

## Merge k Sorted Lists

This is the classic problem which generalises merging two sorted linked lists; the optimal approach is using a min-heap (priority queue).

**[Key Idea:]** Use a min-heap to always extract the node with the smallest value.

- Push the first node of each list into the heap initially.
- Repeatedly pop the smallest node and push its next into the heap (if exists).
- Build the merged list incrementally.

- [Steps:]**
1. Create a min-heap (priority queue) ordered by node value.
  2. Push all head nodes of the lists into the heap (if not null).
  3. Initialise a dummy node and maintain a tail pointer.
  4. While the heap is not empty.
    - Pop the smallest node.
    - Attach it to the merged list.
    - Push the popped node's next into the heap if it exists.
  5. Return dummy  $\rightarrow$  next.

**[Complexity:]** Let  $N$  = total number of nodes across all lists,  $k$  = number of lists.

- Time:  $O(N \log k)$  (each node push/pop costs  $\log k$ ).
- Space:  $O(k)$  (heap size)