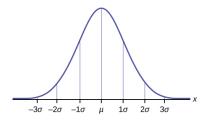
Week 7

Statistics

Normal Distributions

- ► Many data sets follow a **normal distribution**.
- ► The picture to the right shows a distribution function for a normal distribution.
- ► The distribution of the data is determined by the area under the curve of the graph.



Standard Normal Distribution

- ▶ We write $X \sim N(\mu, \sigma)$ to say a random variable X is distributed with a normal distribution with mean μ and stand deviation σ .
- ► The **standard normal distribution** has mean 0 and standard deviation 1.
- We can change any normal distribution to a standard normal distribution using a z-score.

$$z = \frac{x - \mu}{\sigma}$$

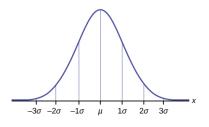
► We can use z-scores to measure standard deviations from the mean

Suppose $X \sim N(-1, 2)$.

- What is the z-score of x = 2?
- ► What is the z-score of x = -13?
- ► What value is 2 standard deviations to the right of the mean?
- ► What value has a z-score of -0.5?

The Empirical Rule

- About 68% of the x values lie between -1σ and $+1\sigma$ of the mean μ .
- About 95% of the x values lie between -2σ and $+2\sigma$ of the mean μ .
- About 99.7% of the x values lie between -3σ and $+3\sigma$ of the mean μ .
- ► Notice that almost all the x values lie within three standard deviations of the mean.



Suppose x has a normal distribution with mean 50 and standard deviation 6. What can we say about the distribution of the data?

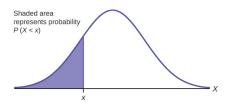
From 1984 to 1985, the mean height of 15 to 18-year-old males from Chile was 172.36 cm, and the standard deviation was 6.34 cm.

- ► About 68% of the values lie between what two values?
- ► About 95% of the values lie between what two values?
- ► About 99.7% of the values lie between what two values?

Using Normal Distributions

If $X \sim N(\mu, \sigma)$:

- ► Calculate P(X < x) by finding the area to the left of x under the bell curve.
- Calculate P(X > x) by finding the area to the right of x under the bell curve.
- Note: P(X > x) = 1 P(X < x).



Calculator Directions

To calculate the probability that a normally distributed random variable is between two values:

- 1. Go to Distr -> 2:normalcdf(.
- 2. Enter: lower bound, upper bound, mean, standard deviation.
- 3. Type ")" and Enter.

Note, use "1 EE 99" for infinite bounds.

The final exam scores in a class were normally distributed with a mean of 63 and a standard deviation of five.

- ► Find the probability that a randomly selected student scored more than 65 on the exam.
- ► Find the probability that a randomly selected student scored less than 85 on the exam.
- ► Find the probability that a randomly selected student scored between 58 and 68.

Inverse Normal Distribution Function

To find the value of x that puts a given area to the left of x, use the invNorm function in the Distr menu.

The final exam scores in a statistics class were normally distributed with a mean of 63 and a standard deviation of five.

- ► Find the 70th percentile for the final exam.
- ► Find the 40th percentile for the final exam.

Suppose that the average number of hours a personal computer is used for entertainment is two hours per day and the standard deviation is half an hour.

- ► Find the probability that a computer is used for entertainment between 1.8 and 2.75 hours per day.
- ► Find the maximum number of hours per day that the bottom quartile of households use a personal computer for entertainment.