

## HW 6

**Problem 1 (8.31)** Anne spins a (fair) coin three times and observes no heads. She gives the coin to Noha who decides to spin the coin until a heads occurs. Noha spins the coin a total of four times. Let  $\theta$  be the probability the coin comes up heads.

- (a) What is the likelihood of  $\theta$ ?
- (b) What is the MLE for  $\theta$ ?

**Problem 2 (8.52)** Let  $X_1, \dots, X_n$  be IID RVs with density

$$f(x; \theta) = (\theta + 1)x^\theta \mathbb{I}\{0 \leq x \leq 1\}.$$

Find the method of moments estimate of  $\theta$ .

**Problem 3 (8.52)** As in the previous problem, let  $X_1, \dots, X_n$  be IID RVs with density

$$f(x; \theta) = (\theta + 1)x^\theta \mathbb{I}\{0 \leq x \leq 1\}.$$

Find the maximum likelihood estimate of  $\theta$ .