

Solving Logarithmic and Exponential Equations

Quick Start

Success in College Math

Overview

This video will cover:

Overview

This video will cover:

1. Inverse Properties of Logarithms and Exponential Functions

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This video will cover:

1. Inverse Properties of Logarithms and Exponential Functions
2. Solving Exponential Equations

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1. Inverse Properties of Logarithms and Exponential Functions
2. Solving Exponential Equations
3. Solving Logarithmic Equations

Inverse Properties of Logarithms and Exponential Functions

For all x ,

$$\log_b b^x = x.$$

For $x > 0$,

$$b^{\log_b x} = x.$$

How To - Solve Exponential Equations

To solve an equation containing an exponential expression:

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3. Cancel the logarithm and exponential expression using the Inverse Property.

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To solve an equation containing an exponential expression:

1. Isolate the exponential expression.
2. Take the logarithm of both sides. Use the same base for the logarithm as the exponential expression.
3. Cancel the logarithm and exponential expression using the Inverse Property.
4. Solve the resulting equation.

Example 1

Solve the equation. Round your answer to three decimal places where appropriate.

$$4 \cdot 9^{2x} = 14$$

Example 1

Solve for the
exponential
expression.

$$\begin{array}{r} 4 \cdot 9^{2x} = 14 \\ \hline \cancel{4} \cdot 9^{2x} = \frac{14}{\cancel{4}} \\ \hline 9^{2x} = 3.5 \end{array}$$

Example 1

- Take the logarithm base 9 of both sides.
- Cancel the logarithm and exponent.

$$9^{2x} = 3.5$$

$$\log_9 9^{2x} = \log_9 3.5$$

$$2x = \log_9 3.5$$

Example 1

- Solve for x .
- Round your answer to three decimal places.

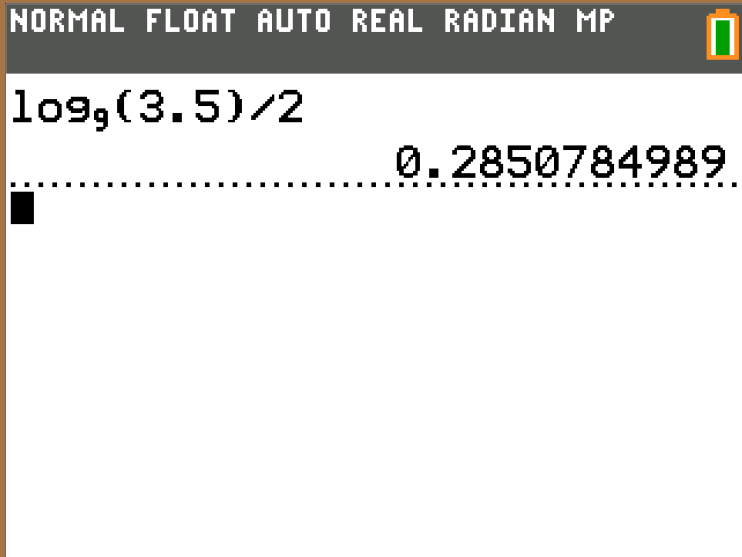
$$2x = \log_9 3.5$$

$$\frac{\cancel{2}x}{\cancel{2}} = \frac{\log_9 3.5}{2}$$

$$x = \frac{\log_9 3.5}{2} = 0.285$$

Example 1

- Solve for x .
- Round your answer to three decimal places.



Example 2

Solve the equation. Round your answer to three decimal places where appropriate.

$$10^{2x-18} + 12 = -3$$

Example 2

Solve for the
exponential
expression.

$$\begin{array}{r} 10^{2x-18} + 12 = -3 \\ 10^{2x-18} + 12 = -3 \\ \quad -12 \quad -12 \\ \hline 10^{2x-18} = -15 \end{array}$$

Example 2

- Take the common logarithm of both sides.
- The common logarithm isn't defined for -15 , so the equation does not have (real number) solutions.

$$10^{2x-18} = -15$$

$$\log 10^{2x-18} = \log(-15)$$

$\log(-15)$ is not defined
for real numbers.

How To - Solve Logarithmic Equations

To solve an equation containing a logarithm:

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To solve an equation containing a logarithm:

1. Isolate the logarithmic expression.
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3. Cancel the exponential expression and logarithm using the Inverse Property.

How To - Solve Logarithmic Equations

To solve an equation containing a logarithm:

1. Isolate the logarithmic expression.
2. Use both sides as an exponent in an exponential expression. Use the same base for the exponential expression as the logarithm.
3. Cancel the exponential expression and logarithm using the Inverse Property.
4. Solve the resulting equation.

Example 3

Solve the equation. Round your answer to three decimal places where appropriate.

$$2 \cdot \log(6x) + 16 = 14$$

Example 3

Solve for the
logarithm.

$$2 \cdot \log(6x) + 16 = 14$$

$$2 \cdot \log(6x) + 16 = 14$$

$$\quad -16 \quad -16$$

$$2 \cdot \log(6x) = -2$$

$$\frac{2 \cdot \log(6x)}{2} = \frac{-2}{2}$$

$$\log(6x) = -1$$

Example 3

- Use both sides as an exponent with base 10.
- Cancel the exponent and logarithm.
- The negative exponent is defined, so we know there are solutions.

$$\log(6x) = -1$$

$$10^{\log(6x)} = 10^{-1}$$

$$6x = 10^{-1}$$

Example 3

- Solve the equation for x .
- Round the answer to three decimal places.

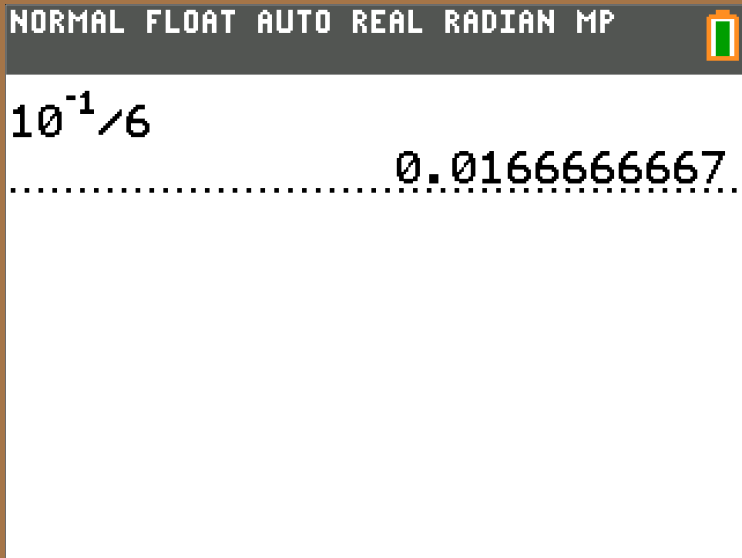
$$6x = 10^{-1}$$

$$\frac{6x}{6} = \frac{10^{-1}}{6}$$

$$x = \frac{10^{-1}}{6} = 0.017$$

Example 3

- Solve the equation for x .
- Round the answer to three decimal places.



Example 4

Solve the equation. Round your answer to three decimal places where appropriate.

$$\log_8 (3x - 18) = 3$$

Example 4

- Use both sides of the equation as an exponent with base 8.
- Cancel the exponent and logarithm.

$$\log_8(3x - 18) = 3$$

$$8^{\log_8(3x - 18)} = 8^3$$

$$3x - 18 = 8^3$$

Example 4

- Solve the equation for x .
- Round the answer to three decimal places.

$$3x - 18 = 8^3$$

$$3x - 18 = 8^3$$

$+ 18 \quad + 18$

$$3x = 8^3 + 18$$

$$\frac{3x}{3} = \frac{8^3 + 18}{3}$$

$$x = (8^3 + 18)/3 = 176.667$$

Example 4

- Solve the equation for x .
- Round the answer to three decimal places.

