

Parallel and Distributed Computing

First Project

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1 Introduction

This report presents the algorithms, performance results and respective analysis of the first project in the Parallel and Distributed Computing course.

The aim of this project was to evaluate performance between single-core (in 2 languages) and multi-core (using OpenMP) approaches to a problem. Specifically, we wanted to implement and compare 5 different algorithms to perform the multiplication of two matrices (see Algorithms Explanation).

By developing the code for these tasks, we became more familiar with modern and high performance C++ and Lua, since we chose it as our alternative implementation language. Moreover, we also had to research about matrix multiplication algorithms and optimizations, a common benchmark in computing. Last but not least, in order to implement multi-core solutions, we explored and experimented with the OpenMP standard, allowing us to learn more about CPU multithreading.

2 Algorithms Explanation

To see the effects of cache locality and parallel computing on matrix multiplication implementations, we used five different matrix multiplication algorithms, described in this section. These algorithms perform the same operations, ending in the same results, only differing by the order of the operations done, which, as we will see, will have crucial impacts on each algorithm's performance.

2.1 Classic Matrix Multiplication

The *classic* matrix multiplication algorithm is closely related to its hand calculation. This method for multiplication of two matrices: $A \times B = C$, where $A(m, n)$, $B(n, p)$ and $C(m, p)$, obtains the sum of a cell (m, p) in the solution, by linear combination of row m of A and column p of C.

Implementing this algorithm is fairly straightforward, as we only need to iterate through every row and column of the solution matrix, and, for each cell, perform the linear combination of the values:

```
for (i = 0; i < m; i++)
    for (j = 0; j < p; j++)
        for (k = 0; k < n; k++)
            // Perform operations
```

Figure 1: Overview of Classic Matrix Multiplication Algorithm

2.2 Line Matrix Multiplication

The line matrix multiplication algorithm is very similar to the previous algorithm. The only difference is that the second and third loops switch places:

```
for (i = 0; i < m; i++)
    for (k = 0; k < n; k++)
        for (j = 0; j < p; j++)
            // Perform operations
```

Figure 2: Overview of Line Matrix Multiplication Algorithm

In practice, the difference between this and the previous approach is that instead of calculating the result matrix cell by cell, we instead focus on calculating and storing some terms of the linear combination line by line.

Although the correctness and overall time complexity of this algorithm remains the same, due to the way the matrices are stored and the memory is accessed, this allows for fewer cache misses, leading to performance improvements.

2.3 Block Matrix Multiplication

The last single-core algorithm implemented is the block matrix multiplication algorithm. This approach expands on top of the previous one and the same logic applied in calculating subresults line by line is now used to calculate the solution block by block. For this, we need 6 nested loops:

```
for (I = 0; I < m; I += block_size)
    for (K = 0; K < n; K += block_size)
        for (J = 0; J < p; J += block_size)
            for (i = I; i < min(I + block_size, m); i++)
                for (k = K; k < min(K + block_size, n); k++)
                    for (j = J; j < min(J + block_size, p); j++)
                        // Perform operations
```

Figure 3: Overview of Block Matrix Multiplication Algorithm

The main idea is that now, we have divided the matrix into smaller blocks and the operations are performed block by block. Again, due to the way the memory is accessed, this leads to better performance and less cache misses because the local block information is already stored in cache.

2.4 Parallel Matrix Multiplication

2.4.1 First Version

2.4.2 Second Version

3 Performance Metrics

MM.

4 Results and Analysis

5 Conclusion

References