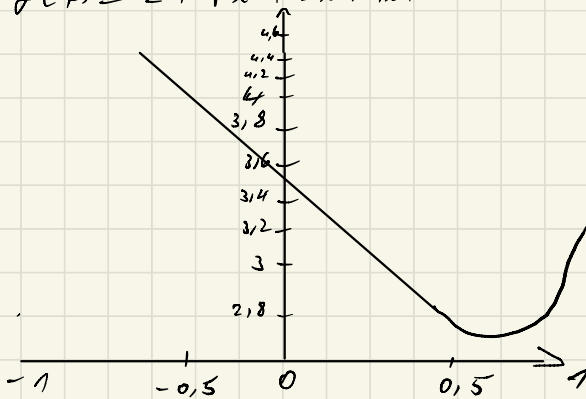


1) a) $y(x) = 2 - \sqrt{x^3 + 2x^2 - 4x + 4}$

$y(x) = 2 + \sqrt{x^3 + 2x^2 - 4x + 4}$

b) $y(x) = 2 + \sqrt{x^3 + 2x^2 - 4x + 4}$

c)



2) a)

b) $y(x) = \left(-\frac{e^{2x}}{x} - 2Ei_1(-2x) - C_1 - C_2 \right) x$

c) $y(x) = \left(\frac{-\frac{e^{2x}}{x} - 2Ei_1(-2x)}{e^2} + \frac{2Ei_1(-2) + 3e^2}{e^2} \right) x$

3) eq. points: 0, 1, $-\frac{1}{2}$

- 0: unstable
- 1: locally asymptotically stable
- $-\frac{1}{2}$: locally asymptotically stable

4) a) $x(x) = C_1 e^{\sqrt{5}x} + C_2 e^{-\sqrt{5}x}$

$y(x) = C_1 \sqrt{5} e^{\sqrt{5}x} - C_2 \sqrt{5} e^{-\sqrt{5}x} - 2C_1 e^{\sqrt{5}x} - 2C_2 e^{-\sqrt{5}x}$

$$b) x(t) = \left(1 + \frac{4\sqrt{5}}{5}\right) e^{\sqrt{5}t} + \left(1 - \frac{4\sqrt{5}}{5}\right) e^{-\sqrt{5}t}$$

$$y(t) = \left(1 + \frac{4\sqrt{5}}{5}\right) \sqrt{5} e^{\sqrt{5}t} - \left(1 - \frac{4\sqrt{5}}{5}\right) \sqrt{5} e^{-\sqrt{5}t} - 2\left(1 + \frac{4\sqrt{5}}{5}\right) e^{\sqrt{5}t}$$

$$- 2\left(1 - \frac{4\sqrt{5}}{5}\right) e^{-\sqrt{5}t}.$$