## 20220517 Wirtschaftsinformatik FAT2

## May 17, 2022

```
[1]: %matplotlib inline
import matplotlib.pyplot as plt
import seaborn as sns
import numpy as np

[2]: '''Der k-means Algorithmus sucht nach einer vorgegebenen
Anzahl von Clustern innerhalb eines unbeschriteten mehrdimensionalen

→Datensatzes.

Er erreicht durch dies eine "einfache" Vorstellung davon,
wie die optimale Clusterbildung aussieht.

Das Clusterzentrum ist das arythmetische Mittel Aller Punkte die zum Cluster

→gehören.

Jeder Punkt liegt näher an seinem eigenen Clusterzentrum als an anderen

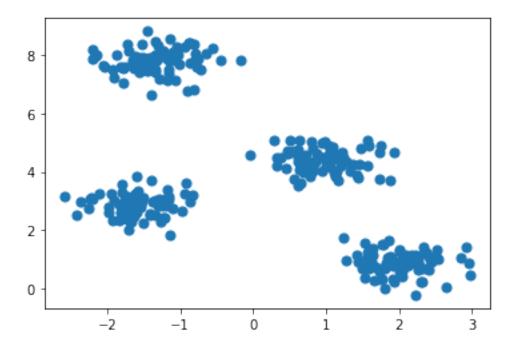
→Clusterzentren.

Diese Beiden Annahmen sind die Grundlage des k-means Clusters Modells.'''
```

[2]: 'Der k-means Algorithmus sucht nach einer vorgegebenen \nAnzahl von Clustern innerhalb eines unbeschriteten mehrdimensionalen Datensatzes.\n\nEr erreicht durch dies eine "einfache" Vorstellung davon, \nwie die optimale Clusterbildung aussieht.\n\nDas Clusterzentrum ist das arythmetische Mittel Aller Punkte die zum Cluster gehören.\n\nJeder Punkt liegt näher an seinem eigenen Clusterzentrum als an anderen Clusterzentren.\n\nDiese Beiden Annahmen sind die Grundlage des k-means Clusters Modells.'

```
plt.scatter(X[:,0], X[:,1], s=50)
```

## [37]: <matplotlib.collections.PathCollection at 0x7fe943751910>



```
[38]: X
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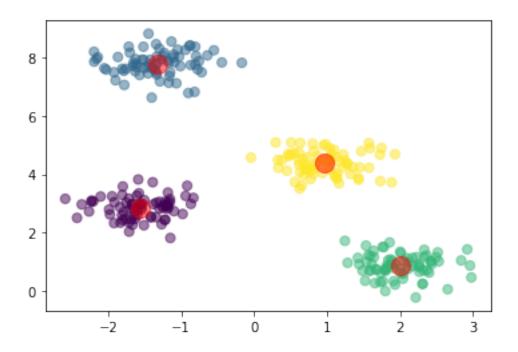
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[39]: X[:,0]

```
[39]: array([ 1.24299373, -1.35852399, 1.09556535, -1.0951628, 1.53265678,
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            -2.02897742, -1.76013144, -2.16370379, -1.97763434, 1.79430409,
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            -1.19025151, -1.3350356, -1.54377259, -1.40211394, 2.01105126,
            -1.80878412, 2.32182075, -1.01230385, 1.81634109, 1.85605454,
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             2.169805 , 2.31132013, 1.22190183, -1.29245154, 0.98047009,
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            -0.64292454, -1.60092548, -1.63399743, 2.3053601, -1.33607219,
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            -2.1440974 , -1.20667809, 1.16253505, -1.58997082, 1.57157096,
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            -2.23431939, 0.62115578, -0.72060102, -1.1685357, 1.74544689,
             0.99457349, -1.34506371, 0.81082249, 1.2807556, -1.24752115,
```

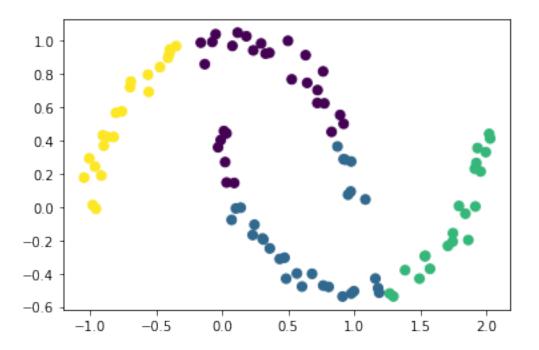
```
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             -1.63245753, -1.53987364, -1.60966548, -1.37857401, -0.90321737,
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             -1.80050837, -0.91890607, 2.03955439, 2.11787014, -1.32941451,
             0.93498254, 0.54796903, -1.9487554, 1.59628006, -0.79681815,
             -1.17931862, 1.32204456, -0.80971704, 0.80220866, 2.09435751,
              1.48564316, -2.20614634, -1.81474577, 1.88417193, 2.9205619,
              1.91366996, 1.56509331, 1.72329366, -1.24480462, -1.65547252,
             2.51620015, 2.42361105, 1.43203035, 2.25276423, 2.16723736,
             2.83763244, -1.45526339, -0.94027253, -1.30067738, 0.93688907,
             2.21488606, 1.89548791, -1.16286376, -1.51946609, -1.26653736,
             2.00088764, 2.36398374, 0.61808345, -0.16976615, -1.70327307])
[40]: y_true
[40]: array([1, 3, 0, 3, 1, 1, 2, 0, 3, 3, 2, 3, 0, 3, 1, 0, 0, 1, 2, 2, 1, 1,
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             3, 3, 0, 1, 3, 2, 2, 0, 1, 1, 0, 2, 3, 1, 3, 1, 0, 1, 1, 0, 3, 0,
             2, 2, 1, 3, 1, 0, 3, 1, 1, 0, 2, 1, 2, 1, 1, 1, 1, 2, 1, 2, 3, 2,
             2, 1, 3, 2, 2, 3, 0, 3, 3, 2, 0, 2, 0, 2, 3, 0, 3, 3, 3, 0, 3, 0,
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             1, 1, 0, 2, 1, 0, 2, 2, 0, 0, 0, 0, 1, 3, 0, 2, 0, 0, 2, 2, 2, 0,
             2, 3, 0, 2, 1, 2, 0, 3, 2, 3, 0, 3, 0, 2, 0, 0, 3, 2, 2, 1, 1, 0,
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             1, 3, 3, 3, 3, 2, 2, 3, 0, 2, 1, 0, 2, 2, 2, 1, 1, 3, 0, 0, 2, 1,
             3, 2, 0, 3, 0, 1, 1, 2, 2, 0, 1, 1, 1, 0, 3, 3, 1, 1, 0, 1, 1, 1,
             3, 2, 3, 0, 1, 1, 3, 3, 3, 1, 1, 0, 3, 2])
[41]: # Lösung 1. Direkt
      from sklearn.cluster import KMeans
      kmeans = KMeans(n clusters=4) # hier sagen wir KMeans wie viele Clusters wir
      \rightarrow haben!
      kmeans.fit(X) # hier lassen wir die Clusters berechnen
      y means = kmeans.predict(X) # hier qeben wir Jedem Punkt einen Label
[42]: plt.scatter(X[:,0], X[:,1], c=y_means, s=50, cmap='viridis', alpha=0.5)
      # hier stellen wir graphisch die Punkte dar.
      # die Farben oder Clusters werden nach den y_labels ausgewählt.
      centers=kmeans.cluster centers
      # hier erzeugen wir eine Variabel welche die Clusterzentren enthält
      plt.scatter(centers[:,0], centers[:,1], c='red', s=200, alpha=0.5)
      # hier stellen wir graphisch die Clusterzentren dar.
```

## [42]: <matplotlib.collections.PathCollection at 0x7fe949863430>



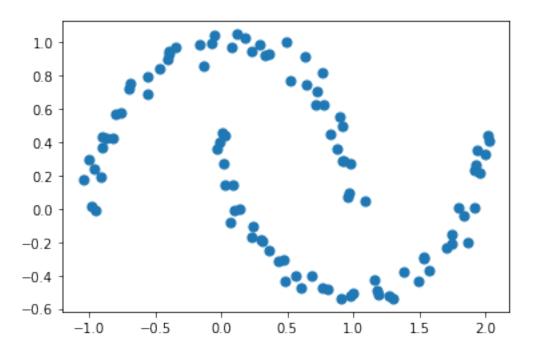
```
[63]: # Lösung 2. Mit Code
      from sklearn.metrics import pairwise_distances_argmin
      def find_clusters(X, n_clusters, rseed=2):
          # 1. Random auswahl von Clusters
          rng = np.random.RandomState(rseed)
          i = rng.permutation(X.shape[0])[:n_clusters]
          centers = X[i]
          while True:
          # 2. Labels werden an den am näshesten Center zugeordnet
              labels = pairwise_distances_argmin(X,centers)
          # 3 Finden Sie neue Zentren aus den Mittelwerten
              new_centers = np.array([X[labels==i].mean(0)
              for i in range(n_clusters)])
          # 4 Konvergenz finden
              if np.all(centers == new_centers):
                  break
              centers = new_centers
          return centers, labels
      centers, labels = find_clusters(X,4)
      plt.scatter(X[:,0], X[:,1], c= labels, s=50, cmap='viridis')
```

[63]: <matplotlib.collections.PathCollection at 0x7fe949f8a460>

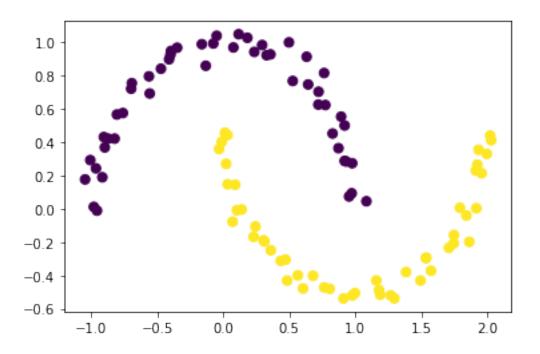


```
[47]: # k-means ist NUR für LINEARE Clustergrenzen beschränkt!
[57]: from sklearn.datasets import make_moons
    X,y = make_moons(100, noise=0.05, random_state=0)
    plt.scatter(X[:,0], X[:,1], s=50, cmap='viridis')
```

[57]: <matplotlib.collections.PathCollection at 0x7fe949da13a0>



[58]: <matplotlib.collections.PathCollection at 0x7fe949ed0f40>



[]: