

6th May, 2023

assign 5

$$1. \text{ i) } 3-\phi \quad \begin{aligned} T &= 30 \angle -30^\circ \text{ A} \\ \text{Star} \quad V_L &= 400 \angle 0^\circ \text{ V} \end{aligned}$$

$$V_{ph} = \frac{400}{\sqrt{3}} = 230.94$$

$$Z = \frac{V_{ph}}{I_{ph}} = \frac{230.94 \angle 0^\circ}{30 \angle -30^\circ} = 7.698 \angle 30^\circ \Omega$$

$$\begin{aligned} \text{ii) Total Power} &= \sqrt{3} V_L I_L \cos \phi \\ &= \sqrt{3} (30)(400) \cos 30^\circ = 18000 \text{ W} \end{aligned}$$

ass. 6. 1.3 ϕ $R = 20 \Omega$

$$L = 0.4 \text{ H}$$

$$X_L = 314(0.4) = 125.6 \Omega$$

$$V_L = 440 \text{ V}, 50 \text{ Hz}$$

$$V_{ph} = 440 \text{ V}$$

$$Z = 20 + j(125.6) \Omega = 127.18 \angle 80.95^\circ$$

$$I_{ph} = \frac{V_{ph}}{Z} = \frac{440}{127.18} = 3.45 \text{ A}$$

$$I_L =$$

$$\begin{aligned} \text{Active Power } P_{3-\phi} &= \sqrt{3} V_L I_L \cos \phi \\ &= \sqrt{3} (440)(3.45) \cos 80.95^\circ \end{aligned}$$

$$I_{ph} = \frac{440}{127.18} = 3.45$$

$$I_L = 3.45(\sqrt{3}) = 5.95$$

$$P = \sqrt{3} (440)(5.95) \cos 80.95^\circ = 652.9$$

1. 3- ϕ , Δ $R = 20 \Omega$

$$L = 0.4$$

$$V_L = V_{ph} = 440 \text{ V}, 50 \text{ Hz}$$

$$X_L = 125.6 \Omega$$

$$Z = 20 + j125.6$$

$$= 127.18 \angle 80.95^\circ$$

$$Z = \frac{V_{ph}}{I_{ph}}, \quad I_{ph} = \frac{V_{ph}}{Z} = \frac{440}{127.18} = 3.46$$

$$I_L = \sqrt{3}(3.46) = 5.99$$

$$\begin{aligned} \text{active Power } P_{3-\phi} &= \sqrt{3} V_L I_L \cos \phi \\ &= \sqrt{3} (440) (5.99) \cos (80.95) \\ &= 718.05 \text{ W} \end{aligned}$$

$$\begin{aligned} \text{Reactive Power } Q_{3-\phi} &= \sqrt{3} V_L I_L \sin \phi \\ &= \sqrt{3} (440) (5.99) \sin (80.95) \\ &= 4508.16 \text{ W} \end{aligned}$$

$$\text{Q8. } W_1 : W_2 = 4 : 1$$

$$\phi = \cos^{-1} \left(\frac{\sqrt{3} (W_2 - W_1)}{(W_1 + W_2)} \right) = \cos^{-1} \left(\frac{\sqrt{3} (3)}{5} \right) = 46.102$$

$$\phi = \cos^{-1} (46.102) = 0.693$$

$$\text{Q9. } W_1 = W_2 = 50 \text{ kW}$$

$$W_1 + W_2 = 100 \text{ kW} \quad \text{--- (1)}$$

$$\text{now } \text{p.f.} = \cos \left(\tan^{-1} \left(\frac{\sqrt{3} (W_2 - W_1)}{W_1 + W_2} \right) \right)$$

$$\text{p.f.} = 0.866$$

$$\frac{1}{\sqrt{3}} = \frac{\sqrt{3} (W_2 - W_1)}{W_1 + W_2}$$

$$W_1 + W_2 = 3 (W_2 - W_1)$$

$$\Rightarrow 3 (W_2 - W_1) = 100$$

$$W_2 - W_1 = \frac{100}{3} = 33.33 \quad \text{--- (2)}$$

$$2 W_2 = 133.33$$

$$\boxed{W_2 = 66.67 \text{ W}}$$

$$\boxed{W_2 = 66.67 \text{ W}}$$

$$\boxed{W_1 = 33.33 \text{ W}}$$

Q8. Δ 3- ϕ $Z = 8 - j6 \Omega = 10 \angle -36.87^\circ$

$Z = R - jX_c$, $V_L = 230V$, $50Hz$
 $R = 8\Omega$ $V_{ph} = 230$

$X_c = 6\Omega$ $C = \frac{1}{314(6)} = 5.3 \times 10^{-4} F$

i) I_L ii) p.f iii) $Q_{3-\phi}$

$I_L = \frac{Z = V_{ph}}{I_{ph}} \quad I_{ph} = \frac{V_{ph}}{Z} = \frac{230}{10} = 23$

$I_L = \sqrt{3}(23)$
 $= 39.83A$
 $= 39.83 \angle 36.87$

ii) $p.f = \cos(36.87) = 0.799 = 0.8$

iii) $S = \sqrt{3} V_L I_L \sin \phi$
 $= \sqrt{3} (23) (39.83) \sin(36.87)$
 $=$

3. 3- ϕ Δ $I_L = I_{ph}$
 $V_{ph} = \frac{V_L}{\sqrt{3}}$

$V_L = 400V$, $50Hz$

$V_{ph} = 230.94V$

$P_1 = 3kW$

$P_2 = 1kW$

$R = ?$ $C = ?$

$p.f = \cos\left(\tan^{-1}\left(\frac{\sqrt{3}(\omega_2 - \omega_1)}{\omega_1 + \omega_2}\right)\right)$
 $= 0.755$

$\phi = 40.89^\circ$

$Z = \frac{V_{ph}}{I_{ph}}$

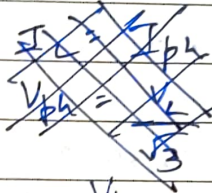
$400 = \sqrt{3} (400) I_L \cos(0.755)$

$I_L = \frac{400}{\sqrt{3} \cos(0.755)} = 7.647$

$$Z = 30.2 \angle -40.89^\circ$$

$$= \frac{22.83}{R} - j \frac{19.769}{X_L}$$

$$C = \frac{1}{314(19.769)} = 161 \mu F$$

4. 3- ϕ Δ 

$$I_L = \sqrt{3} I_{ph}$$

$$V_{ph} = V_L$$

$$V_{ph} = 115.47 V$$

$$V_L = 200 V = V_{ph}$$

$$Z = 14 - j14 \Omega = 19.79 \angle -45^\circ$$

$$P = ? \quad S = ?$$

$$I_L = \frac{V_{ph}}{Z} = \frac{115.47}{19.79} = 5.834 A$$

$$I_{ph} = \frac{200 \angle 45^\circ}{19.79} = 10.10 \angle 45^\circ$$

$$I_{ph1} = 10.10 \angle 45^\circ$$

$$I_{ph2} = 10.1 \angle 45 - 120^\circ = 10.1 \angle -75^\circ$$

$$I_{ph3} = 10.1 \angle -75 - 120^\circ = 10.1 \angle -195^\circ$$

$$I_{L1} = 10.1(\sqrt{3}) \angle 45 - 30^\circ = 17.5 \angle 15^\circ$$

$$I_{L2} = 17.5 \angle -75 - 30^\circ = 17.5 \angle -105^\circ$$

$$I_{L3} = 17.5 \angle -195 - 30^\circ = 17.5 \angle -225^\circ$$

$$p_h = 0.707 (\text{lead})$$

$$P_T = \sqrt{3} V_L I_L \cos \phi$$

$$= \sqrt{3} (200) (17.5) (0.707)$$

$$= 4.286 \text{ kW}$$

$$Q = \sqrt{3} V_L I_L \sin \phi$$

$$= 4.286 \text{ kW}$$

$$S = \sqrt{P^2 + Q^2} = 6.06 \text{ kW}$$

5. $P = 150 \text{ kW}$
 $I_L = 100 \text{ A (lead)}$
 $V_L = 1100 \text{ V, } 50 \text{ Hz}$
 circuit constants: ? R, C

3- ϕ star

$I_L = I_{ph}$
 $V_{ph} = \frac{1100}{\sqrt{3}} = 635.08$

$$150 \times 10^3 = \sqrt{3} (1100) (100) \cos \phi$$

$$\cos \phi = 0.787$$

$$\phi = 38.06^\circ$$

$$Z = \frac{V_{ph}}{I_{ph}} = \frac{635.08}{100} = 6.3508 \angle 38.06$$

$$Z = 5.00 - j3.97$$

X_C

$$C = \frac{1}{314(3.97)} = 812.4 \mu\text{F}$$

6. $V_L = 400 \text{ V}$
 o/p $P = 25 \text{ HP}$
 $\eta = 87\%$
 $\text{pf} = 0.82$

3- ϕ Δ : I_L, I_{ph}

$V_L = V_{ph}$
 $I_L = \sqrt{3} I_{ph}$

$$0.87 = \frac{25 \times 746}{P \cdot I}$$

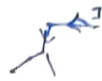
$$21436.78$$

$$P = \cancel{23151.73} \text{ W}$$

$$\cancel{23151.78} = \sqrt{3} (400) (I_L) (0.82)$$

$$I_L = \cancel{40.752} 37.73 \text{ A}$$

$$I_{ph} = \frac{37.73}{\sqrt{3}} = 21.78 \text{ A}$$



7. 3- ϕ $V_L = 2600V = V_{ph}$

Δ $P = 300 \times 10^3 W$

$I_L = \sqrt{3} I_{ph}$ $I_L = 100A$ (lead)

$I_{ph} = 57.74$

$3 \times 10^5 = \sqrt{3} (2600) (100) \cos \phi$

$\cos \phi = 0.866$

$\phi = 30^\circ$

$Z = \frac{V_{ph}}{I_{ph}} = \frac{2600}{57.74} = 34.64 \angle -30^\circ$

$Z = \frac{29.999}{R} - j \frac{17.32}{X_L}$

$C = \frac{1}{314(17.32)} = 183.87 \mu F$

8. $Z = 20 + j15 \Omega = \frac{25 \angle 36.86^\circ}{3 \phi \text{ Y conn}}$

$V_{ph} = \frac{400}{\sqrt{3}} = 230.94$

$V_L = 400$

$I_{ph} = \frac{230.94}{25} = 9.24A$

$P = \sqrt{3} V_L I_L \cos \phi$

$= \sqrt{3} (400) (9.24) \cos(36.86^\circ) = 5151.99$

$= 2515W$

9. $W_1 = 8kW$ $W_2 = -0.8kW$

$pf = \cos \left(\tan^{-1} \left(\frac{\sqrt{3}(\omega_2 - \omega_1)}{\omega_1 + \omega_2} \right) \right) = 0.427$

$\phi = 64.72^\circ$

$P = W_1 + W_2$

$= 7.2kW$

$Q = \sqrt{3} V_L I_L \sin \phi$

$\phi = 16.86^\circ (\sin(64.72^\circ))$

$7.2 = \sqrt{3} V_L I_L \cos \phi$

$Q = 15.24 VAR$

$7.2 = \sqrt{3} V_L I_L$

0.427

$= 1686W$

10. $V_L = 200V$ 3- ϕ star star $V_{ph} = 115.47$
 $Z = 9 - j5$
 $= 10.29 \angle -29.05^\circ$ $\phi = -29.05$

$$I_{ph} = \frac{115.47}{10.29} = 11.23 = I_L$$

$$P_1 = V_L I_L \cos(30 + \phi)$$

$$= 200(11.23) \cos(30 - 29.05)$$

$$= 2243.69 W$$

$$P_2 = V_L I_L \cos(30 - \phi)$$

$$= 1154.06 W$$

11. 3- ϕ Δ $V_L = 400V$
 50Hz $I_L = 27.72$; $I_{ph} = \frac{27.72}{\sqrt{3}} = 16.00$
 $P = 15360$

$$15360 = \sqrt{3}(400)(27.72) \cos \phi$$

$$\cos \phi = 0.799$$

$$\phi = 36.88^\circ$$

$$Z = \frac{V_{ph}}{I_{ph}} = \frac{400}{16} = 25$$

$$Z = 25 \angle 36.88^\circ$$

$$= 19.99 + j15.00$$

$$R = 20 \Omega$$

$$X_L = 15$$

$$L = \frac{15}{314} = 0.0477 = 47.7 \text{ mH}$$