CIS 606 Machine Learning

Lecture 14

AdaBoost

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Original Scoure:

 $http://informatik.unibas.ch/lehre/ws05/cs232/_Folien/08_AdaBoost.pdf$

AdaBoost

Slides modified from: MLSS'03: Gunnar Rätsch, Introduction to Boosting

http://www.boosting.org

AdaBoost: Agenda

• Idea AdaBoost (Adaptive Boosting, R. Scharpire, Y. Freund, ICML, 1996):

- Combine many low-accuracy classifiers (weak learners) to create a high-accuracy classifier (strong learners)

AdaBoost: Introduction

• Example: 2 classes of apples











The World:

+1

 $\{(\underline{x}_n, y_n)\}_{n=1}^N, \quad \underline{x}_n \in \mathbb{R}^d, \quad y_n \in \{\pm 1\}$ Data:

 $y = f(\underline{x}) (or \ y \sim P(y \mid \underline{x}))$ Unknown target function:

Unknown distribution: $\underline{x} \sim p(\underline{x})$

Objective: Given new \underline{x} , predict y

Problem: $P(\underline{x}, y)$ is unknown!

AdaBoost: Introduction

The Model:

• Hypothesis class: $\mathcal{H} = \left\{ h \mid h : \mathbb{R}^d \to \{\pm 1\} \right\}$

• Loss: $l(y, h(\underline{x}))$ (e.g. $\mathbf{I}[y \neq h(\underline{x})]$)

• Objective: Minimize the true (expected) loss – ("generalization error")

 $h^* = \min_{h \in \mathcal{H}} L(h)$ with $L(h) := \mathbf{E}_{\mathbb{X} \times \mathbb{Y}} l(\mathbb{Y}, h(\mathbb{X}))$

• Problem: Only a data sample is available, $P(\underline{x}, y)$ is unknown!

• Solution: Find empirical minimizer $\hat{h}_N = \min_{h \in \mathcal{H}} \frac{1}{N} \sum_{n=1}^N l(y_n, h(\underline{x}_n))$

How can we efficiently construct complex hypotheses with small generalization errors?

AdaBoost: Frame work

Algorithm

- Simple Hypotheses are not perfect!
- Hypotheses combination → increased accuracy

- · How to generate different hypotheses?
- · How to combine them?

Method:



- Compute distribution d_1,\ldots,d_N on examples Find hypothesis on the weighted training sample $(\underline{x}_1, y_1, d_1), \ldots, (\underline{x}_N, y_N, d_N)$
- Combine hypotheses h_1, h_2, \dots linearly:

$$f = \sum_{t=1}^{T} \alpha_t h_t$$

AdaBoost: Frame work

Input: N examples $\{(\underline{x}_l, y_l), \ldots, (\underline{x}_N, y_N)\},\$

L a learning algorithm generating hypothesis $h_i(\underline{x})$ (classifiers)

T maxNumber of hypotheses in the ensemble

Initialize: d_n weigth of example n (\underline{d} is a distribution with $1 = \sum_{n=1}^{N} d_n^{(t)}$)

 $d_n^{(1)} = 1/N$ for all n = 1, ..., N

Do for t = 1, ..., T,

1. Train base learner according to example distribution $\underline{d}^{(t)}$ and obtain hypothesis $h_i: x \mapsto \{\pm 1\}.$

 $\varepsilon_t = \sum_{n=1}^N d_n^{(t)} \ \mathbf{I}(y_n \neq \frac{\mathbf{h}_t(\mathbf{x}_n)}{\mathbf{h}_t(\mathbf{x}_n)})$ 2. compute weighted error

3. compute hypothesis weight $\alpha_t = \frac{1}{2} \ln \frac{1 - \varepsilon_t}{\varepsilon_t}$

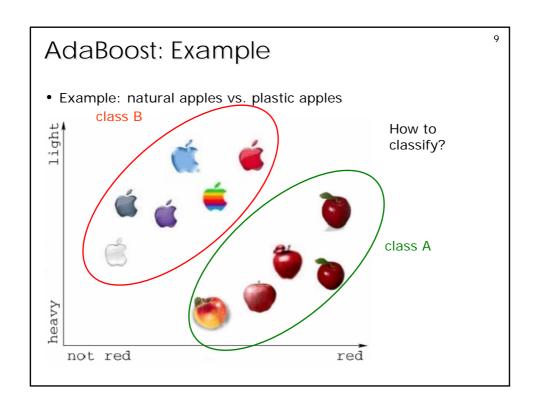
4. update example distribution $d_n^{(t+1)} = d_n^{(t)} \exp(-\alpha_t y_n h_t(\underline{x}_n))/Z_t$ Z_t is a normalization factor

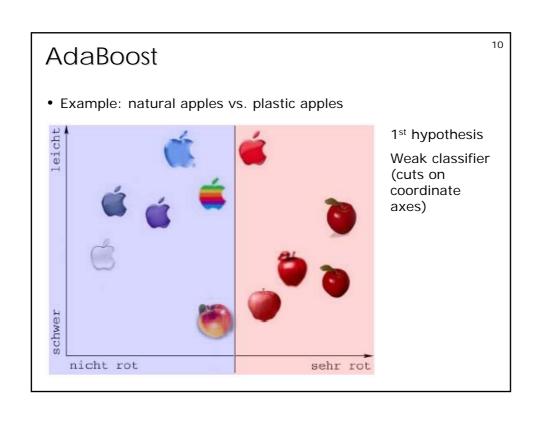
Output: final hypothesis $f_{Ens}(\underline{x}) = \sum_{t=1}^{T} \alpha_t h_t(\underline{x})$

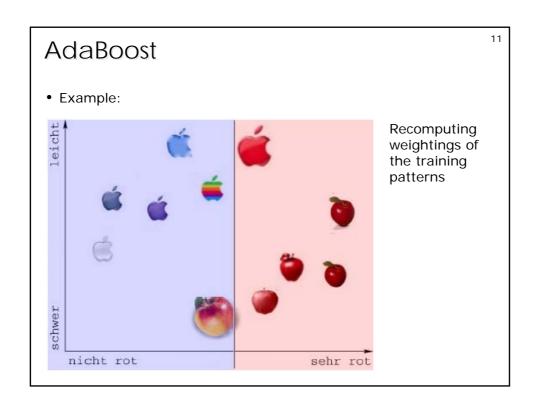
AdaBoost: Decision Stumps

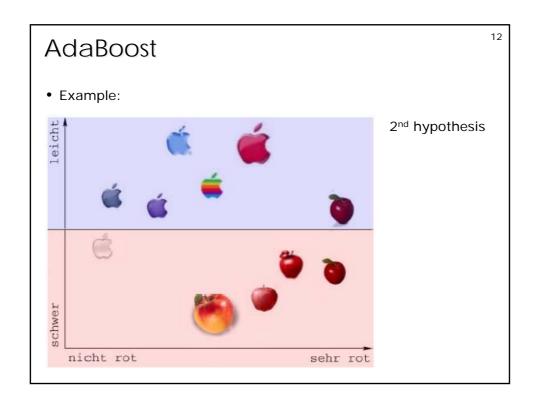
- · A family of weak learners,
 - e.g. Decision stump:
 - can perform a single test on a single attribute with threshold Θ .
 - parameterize all decision stumps as follows:

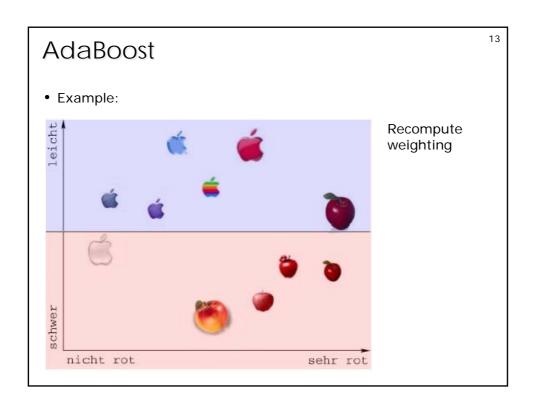
$$f^{j}(\underline{x};\theta) = \begin{cases} 1 & \text{if } x_{j} > \theta \\ -1 & \text{else} \end{cases}, \quad j = 1,....,d$$

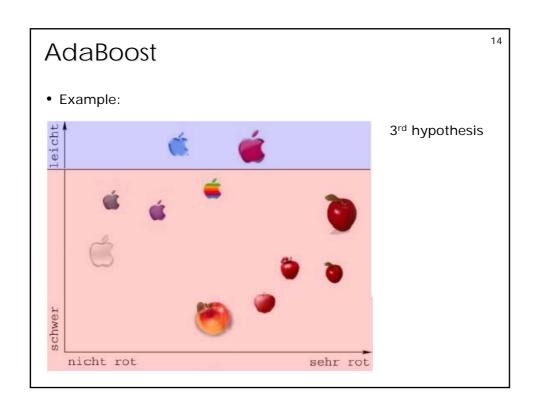


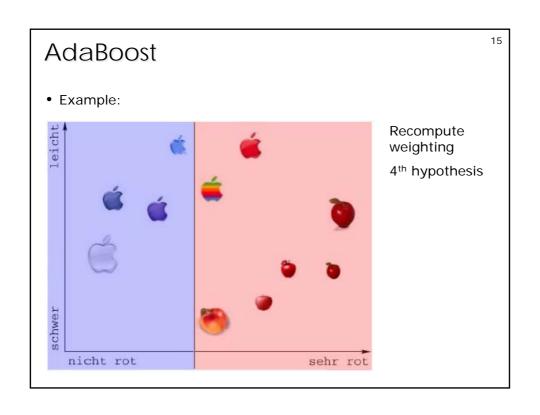


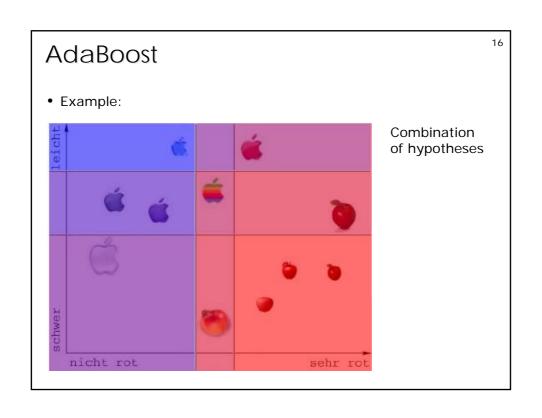


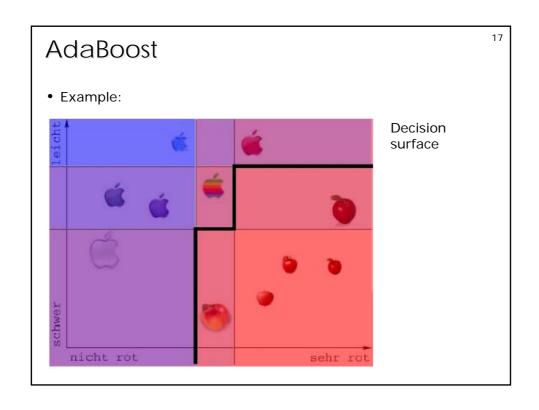


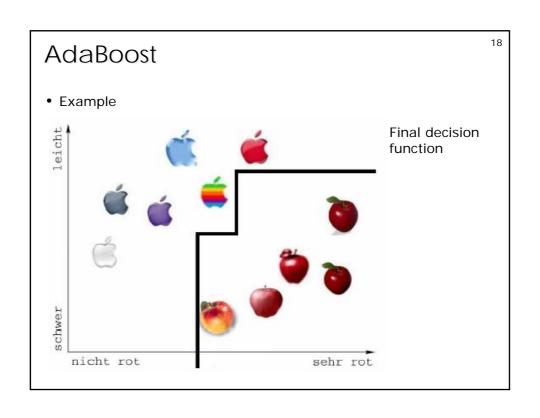












AdaBoost: Frame work

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Input: N examples $\{(\underline{x}_{I}, y_{I}), \ldots, (\underline{x}_{N}, y_{N})\},\$

L a learning algorithm generating hypothesis $h_i(\underline{x})$ (classifiers)

 ${\cal T}$ maxNumber of hypotheses in the ensemble

Initialize: d_n weigth of example n (\underline{d} is a distribution with $1 = \sum_{n=1}^{N} d_n^{(t)}$)

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Do for t = 1, ..., T,

Data

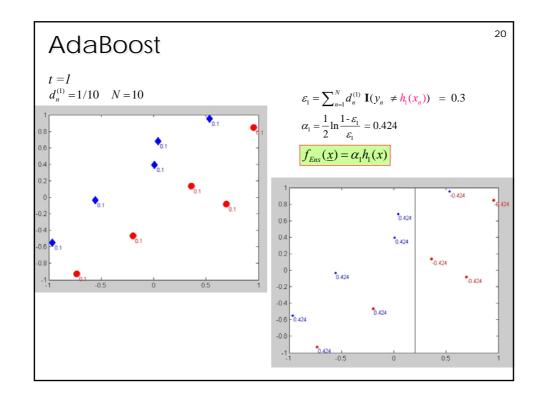
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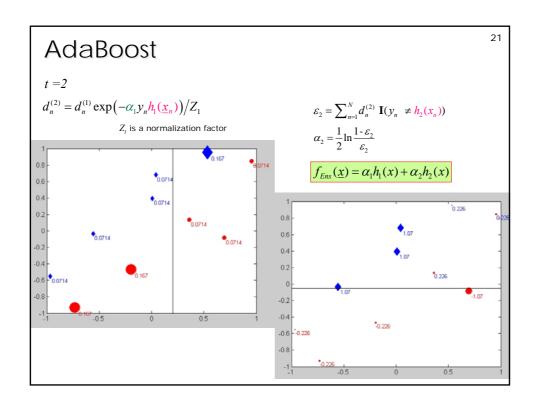
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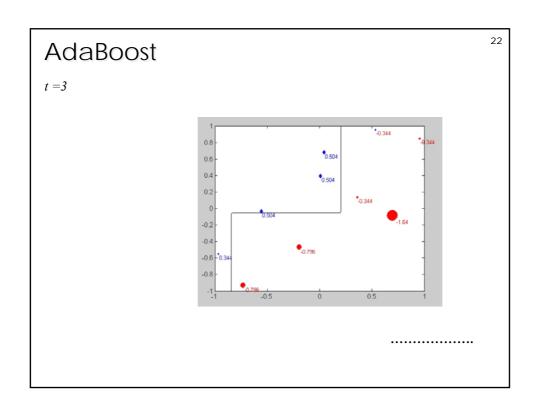
3. compute hypothesis weight $\alpha_t = \frac{1}{2} \ln \frac{1 - \varepsilon_t}{\varepsilon_t}$

4. update example distribution $d_n^{(t+1)} = d_n^{(t)} \exp\left(-\alpha_t y_n h_t(\underline{x}_n)\right) / Z_t$ Z_t is a normalization factor

Output: final hypothesis $f_{Ens}(\underline{x}) = \sum_{i=1}^{T} \alpha_i h_i(\underline{x})$







AdaBoost: Frame work

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- · Weak Learners used with Boosting
 - Decision stumps (axis parallel splits)
 - Decision trees (e.g. C4.5 by Quinlan 1996)
 - Multi-layer Neural networks (e.g. for OCR)
 - Radial basis function networks (e.g. UCI benchmarks, etc)

Decision trees:

- Hierarchical and recursive partitioning on the input space
- Many approaches, usually axis parallel splits

• Comparison AdaBoost vs. SVM • Comparison AdaBoost vs. SVM AdaBoost's decision line These decision lines are for a low noise case with similar generalization errors. In AdaBoost, RBF networks with 13 centers were used.

AdaBoost: Application

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Application

- DT C4.5 as weak classifier
- Spam, Zip Code OCR
- Text classification: Schapire and Singer Used stumps with normalized term frequency and multi-class encoding
- OCR: Schwenk and Bengio (neural networks)
- Natural language Processing: Collins; Haruno, Shirai and Ooyama
- Image retrieval: Thieu and Viola
- Medical diagnosis: Merle et al.
- Fraud Detection: Rätsch & Müller 2001
- Drug Discovery: Rätsch, Demiriz, Bennett 2002
- Elect. Power Monitoring: Onoda, Rätsch & Müller 2000

AdaBoost: Information

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Introduction http://informatik.unibas.ch/lehre/ws05/cs232/Downloads/

Schapire A Short Introduction to Boosting.pdf

Internet http://www.boosting.org

http://www.cs.princeton.edu/~schapire/boost.html

Conferences Computational Learning Theory (COLT), Neural Information

Processing Systems (NIPS), Int. Conference on Machine

Learning (ICML), . . .

Journals <u>Machine Learning</u>, Journal of Machine Learning Research,

Information and Computation, Annals of Statistics

People List available at http://www.boosting.org

Software Only few implementations (algorithms 'too simple')

(cf. http://www.boosting.org)