

The Multiplication Rule for Counting

Detailed Examples

Introduction

Using the Multiplication Rule for Counting can look difficult at first. The key is to follow the following steps.

1. Determine how many decisions must be made for each step of the problem. Write a slot for each decision.
2. Fill in the number of possibilities for each decision in the corresponding slot. Work on each decision one at a time.
3. Multiply the numbers in each slot. The product is your answer.

These problems can have large numbers for answers.

Examples

Example 7.2

The University Combinatorics Club has 31 members: 8 seniors, 7 juniors, 5 sophomores, and 11 first-years. How many possible 4-person committees can be formed by selecting 1 member from each class?

Step	Work
Write four slots, one each for: seniors, juniors, sophomores, and first-years.	

Seniors Juniors Sophomores First-Years

Fill in the slots: 8 for the seniors, 7 for the juniors, 5 for the sophomores, and 11 for the first-years.

<u>8</u>	<u>7</u>	<u>5</u>	<u>11</u>
Seniors	Juniors	Sophomores	First-Years

$$\begin{array}{ccccccc} \underline{8} & \times & \underline{7} & \times & \underline{5} & \times & \underline{11} \\ \text{Seniors} & & \text{Juniors} & & \text{Sophomores} & & \text{First-Years} \\ & & & & = & & 3,080 \end{array}$$

Example 7.3

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Step

Write six slots: three for the three letters and three for the numbers.

Work

<u>1st</u>	<u>2nd</u>	<u>3rd</u>	<u>1st</u>	<u>2nd</u>	<u>3rd</u>
letter	letter	letter	number	number	number

Fill in the slots. The first three slots are 26, which is the number of letters. The last three slots are 10, which is the number of numbers.

26	26	26	10	10	10
<u>1st</u>	<u>2nd</u>	<u>3rd</u>	<u>1st</u>	<u>2nd</u>	<u>3rd</u>
letter	letter	letter	number	number	number

Multiply the numbers in each slot.

26	x	26	x	26	x	10	x	10	x	10
<u>1st</u>		<u>2nd</u>		<u>3rd</u>		<u>1st</u>		<u>2nd</u>		<u>3rd</u>
letter		letter		letter		number		number		number
$= 17,576,000$										

The number of possible license plates is 17,576,000. For a large state, having this many possibilities is good so you will not run out of plates.