

HW7 - Lucas Fellmeth, Sven Bergmann

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Chapter 15

Problem 3

Refer to insect waiting times for the female Western White Clematis in Table 10.1. Use the percentile method to find a 90 confidence interval for $F(30)$, the probability that the waiting time is less than or equal to 30 minutes.

Table 10.1

Waiting times for insects to visit flowers.

Male flowers			Female flowers		
1	9	27	1	19	57
1	9	27	2	23	59
2	9	30	4	23	67
2	11	31	4	26	71
4	11	35	5	28	75
4	14	36	6	29	75
5	14	40	7	29	78
5	14	43	7	29	81
6	16	54	8	30	90
6	16	61	8	32	94
6	17	68	8	35	96
7	17	69	9	35	96
7	18	70	14	37	100
8	19	83	15	39	102
8	19	95	18	43	105
8	19	102	18	56	
104					

```
library(survival)
female <- c(1, 2, 4, 4, 5, 6, 7, 7, 8, 8, 8, 9, 14, 15, 18, 18, 19, 23, 23, 26, 28,
  29, 29, 29, 30, 32, 35, 35, 37, 39, 43, 56, 57, 59, 67, 71, 75, 75, 78, 81, 90,
  94, 96, 96, 100, 102, 105)
female.event <- c(rep(1, 32), 1, 1, 1, 1, 1, 0, 0, 1, 0, 0, 1, 0, 0, 0, 0)

T_i <- replicate(10000, {
  idx_boot <- sample(seq_along(female), size = length(female), replace = T)
  x_boot <- female[idx_boot]
  female.event.boot <- female.event[idx_boot]
```

```

k mest <- (1 - survfit(Surv(x_boot, event = female.event.boot, type = "right") ~
1, type = "kaplan-meier")$surv)
k mest[sum(30 >= x_boot)]
})
quantile(T_i, probs = c(0.05, 0.95), na.rm = T)

```

```

##          5%          95%
## 0.6595745 0.9109549

```

Problem 7

Seven patients each underwent three different methods of kidney dialysis. The following values were obtained for weight change in kilograms between dialysis sessions:

Patient	Treatment 1	Treatment 2	Treatment 3
1	2.90	2.97	2.67
2	2.56	2.45	2.62
3	2.88	2.76	1.84
4	2.73	2.20	2.33
5	2.50	2.16	1.27
6	3.18	2.89	2.39
7	2.83	2.87	2.39

Test the null hypothesis that there is no difference in mean weight change among treatments. Use properly designed permutation test.

```

x <- c(2.9, 2.56, 2.88, 2.73, 2.5, 3.18, 2.83)
y <- c(2.97, 2.45, 2.76, 2.2, 2.16, 2.89, 2.87)
z <- c(2.67, 2.62, 1.84, 2.33, 1.27, 2.39, 2.39)
T_obs <- mean(x) - mean(y) + mean(x) - mean(z)
T_obs

```

```
## [1] 0.7642857
```

```

n1 <- length(x)
n2 <- length(y)
n3 <- length(z)
T_perm <- replicate(10000, {
  z_perm <- sample(c(x, y, z), size = n1 + n2 + n3, replace = F)
  x_perm <- z_perm[1:n1]
  y_perm <- z_perm[(n1 + 1):(n1 + n2)]
  z_perm <- z_perm[(n1 + n2 + 1):(n1 + n2 + n3)]
  mean(x_perm) - mean(y_perm) + mean(x_perm) - mean(z_perm)
})
mean(T_perm > T_obs)

```

```
## [1] 0.0151
```

We reject H_0 since the p -value is very small.

Problem 10

Return to Example 7.5 in which tread wear for tires is measured using weight loss and groove wear. Construct a randomization test to compute the significance of the Pearson correlation coefficient. How does this value compare with the p -value in the R function `cor.test`?

Example 7.5

Stichler, Richey, and Mandel (1953) list tread wear for tires (see table below), each tire measured by two methods based on (i) weight loss and (ii) groove wear. In R, the function `cor(x,y,method="spearman")` computes the Spearman coefficient. For this example, $\hat{\rho} = 0.9265$. Note that if we opt for the parametric measure of correlation, the Pearson coefficient is 0.948:

Weight	Groove	Weight	Groove
45.9	35.7	41.9	39.2
37.5	31.1	33.4	28.1
31.0	24.0	30.5	28.7
30.9	25.9	31.9	23.3
30.4	23.1	27.3	23.7
20.4	20.9	24.5	16.1
20.9	19.9	18.9	15.2
13.7	11.5	11.4	11.2

```
weight <- c(45.9, 37.5, 31, 30.9, 30.4, 20.4, 20.9, 13.7, 41.9, 33.4, 30.5, 31.9,
            27.3, 24.5, 18.9, 11.4)

groove <- c(35.7, 31.1, 24, 25.9, 23.1, 20.9, 19.9, 11.5, 39.2, 28.1, 28.7, 23.3,
            23.7, 16.1, 15.2, 11.2)

T_obs <- cor(weight, groove)

T_i <- replicate(10000, {
  X <- weight
  Y <- sample(groove, length(groove), replace = FALSE)
  cor(X, Y)
})

p_value <- mean(T_i > T_obs)

p_value_of_r_test <- cor.test(x = weight, y = groove)$p.value

cat("Difference between our p_value", p_value, "and the p_value from the test in R",
    p_value_of_r_test, ":", abs(p_value - p_value_of_r_test))
```

```
## Difference between our p_value 0 and the p_value from the test in R 2.459998e-08 : 2.459998e-08
```