

CIS501 – Lecture 15

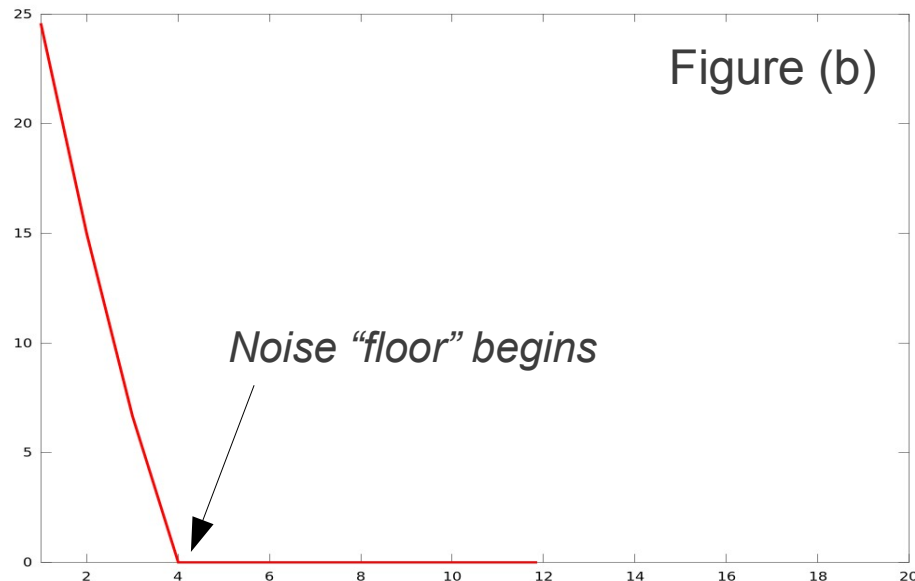
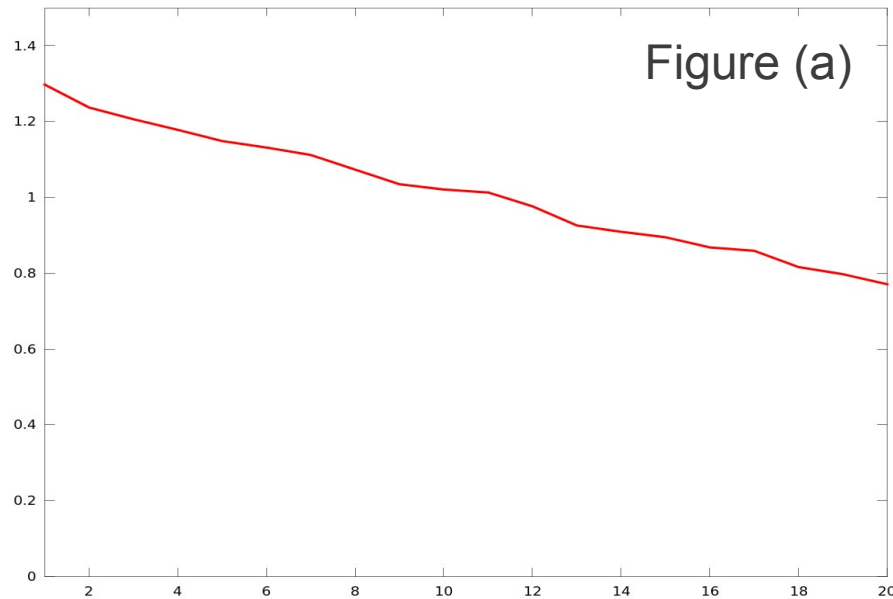
Woon Wei Lee

Fall 2013, 10:00-11:15pm,
Sundays and Wednesdays

For today:

- Self-Organizing maps
- Unsupervised learning wrap-up
- Presentations
 - Azhar Ahmed
 - Khawla Masood Al Dhaheri

PCA (Cont'd)



i.e. The principle components are given by the **eigenvectors** of the covariance matrices

- For an n -dimensional dataset, there will be n such eigenvectors.
- Eigenvectors are mutually orthonormal
- Matrix of eigenvectors is hence a *rotation matrix*

Project upon a subset of these eigenvectors
→ **dimensionality reduction**

- The λ value → the eigenvalues of the covariance matrix
- Sorting these and plotting gives the *singular spectrum (SS)*

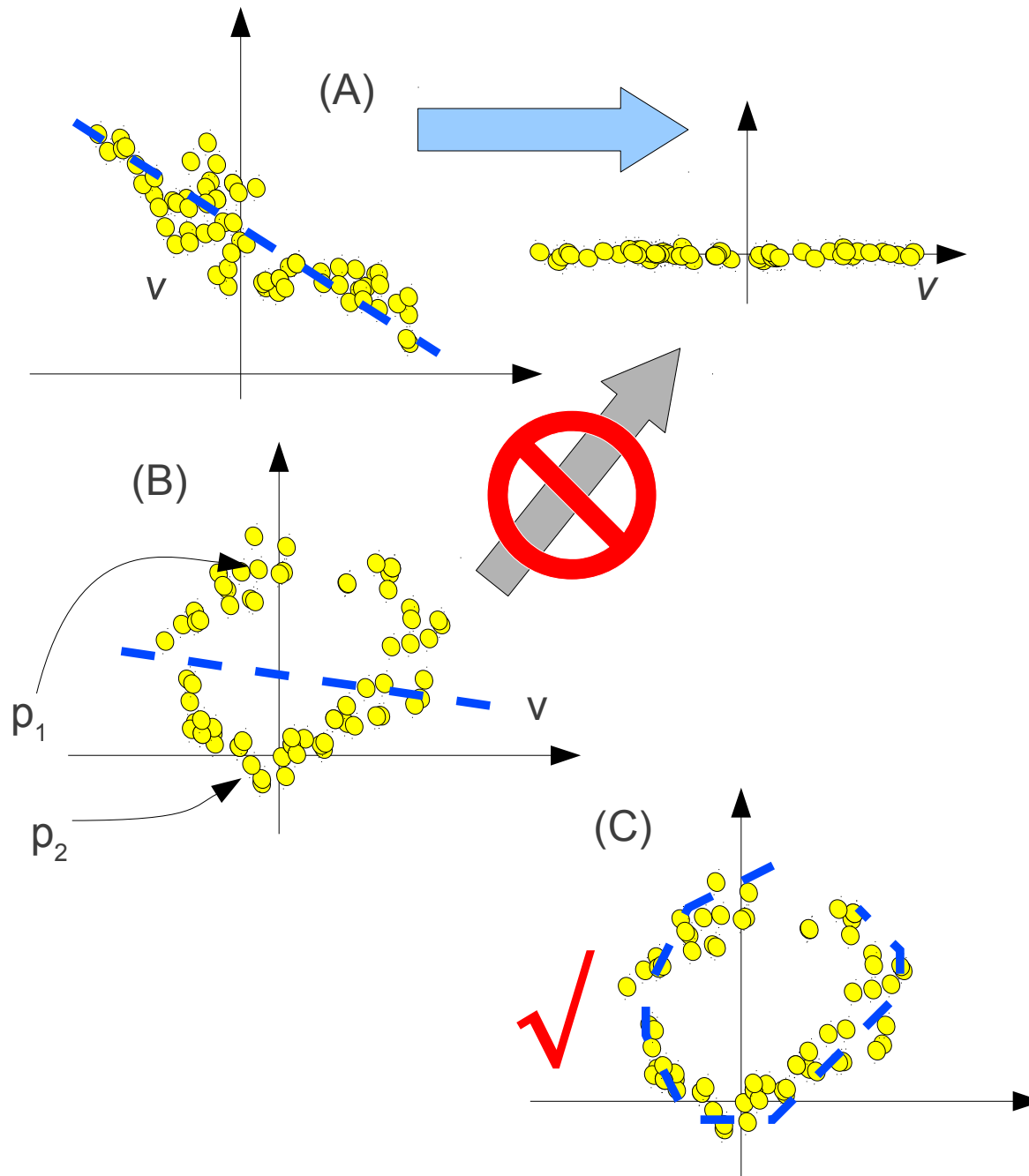
Figures (a) and (b):

(a) SS corresponding to 20 dimensional white noise

(b) SS for 3 dimensional white noise embedded in 20 dimensional space

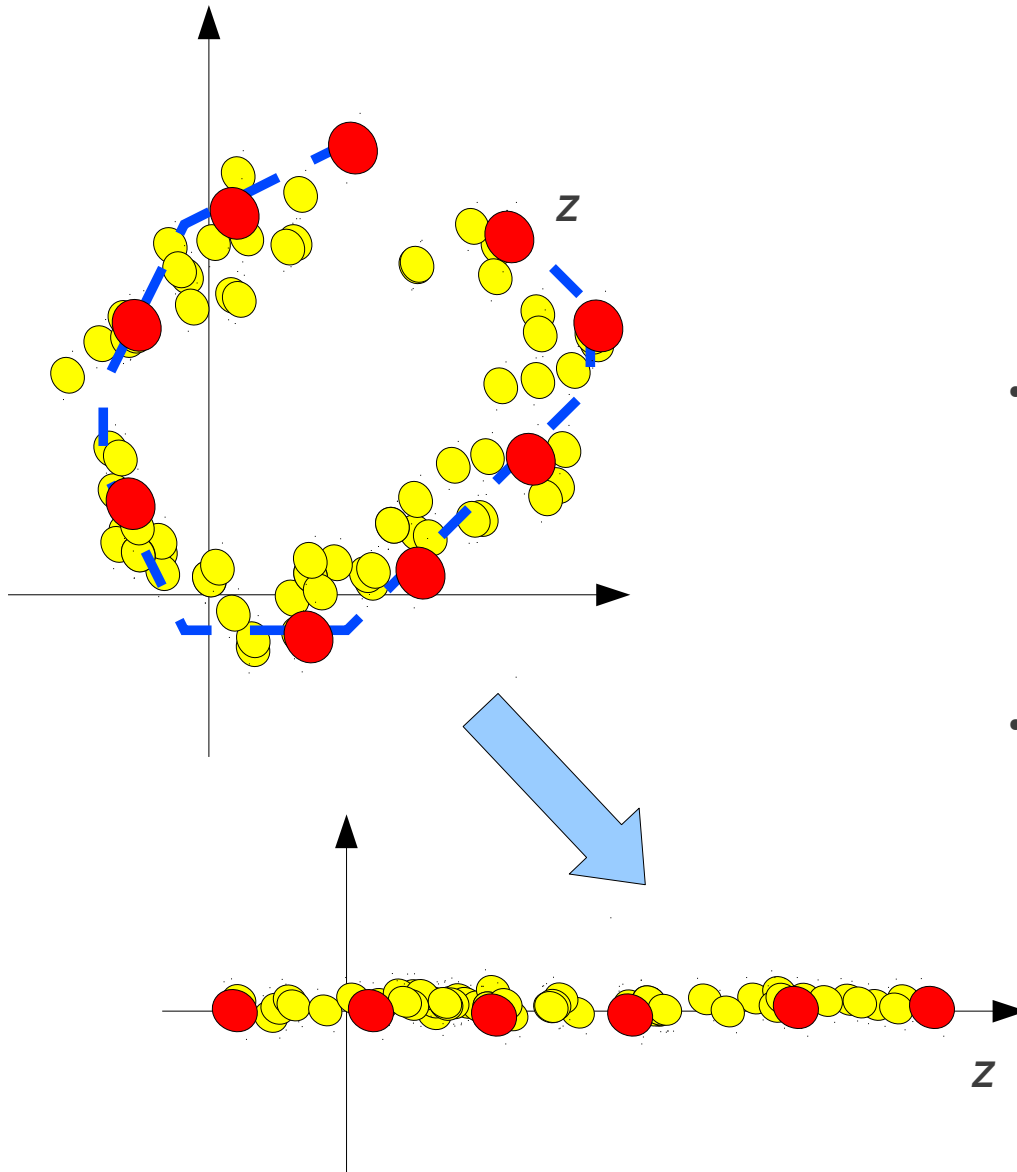
- Note the noise "floor" in figure (b).

Linear vs Non-linear



- **Linear techniques like PCA project data onto *hyper-plane***
 - Works well when data contains linear relationships
 - (e.g. (A) → two dimensional case, relationship written:
 $y=mx+c$ (+noise)
- **Alternative: *nonlinear* structure/data**
 - (B) is an example
 - Linear projections → weird things can happen
 - For e.g., if projected onto v , p_1 and p_2 will look around the same
- **Solution:**
 - Use nonlinear axes! (C)

Kohonen's self-organizing map



- **How can we create this nonlinear mapping?**
 - Use nonlinear mapping function → difficult!
 - Create a virtual axis of points (on left)
- **This is the principle of the “self-organizing-map” or SOM**
 - Objective: learn nonlinear axis “z”
 - Unfold to form a traditional visualization surface
- **Strategy**
 - Embed a string of markers or nodes along the axes
 - Optimize position of nodes so that each approximates position of nearby points
 - Projection: points attached to closest node

SOM learning algorithm

- **Two main concepts:**

- Perform *clustering* to fix location of each node
- Concept of a *neighborhood* so that topological relationships preserved

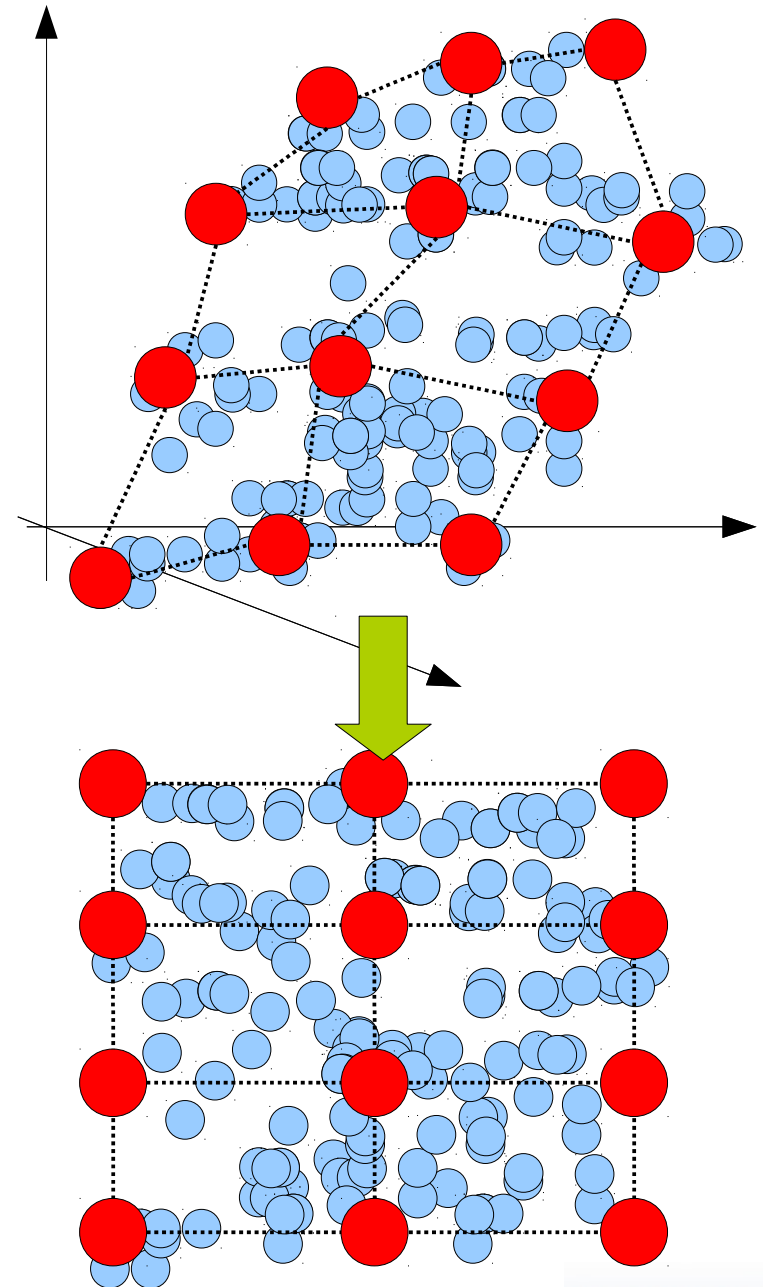
- **Algorithm:**

- (1) Initialize position of the node
- (2) Cycle through the input vectors
- (3) Determine similarity between the input vector and each of the node
- (4) Identify the node that produces the smallest distance.
- (5) Update the position of *all* nodes as follows:
$$\mathbf{v}^{(t+1)} = \mathbf{v}^{(t)} + \eta^{(t)} \Theta^{(t)} (\mathbf{x}^{(t)} - \mathbf{v}^{(t)})$$
- (6) Repeat from 2

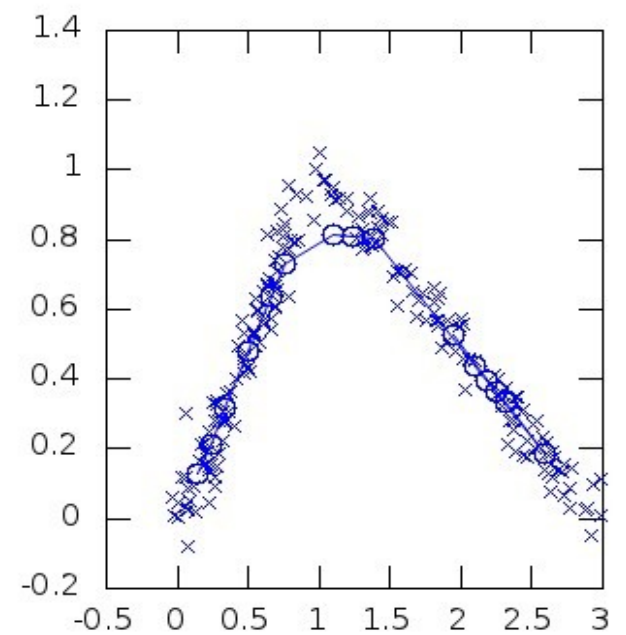
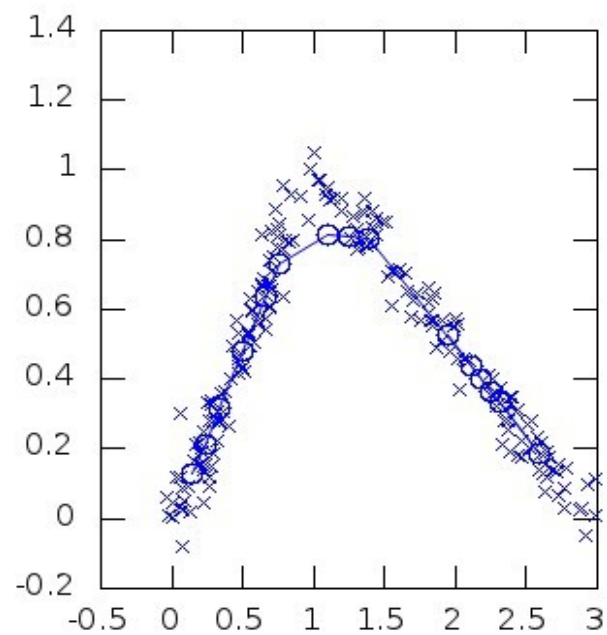
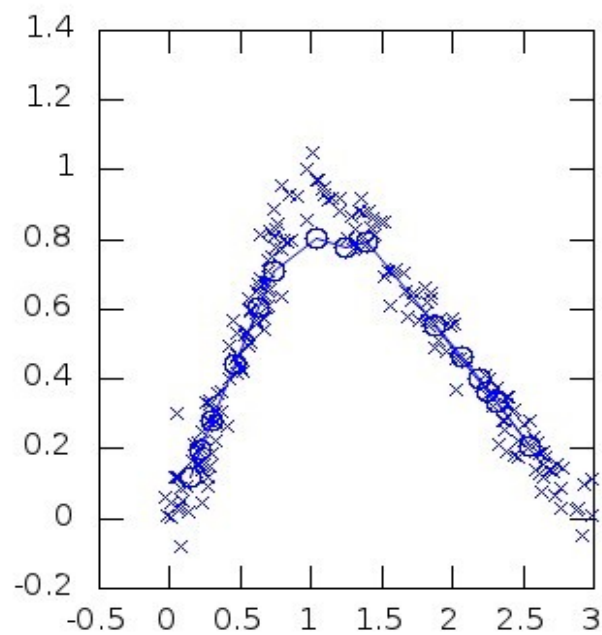
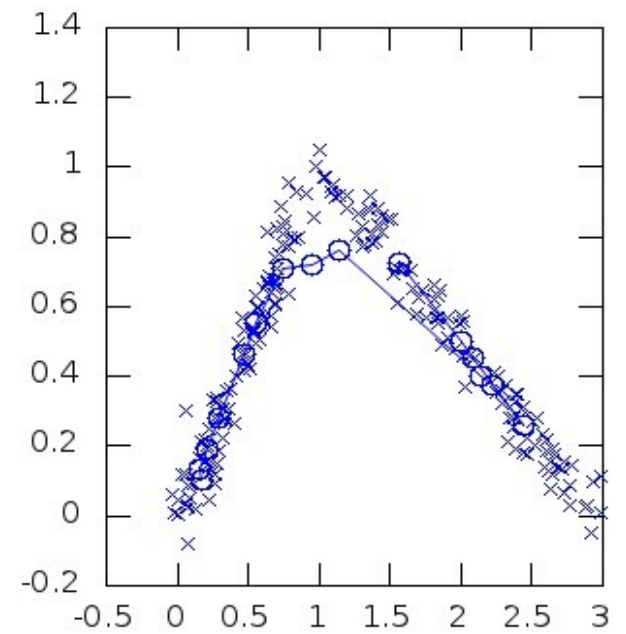
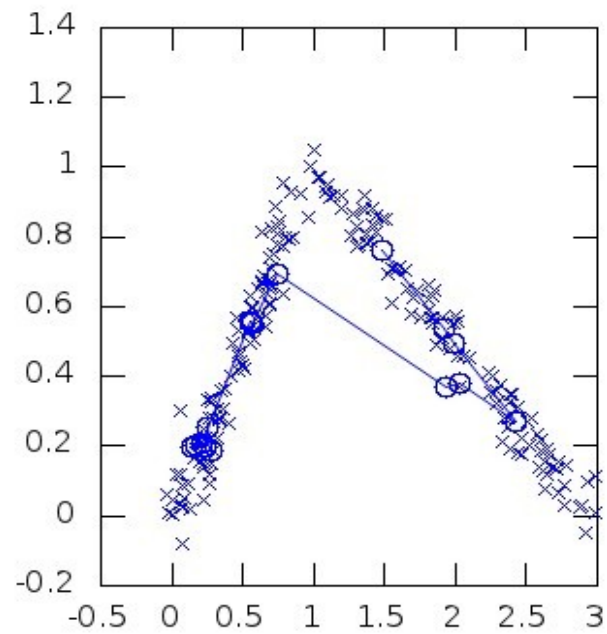
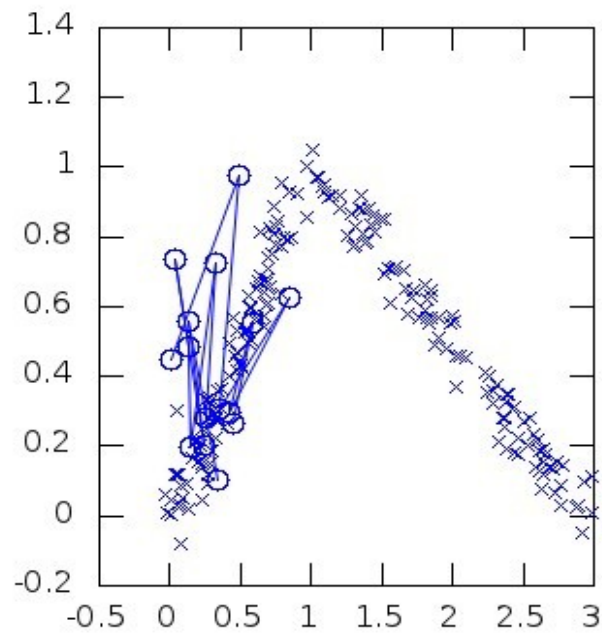
- $\mathbf{v}^{(t)}$ – position of the node at time t
- $\eta^{(t)}$ – Learning rate (time dependent)
- $\Theta^{(t)}$ – Neighborhood function
- $\mathbf{x}^{(t)}$ – Input vector selected at time t

(Cont'd)

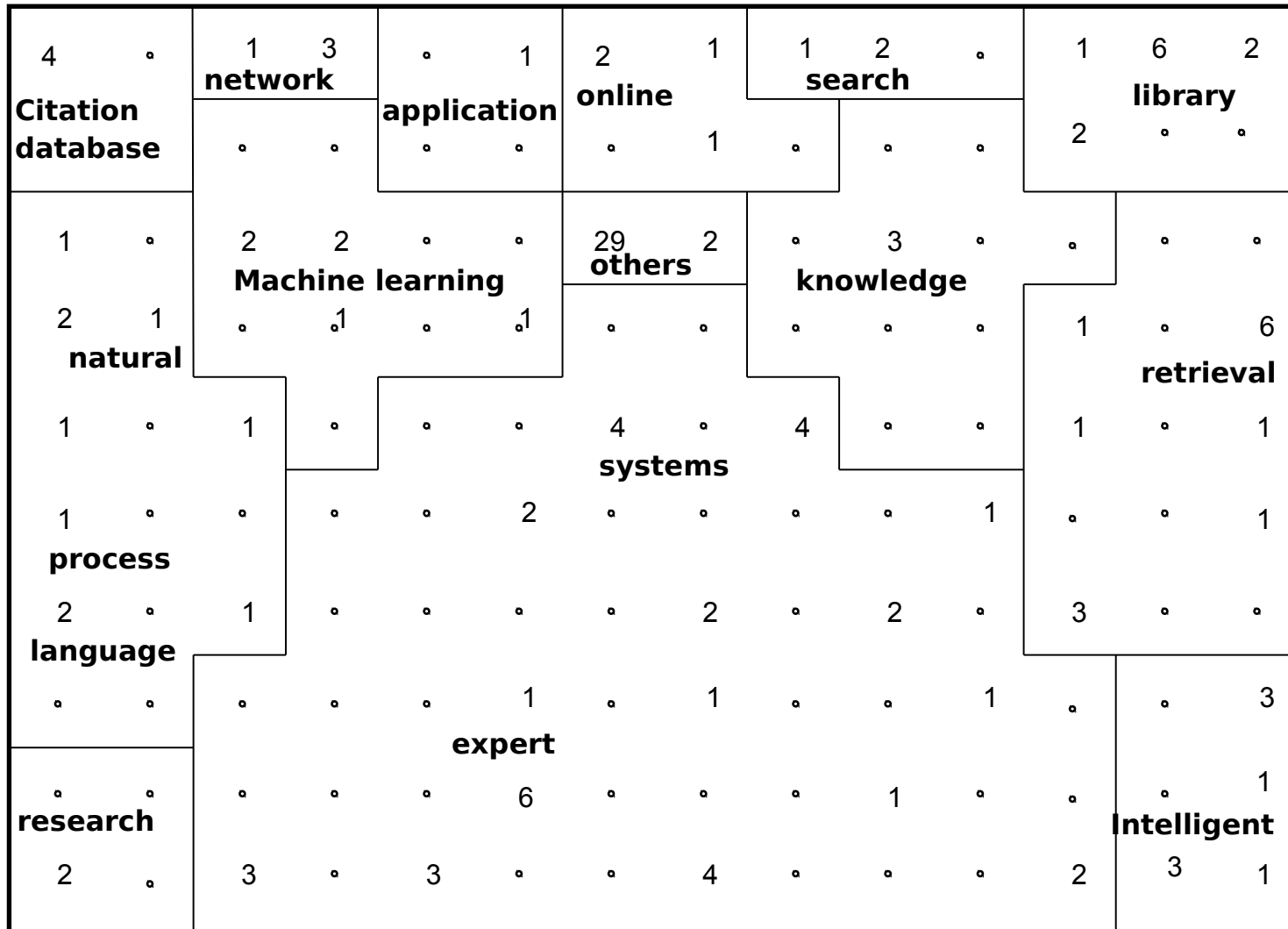
- **Additional notes:**
 - The learning rate $\eta^{(t)}$ and neighborhood function $\Theta^{(t)}$ are shown to be time dependent
 - $\eta^{(t)}$ decreases monotonically as training progresses, while $\Theta^{(t)}$ also reduces in size
 - This allows the nodes to
 - First learn the overall topological structure of the data
 - Smaller values allow “fine-tuning” so that nodes match the data distribution
 - SOMs can be built with any number of dimensions
 - BUT typically 2, which is the most practical and useful
 - Hence, the map in “Self-Organizing-*Map*”



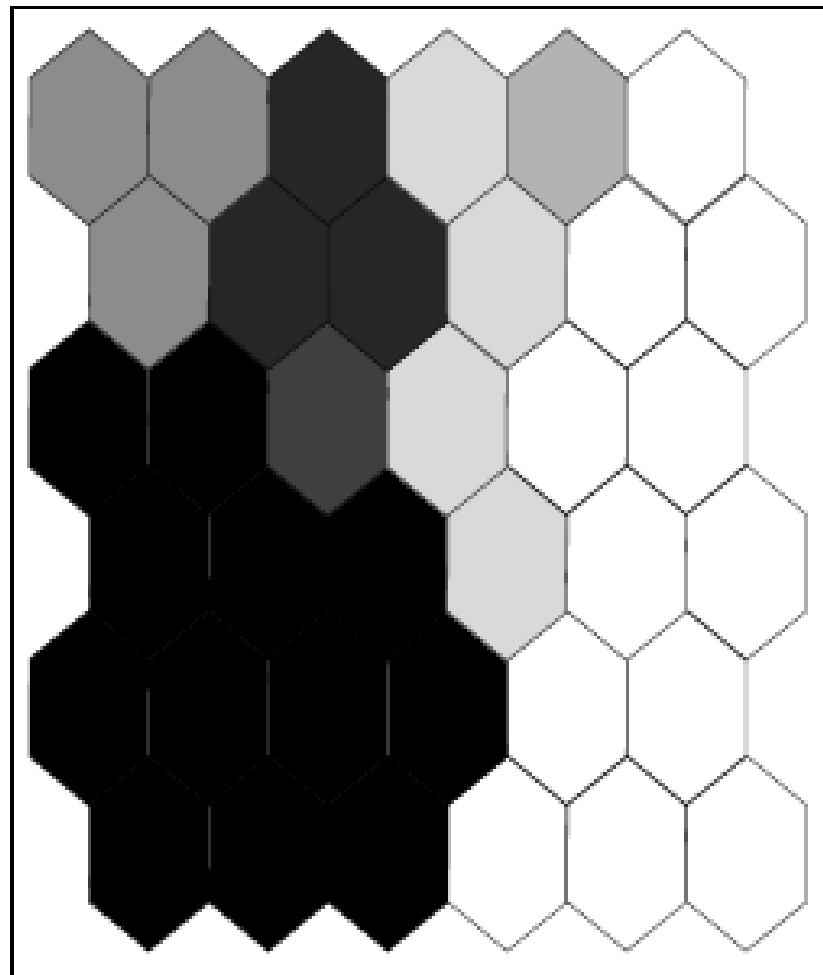
Simple demonstration



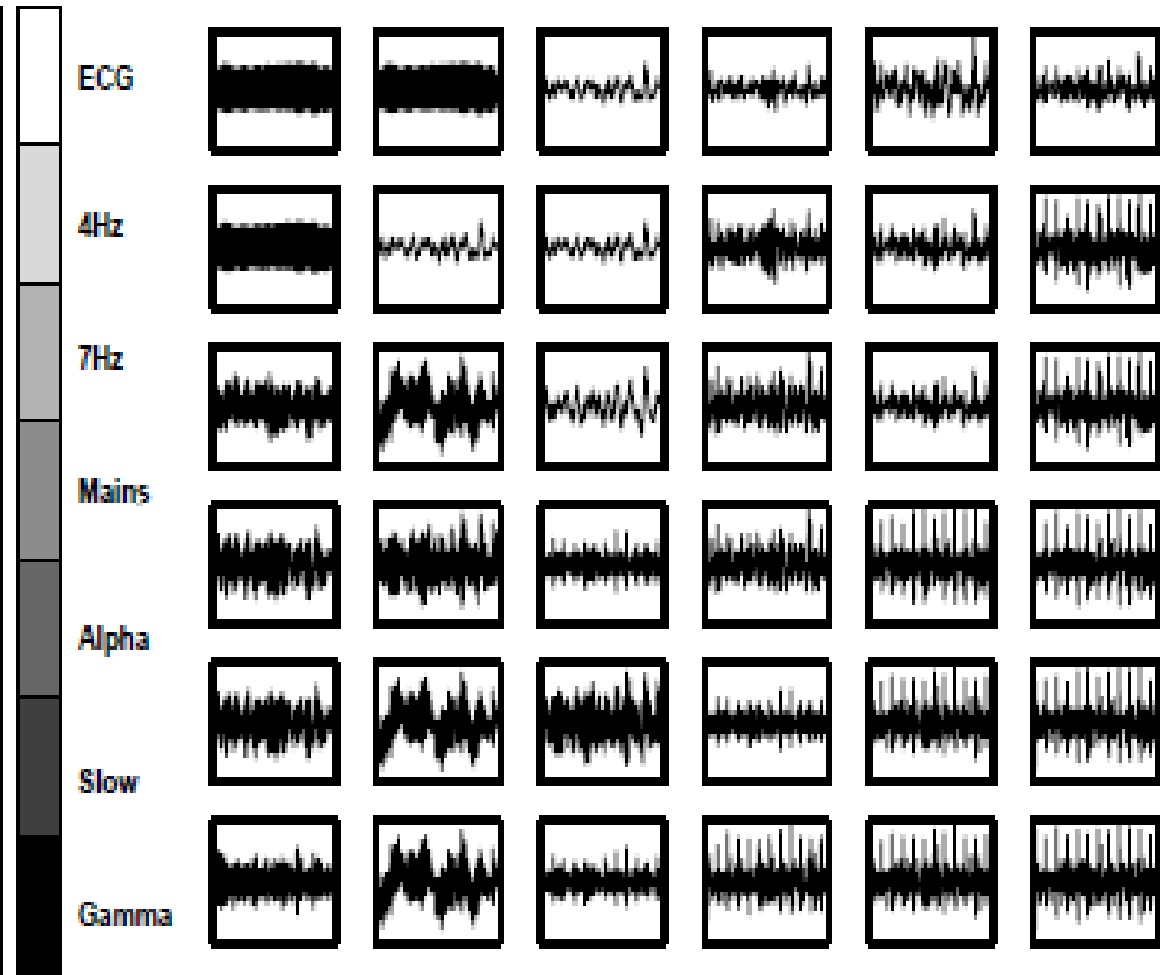
Visualization example: map of 140 A.I. Documents



Visualization example: Brain Signals



(a) Class assignments



(b) ICs corresponding to the SOM lattice neurons

Unsupervised learning: Round-up

- **Time was tight, but we covered two main concepts:**
 1. Clustering:
 - Partitional clustering → k -means and k -centroidS
 - Hierarchical clustering → methods UPGMA and the “Saitou-Nei” method
 2. Visualization
 - Linear (PCA)
 - Non-linear (SOM)
- **Compared to supervised algorithms, unsupervised algorithms tend to be exploratory**
 - Descriptive in nature rather than prescriptive
 - Often richer probabilistic interpretations than supervised learning

(not possible to cover in this introductory course)