

ANALYTIC GEOMETRY, PROBLEM SET 5

Representations of the line in plane

1. Find the equation of the line passing through the intersection point of the lines $d_1 : 2x - 5y - 1 = 0$ and $d_2 : x + 4y - 7 = 0$ and through a point M which divides the segment $[AB]$, given by $A(4, -3)$ and $B(-1, 2)$, into the ratio $k = 2/3$.
2. Find the equation of the line passing through the intersection point of $d_1 : 3x - 2y + 5 = 0$, $d_2 : 4x + 3y - 1 = 0$ and intersecting the Oy axis at the point A with $OA = 3$.
3. Find the parametric equations of the line through P_1 and P_2 , when
 - (1) $P_1(3, -2)$, $P_2(5, 1)$;
 - (2) $P_1(4, 1)$, $P_2(4, 3)$.In each case, find the vector equation of the line passing through these points.
4. Find the parametric equations of the line through $P(-5, 2)$ and parallel to $\vec{v}(2, 3)$.
5. Show that the equations $x = 3 - t$, $y = 1 + 2t$ and $x = -1 + 3t$, $y = 9 - 6t$ represent the same line. Write down a director vector for this line.
6. The points $M_1(1, 2)$, $M_2(3, 4)$ and $M_3(5, -1)$ are the midpoints of the sides of a triangle. Write down the equations of the lines determined by the sides of the triangle.
7. Given the line $d : 2x + 3y + 4 = 0$, find the equation of a line d_1 passing through the point $M_0(2, 1)$, in the following situations: a) d_1 is parallel with d ; b) d_1 is orthogonal on d ; c) the angle determined by d and d_1 is $\pi/4$.
8. The vertices of the triangle $\triangle ABC$ are the intersection points of the lines $d_1 : 4x + 3y - 5 = 0$, $d_2 : x - 3y + 10 = 0$, $d_3 : x - 2 = 0$. a) Find the coordinates of A , B and C . b) Find the equations of the median lines of the triangle. c) Find the equations of the heights of the triangle.
9. Find the coordinates of the symmetrical of the point $P(-5, 13)$ with respect to the line $d : 2x - 3y - 3 = 0$.
10. Find the coordinates of the point P on the line $d : 2x - y - 5 = 0$, for which the sum $AP + PB$ attains its minimum, when $A(-7, 1)$ and $B(-5, 5)$.
11. Find the coordinates of the circumcenter (the center of the circumscribed circle) of the triangle determined by the lines $4x - y + 2 = 0$, $x - 4y - 8 = 0$ and $x + 4y - 8 = 0$.