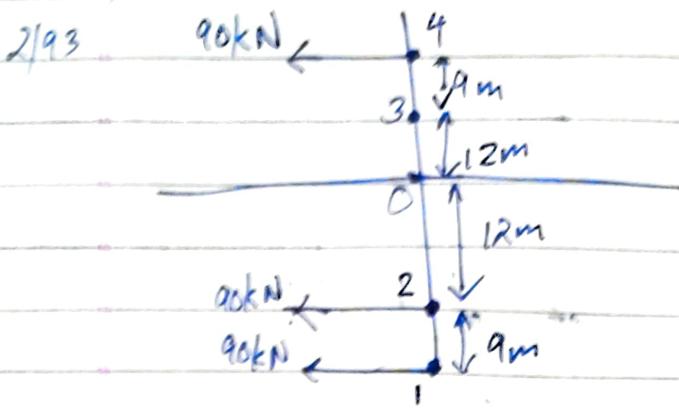
$$y = \frac{1515}{1439.78} = 1.0522$$

M is CCW $\Rightarrow R_x$ should be ~~upward~~ to the left
 $(0, -1.0522)$

$$R_y(x) = M_{G_1}$$

$$x = \frac{1515}{577.91} = 2.62$$

R_y ~~upward~~ to the left of G
 $(+2.62, 0)$



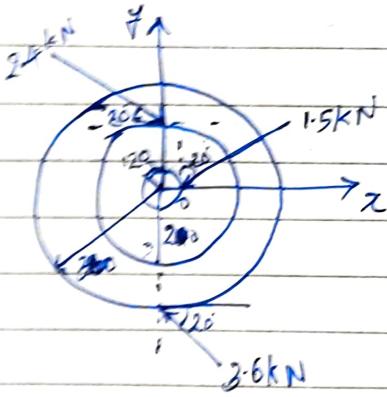
$$R = \cancel{270} \text{ kN } (-\hat{j})$$

$$\begin{aligned} M_0 &= 90(21) - 90(12) - 90(21) \\ &= -1080 \text{ kNm} \\ &= 1080 \text{ kNm CW} \end{aligned}$$

$$R_g(\cancel{d}) = 1080$$

$$d = \frac{1080}{270} = 4 \text{ m } \cancel{\text{below } O}$$

2/24



$$\begin{aligned} R &= (2.4 \cos 20 - 1.5 \sin 20 - 3.6 \cos 20) \hat{i} \\ &\quad + (-2.4 \sin 20 - 1.5 \cos 20 + 3.6 \sin 20) \hat{j} \\ &= -1.64 \hat{i} + -0.999 \hat{j} \end{aligned}$$

$$\begin{aligned} \sum M_O &= -2.4 \cos 20 (200) + 1.5 \sin 20 (120) - 3.6 \cos 20 (300) \\ &\quad - 1.5 \cos 20 (120) = \cancel{-1635} \text{ Nm CW} \\ &\approx 541 - 811 - 169.14 \\ &\approx 439.14 \text{ Nm} \Rightarrow 439.14 \text{ Nm CW} \end{aligned}$$

x & y intercepts

~~$R_y(x) = 439.14$~~

~~$x = 439.14 \text{ mm}$~~

~~0.999~~

~~$x = 439.57 \text{ mm}$~~

$R_x(y) = 1635$

$y = 996.95$

below 0

$(0, -996.95) \text{ mm}$

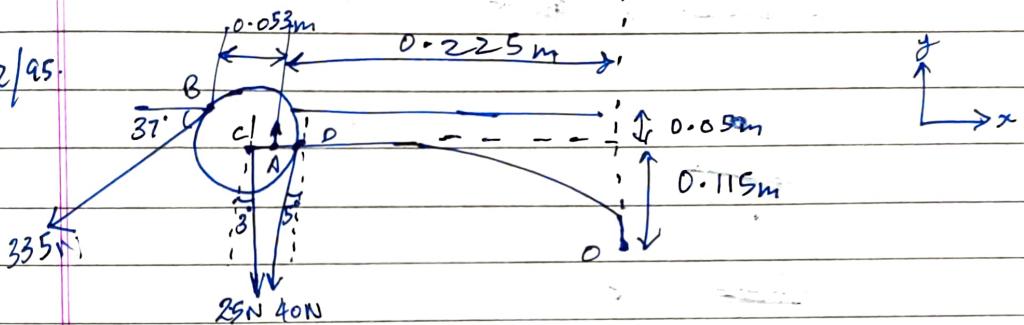
$R_y(x) = 1635 \text{ (cw)}$

$x = 1636.63 \text{ mm}$

sight of 20

$(1636.63, 0) \text{ mm}$

2/95



$AC = AD = 0.015 \text{ m}$

$$R = (-335 \cos 37 + 25 \sin 3^\circ) \hat{i} + (-335 \sin 37 - 25 \cos 3^\circ - 40 \cos 5^\circ) \hat{j}$$

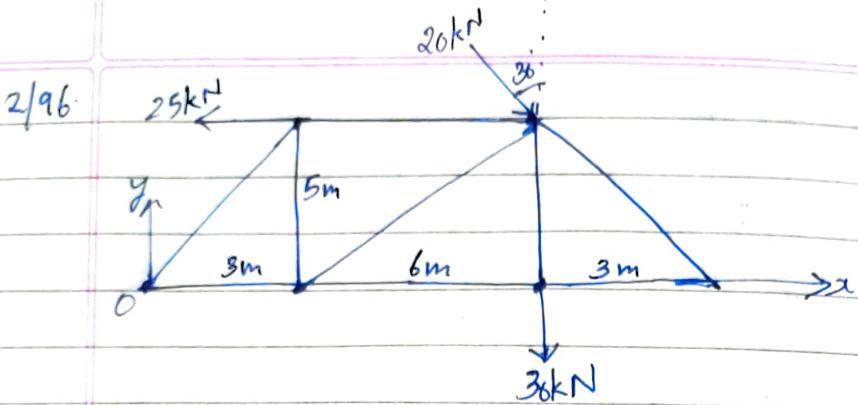
$= -269.72 \hat{i} + (-266.42) \hat{j}$

$M_o = +335 \cos 37 (0.165) - 25 \sin 3^\circ (0.115) + 40 \sin 5^\circ (0.115)$

$+ 335 \sin 37 (0.218) + 25 \cos 3^\circ (0.21) + 40 \cos 5^\circ (0.21)$

$= 210.968 \text{ Nm CCW}$

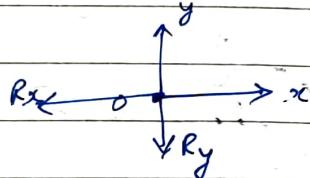
$.122.8$



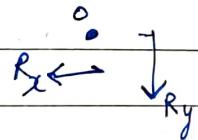
$$\begin{aligned}
 R &= (-25 + 20 \sin 30) \hat{i} + (-30 - 20 \cos 30) \hat{j} \\
 &= -15 \hat{i} - 47.32 \hat{j}
 \end{aligned}$$

$$\begin{aligned}
 M_0 &= +25(5) - 20 \sin 30(5) = 47.32(9) \text{ kNm} \\
 &= \cancel{-\frac{350 \cdot 88}{200}} = 350 \cdot 88 \text{ kNm CCW}
 \end{aligned}$$

$$\begin{aligned}
 R_x(y) &= 350 \cdot 88 \text{ CCW} \\
 y &= \frac{23.392}{15} = 350 \cdot 88
 \end{aligned}$$



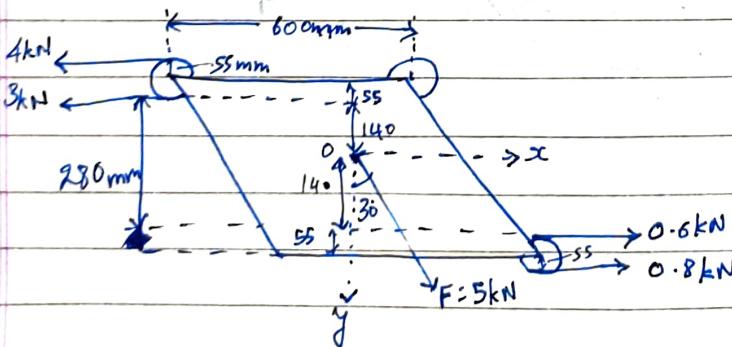
$$\begin{aligned}
 y &= \frac{23.392}{15} \text{ m fd CCW moment} \\
 \Rightarrow \text{below } O & \quad (0, -23.392)
 \end{aligned}$$



$$R_y(x) = 500 \cdot 88 \text{ CCW.}$$

$$\begin{aligned}
 x &= \frac{350 \cdot 88}{47.32} = 7.41 \text{ m fd CCW moment} \\
 &\text{right of } O \quad (7.41, 0)
 \end{aligned}$$

2/98.



point on y-axis through which R must pass through

$$R = (1.4 - 7)\hat{i} + (5 \cos 30)\hat{i} + 5 \sin 30$$

$$R = -3.1\hat{i} + 4.33\hat{i}$$

$$M_o = +4(55+55+140) + 3(140) + (0.6)(140) + (0.8)(140+55+55)$$

$$= 1000 + 420 + 84 + 200$$

$$= 1704 \text{ Nm CCW}$$

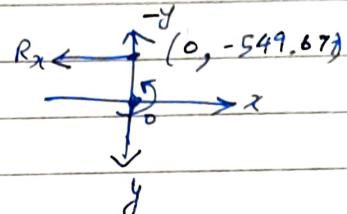
$$R_x(y) = M_o$$



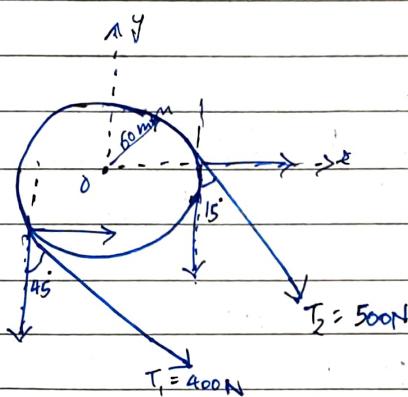
$$2.1 y = 1704$$

~~$y = 549.677$~~

$$x, y = (0, -549.677)$$

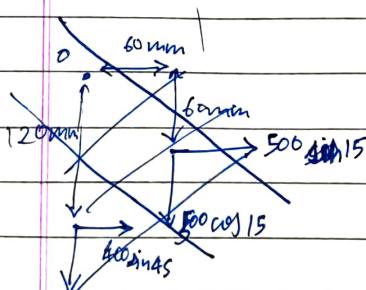
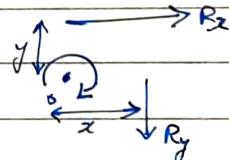


2/99.



$$R = (500 \sin 15 + 400 \sin 45)\hat{i} + (-400 \cos 45 - 500 \cos 15)\hat{j}$$

$$R = 412.25\hat{i} - 765.80\hat{j}$$

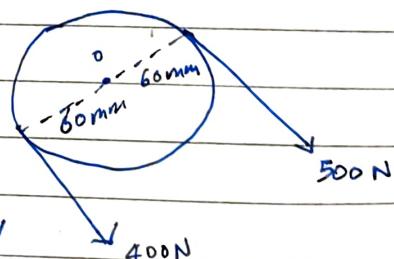


~~$$M_o = (500 \sin 15)(0.06) + (400 \sin 15)(0.12)$$

$$+ -(500 \cos 15)(0.06)$$~~

$$M_o = -500(0.06) + 400(0.06)$$

$$= -6 \text{ Nm} = 6 \text{ Nm CW}$$



$$R_x y = 6$$

$$y = \frac{6}{765.8} = 0.0078 \text{ m}$$

$$R_y x = 6$$

$$x = 0.0145 \text{ m}$$

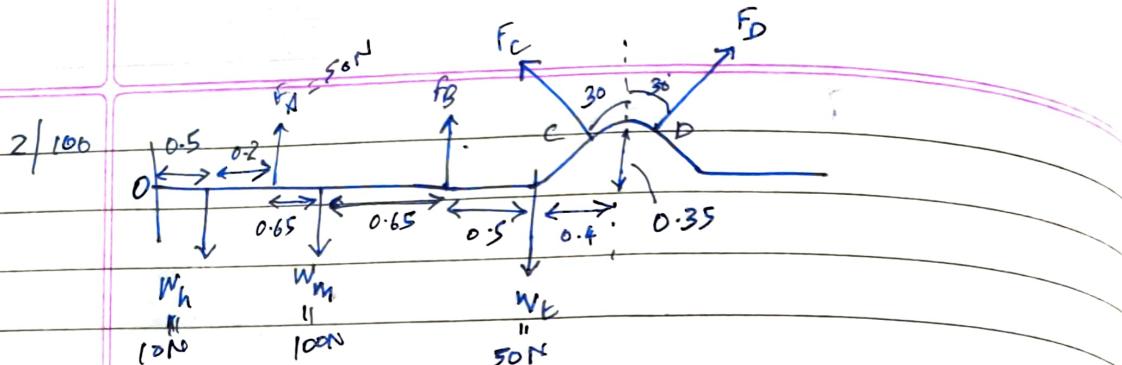
for R_x to produce CW $\Rightarrow R_x$ to be above 0

$$(0, 0.078) \text{ m}$$

for R_y to produce CW

$\Rightarrow R_y$ right of 0

$$(0.0145, 0)$$



$$F_C = F_D = F$$

Zero Force - couple system

$$R = (-F_C \sin 30 + F_D \sin 30) \hat{i} + [50 - 10 - 100 - 50 + F_C \cos 30 + F_D \cos 30] \hat{j} = 0$$

$$F_B + 2F(\cos 30) - 110 = 0 \\ F_B + \sqrt{3}F = 110$$

$$\sum M_o = 0 \\ -10(0.5) - 100(1.35) - 50(2.5) + 50(0.7) + F_B(2) \\ + 2F(\cos 30(2.9) + F \sin 30(0.35) - F \sin 30(0.3)) = 0$$

$$\text{on solving } F = F_C = F_D = 64.2N$$

$$F_B = 98.9N$$