

## SEMINARS 7

1) Solve the following systems of linear equations using Gauss elimination algorithm:

$$\text{a) } \begin{cases} x_1 + x_2 + 2x_3 = -1 \\ 2x_1 - x_2 + 2x_3 = -4 \text{ (in } \mathbb{R}^3); \\ 4x_1 + x_2 + 4x_3 = -2 \end{cases} \quad \text{b) } \begin{cases} 3x_1 + 4x_2 + x_3 + 2x_4 = 3 \\ 6x_1 + 8x_2 + 2x_3 + 5x_4 = 7 \text{ (in } \mathbb{R}^4); \\ 9x_1 + 12x_2 + 3x_3 + 10x_4 = 13 \end{cases}$$

$$\text{c) } \begin{cases} x_1 + x_2 - 3x_3 = -1 \\ 2x_1 + x_2 - 2x_3 = 1 \\ x_1 + x_2 + x_3 = 3 \\ x_1 + 2x_2 - 3x_3 = 1 \end{cases} \quad (\text{in } \mathbb{R}^3).$$

2) Using Gauss elimination algorithm, discuss on the real parameter  $\alpha$  the consistency of the following systems, then solve them:

$$\text{a) } \begin{cases} 5x_1 - 3x_2 + 2x_3 + 4x_4 = 3 \\ 4x_1 - 2x_2 + 3x_3 + 7x_4 = 1 \\ 8x_1 - 6x_2 - x_3 - 5x_4 = 9 \\ 7x_1 - 3x_2 + 7x_3 + 17x_4 = \alpha \end{cases}, \quad \text{b) } \begin{cases} 2x_1 - x_2 + 3x_3 + 4x_4 = 5 \\ 4x_1 - 2x_2 + 5x_3 + 6x_4 = 7 \\ 6x_1 - 3x_2 + 7x_3 + 8x_4 = 9 \\ \alpha x_1 - 4x_2 + 9x_3 + 10x_4 = 11 \end{cases};$$

$$\text{c) } \begin{cases} \alpha x_1 + x_2 + x_3 = 1 \\ x_1 + \alpha x_2 + x_3 = 1 \\ x_1 + x_2 + \alpha x_3 = 1 \end{cases}.$$