

Unique Paths II

Key idea (DP with obstacles):

Let $ways[i][j]$ be the number of paths to cell (i, j) from $(0, 0)$ moving only right/down and never stepping on a 1.

Transition:

- If obstacle $Grid[i][j] = 1$, then $ways[i][j] = 0$ (can't stand here).

- Else, $ways[i][j] = ways[i-1][j] + ways[i][j-1]$ (from top + from left).

Base:

- If the start is blocked ($obstacle\ Grid[0][0] = 1$) or the end is blocked, answer is 0.

- Otherwise, $ways[0][0] = 1$.

Space-optimized (1D DP):

Use a 1D array $dp[j]$ that represents ways for the current row:

- Initialize $dp[0] = 1$ if the start cell is not an obstacle; otherwise 0.

- For each row i :

- For each column j from left to right:

- If $obstacle\ Grid[i][j] = 1$:

- set $dp[j] = 0$ (you cannot land here)

- Else update $dp[j] += dp[j-1]$ if $j > 0$ (add ways from the left).

- (Note: $dp[j]$ already holds the ways from above)

This works because:

- $dp[j]$ before the update = ways from above.

- $dp[j-1]$ = ways from left in the current row.

- Setting to 0 on obstacle kills any paths landing on that cell.