

Find Peak Element

Key Idea:

Look at the slope around a middle index:

- Pick mid:
- Compare $\text{nums}[\text{mid}]$ and $\text{nums}[\text{mid}+1]$ (safe if you keep the search range so $\text{mid}+1$ is valid).
 - If $\text{nums}[\text{mid}] < \text{nums}[\text{mid}+1]$, you are on an uphill slope \rightarrow a peak must exist to the right. Move $\text{lo} = \text{mid}+1$.
 - Else, you are on a downhill (or at a local ridge) \rightarrow a peak must exist to the left or at mid.

Why is this safe? Because with the $-\infty$ padding outside the array and the $\text{nums}[i] \neq \text{nums}[i+1]$ constraint, any uphill must crest somewhere; any downhill came from a crest to the left.

Algorithm (binary search):

- Initialize $\text{lo} = 0$, $\text{hi} = n-1$.
- While $\text{lo} < \text{hi}$:
 - $\text{mid} = (\text{lo} + \text{hi}) / 2$.
 - If $\text{nums}[\text{mid}] < \text{nums}[\text{mid}+1]$: $\text{lo} = \text{mid}+1$
 - Else: $\text{hi} = \text{mid}$
- Return lo (or hi ; they're equal). That index is a peak.

Complexity:

- Time: $O(\log n)$
- Space: $O(1)$