

Resolución Examen Ingreso 1-2018 2<sup>a</sup> opción  
ARITMÉTICA-ÁLGEBRA

UMSS-FCYT Fila 1

A<sub>1</sub>.  $4x^2 + (-2m-5)x + (m-1) = 0$  y  $\frac{x_2 + x_1}{x_1 x_2} = \frac{3}{5}$  (1)

$\Rightarrow a=4; b=-2m-5; c=m-1$  y  $x_1 + x_2 = -\frac{b}{a} = \frac{2m+5}{4}$  (2)

Reemplazando (2) en (1) tenemos:  $x_1 x_2 = \frac{c}{a} = \frac{m-1}{4}$

$\frac{2m+5}{m-1} = \frac{3}{5} \Rightarrow 10m+25 = 3m-3$   
 $7m = -28$

$m = -4$

A<sub>2</sub>.  $a, b, c$  en P. G.  $\Rightarrow b = ax$  y  $c = ax^2$   
con  $a > 0$  y  $x > 0$

$\Rightarrow \log a, \log b, \log c$  satisfacen:  $\log a, \log(ax), \log(ax^2)$

$\Rightarrow \underbrace{\log a}_u, \underbrace{\log a + \log x}_{u+d}, \underbrace{\log a + 2\log x}_{u+2d}$  están en P. A  
y  $d = \log x$

A<sub>3</sub>.  $\sqrt[n]{\frac{20^n \cdot 20}{4^n \cdot 4^2 + 4^{n+1}}} = \sqrt[n]{\frac{4^n \cdot 5^n \cdot 20}{4^n \cdot 16 + 4^n \cdot 4}} = \sqrt[n]{\frac{4^n \cdot 5^n \cdot 20}{4^n \cdot (20)}} = \sqrt[n]{5^n} = 5$

A<sub>4</sub>.  $\begin{cases} \frac{(x+y)}{2} - \frac{xy}{2(x-y)} = \frac{(2+x)}{2} - \frac{(y^2-x)}{2(x-y)} \Rightarrow \cancel{x^2} - \cancel{y^2} - \cancel{xy} = 2x - 2y + \cancel{x^2} - \cancel{xy} - y^2 + x \\ 2y = 3x \Rightarrow y = \frac{3x}{2} \quad (1) \\ yx + x - 1 = (y+2)(x-1) \Rightarrow \cancel{xy} + x - 1 = \cancel{xy} - y + 2x - 2 \\ \Rightarrow y = x - 1 \quad (2) \end{cases}$

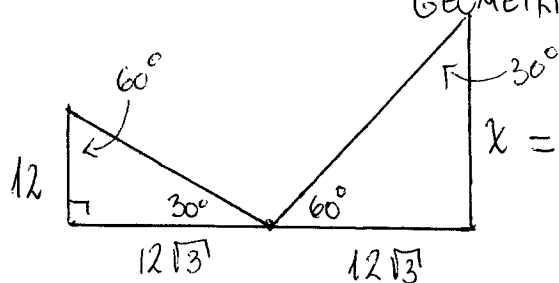
(2) en (1):  $2(x-1) = 3x$

$2x - 2 = 3x \Rightarrow -2 = x \Rightarrow$  En (1):  $y = -3$

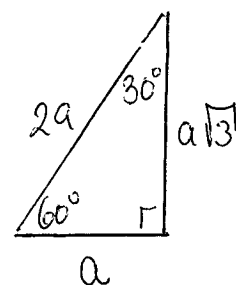
$\Rightarrow x + y = -2 - 3 = -5$

GEOMETRÍA TRIGONOMETRÍA

6.5



$$x = (12\sqrt{3})\sqrt{3} = 12 \cdot 3 = \underline{36}$$



6.6

$$\cos 4x + \cos 2x = \cos x$$

$$2 \cos\left(\frac{4x+2x}{2}\right) \cos\left(\frac{4x-2x}{2}\right) = \cos x$$

$$2 \cos 3x \cos x - \cos x = 0$$

$$\Rightarrow \underline{x = 20^\circ}$$

$$\cos x (2 \cos 3x - 1) = 0$$

$$\cos x = 0$$

$$x = 90^\circ \pm k360$$

$$x = 270^\circ \pm k360$$

$$\cos 3x = \frac{1}{2}$$

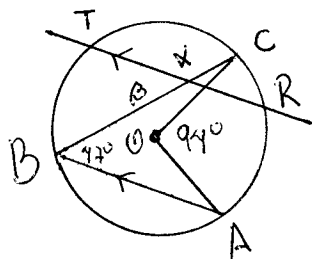
$$3x = 60^\circ \pm k360$$

$$\Rightarrow x = 20^\circ \pm k120$$

$$3x = 300^\circ \pm k360$$

$$\Rightarrow x = 100^\circ \pm k120$$

6.7



$$\angle AOC = 94^\circ \text{ (}\angle \text{ central)}$$

$$\angle CBA = \frac{94^\circ}{2} = 47^\circ \text{ (}\angle \text{ inscribed)}$$

$$\hat{\beta} = 47^\circ \text{ (alternos internos)}$$

$$\alpha + \beta = 180^\circ \text{ (Suplem.)}$$

$$\alpha = 180^\circ - 47^\circ$$

$$\underline{\alpha = 133^\circ}$$

6.8

$$\sin \theta = \frac{4}{5} \text{ y } \theta \in \text{II}^\circ \Rightarrow y = 4, x = 5; x^2 + y^2 = r^2 \Rightarrow x = \pm 3 = -3$$

$$\text{uego: } Z = \frac{\tan\left(\frac{6\pi}{2} - \theta\right) + \tan \theta}{\cos\left(\frac{3\pi}{2} - \theta\right) \cdot \tan(\theta)} = \frac{(-\tan \theta) + \tan \theta}{(-\sin \theta) \cdot \tan \theta} = \frac{-\left(-\frac{4}{3}\right) + \frac{4}{5}}{-\left(\frac{4}{5}\right) \cdot \left(-\frac{4}{3}\right)}$$

$$Z = \frac{\frac{4}{3} + \frac{4}{5}}{+\frac{4}{5} \cdot \frac{4}{3}} = \frac{\frac{32}{15}}{\frac{16}{15}} = \underline{2}$$

# Exercice 1

Exercice 9 1<sup>er</sup> tramo

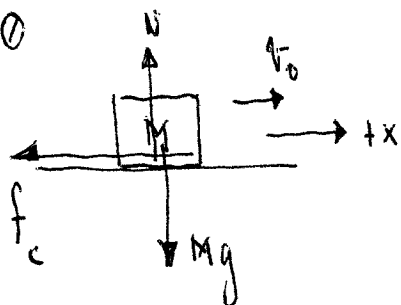
$$a = \frac{\Delta v}{\Delta t} = \frac{8}{4} = 2 \text{ [m/s}^2\text{]} \rightarrow x_1 = \frac{1}{2} a t^2 = 16 \text{ [m]}$$

2<sup>do</sup> tramo

$$v = 8 \text{ [m/s]} \rightarrow x_2 = 8(10-4) = 48 \text{ [m]}$$

$$\Rightarrow D = 16 + 48 = 64 \text{ [m]} \quad \textcircled{a}$$

Exercice 10



$$y: N - Mg = 0 \rightarrow N = Mg$$

$$x: -\mu_c N = Ma$$

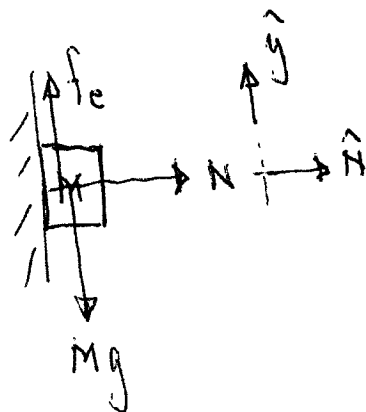
$$\hookrightarrow a = -\mu_c g$$

$$v^2 = v_0^2 + 2a\Delta x$$

$$0 = 5^2 + 2(-\mu_c g)\Delta x$$

$$\hookrightarrow \Delta x = \frac{25}{2(0,1)(10)} = 12,5 \text{ [m]} \quad \textcircled{d}$$

Exercice 11

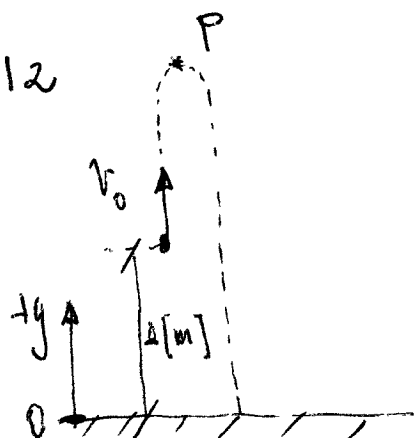


$$\hat{y}: \mu_e N - Mg = 0 \Rightarrow \mu_e \frac{Mv^2}{r} = Mg$$

$$\hat{x}: N = M \frac{v^2}{r}$$

$$v = \sqrt{\frac{rg}{\mu_e}} = \sqrt{\frac{20(10)}{\frac{1}{2}}} = 20 \text{ [m/s]} \quad \textcircled{a}$$

Exercice 12



$$y = 1 + 10t - \frac{g}{2}t^2$$

$$v = 10 - gt$$

$$\text{En P } v = 0$$

$$0 = 10 - gt_p \rightarrow t_p = 1 \text{ [s]}$$

$$y_p = 1 + 10(1) - \frac{10}{2}(1)^2 = 6 \text{ [m]}$$

$$\Rightarrow D = 5 + 6 = 11 \text{ [m]} \quad \textcircled{d}$$

ResoluciónNº 1

Q 13 ¿ Cuantos gramos de metano ( $\text{CH}_4$ ) contendrán  $12,044 \times 10^{23}$  moléculas de  $\text{CH}_4$  (masa molar =  $16 \text{ g/mol}$ )

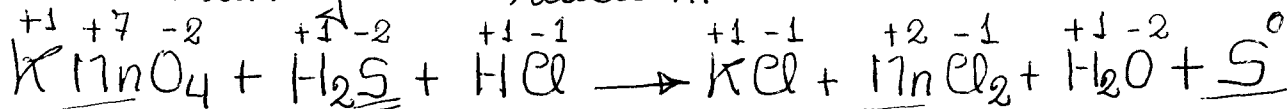
Datos

$$m_{\text{CH}_4} = ?$$

$$12,044 \times 10^{23} \text{ moléculas CH}_4 \times \frac{1 \text{ mol de CH}_4}{6,022 \times 10^{23} \text{ moléculas CH}_4} \times \frac{16 \text{ g de CH}_4}{1 \text{ mol CH}_4} = 32 \text{ g de CH}_4$$

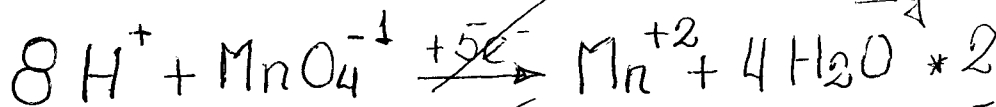
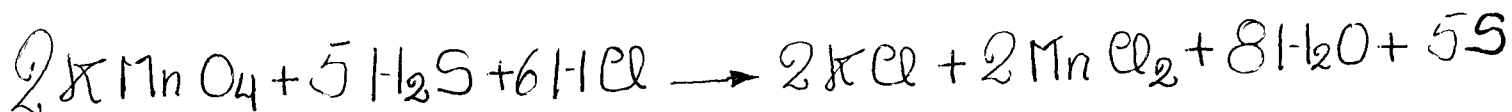
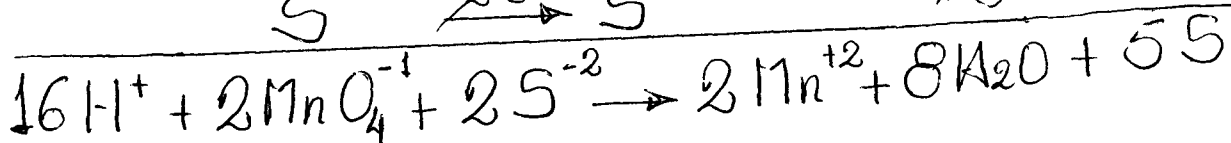
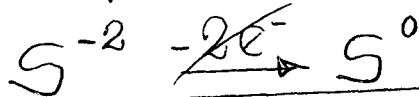
Respuesta A) 32 //

Q. 14 Considere la siguiente reacción:



Una vez igualada la ecuación, el coeficiente que acompaña al  $\text{HCl}$  es?

Semiecuaciones:

Igualar atómicamente  
electrónicamente

R	P
K: 2	2 ✓
Mn: 2	2 ✓
Cl: 6	6 ✓
S: 5	5 ✓
H: 16	16 ✓
O: 8	8 ✓

Rpta: 6

B) 6 //

Q 15. 64 g de un gas ocupan 200L a  $-73^{\circ}\text{C}$  y 124,8 torr ¿Cuál es la masa molecular del gas? ( $R = 62,4 \text{ torrL/molK}$ )

Datos:  $m = 64 \text{ g}$

$V = 200 \text{ L}$

$T = -73 + 273$

$P = 124,8 \text{ torr}$

$PV = nRT$

$$n = \frac{124,8 \text{ torr} \times 200 \text{ L}}{62,4 \text{ torrL/molK} \times 200 \text{ K}}$$

$n = 2 \text{ moles de gas}$  como  $n = \frac{m}{M}$

despejamos  $M = ?$

$M = \frac{64}{2} = \underline{\underline{32}} \text{ Rpta C) } \underline{\underline{32}}$

Q.16 c) ¿Que molaridad tiene una solución al 8,0% de NaOH?  
La densidad de la solución es de 1,028 g/mL

Datos:

Solución al 8,0% NaOH

$P = 1.028 \text{ g/mL}$

100g de solución = 8,0g de NaOH

$$1,028 \frac{\text{g de solución}}{\text{mL de solución}} \times \frac{8,0 \text{ g de NaOH}}{100 \text{ g de solución}} \times \frac{1 \text{ mol de NaOH}}{40 \text{ g de NaOH}} \times \frac{1000 \text{ mL de solución}}{1 \text{ L de solución}}$$

$M = 2,056 //$

Rpta: D) 2,056 //