

# UCC501 Homework 2 Solutions

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## 1 Energy Scales, CO2 Emissions and Renewables

### 1.1 Energy Scales

- Natural gas consumption year 2012: in Billion Cubic Feet: 2235.169.
- For natural gases btu we have

$$1cf \rightarrow 1027Btu \quad (1)$$

source: <http://www.aga.org/KC/ABOUTNATURALGAS/ADDITIONAL/Pages/HowtoMeasureNaturalGas.aspx>, use MATLAB to convert units, we have

$$2012 \text{ Yearly } btu = 2235.169 * 10^9 * 1027 \quad (2)$$

Evaluate the equation we get  $2.2955 * 10^{15} Btu$ , divided by millions we get  $2.2955 * 10^9 MBtu$ .

- From this unit conversion site <http://www.eia.gov/cfapps/ipdbproject/docs/units.cfm> we have

$$MTOE = MBtu * 0.02520 * 10^{-6} \quad (3)$$

Evaluate the above equation we have  $57.8471MTOE$

- Similarly we have  $1MBtu = 1.05506 * 10^9 \text{ Joules}$  and  $1KWh = 3.6 * 10^6 \text{ Joules}$ , thus

$$2012 \text{ Yearly } GKWh = 2.2955 * 10^9 * 1.05506 * 10^9 / (3.6 * 10^6 * 10^9) \quad (4)$$

Evaluate the above equation we have  $672.7527 \text{ GKWh}$

## 1.2 CO2 Emissions

- Assume complete combustion, we have  $2235.169 \text{ Bcf}$  natural gas burned in UAE for year 2012. Assume under normal temperature and pressure the natural gas is measured, we google the bold texts **natural gas density** and get the following:

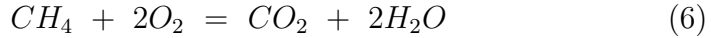
Density

0.656 g/L at 25 C, 1 atm; 0.716 g/L at 0 C, 1 atm;  
0.42262 g cm<sup>3</sup>; (at 111 K)

Since we assume normal density, we use  $\rho = 0.656 \text{ g/L} = 656 \text{ kg/m}^3$ . Thus we have the total mass of CO<sub>2</sub> burned in year 2012

$$\text{Mass of } CH_4 = 4.1525 * 10^{13} \text{ kg} \quad (5)$$

Since the background is complete combustion, from chemistry we have



and introduce a concept from chemistry, **molecular weight** we have

$$\text{Mass of } CO_2 = m_{CH_4} * \frac{M_{CO_2}}{M_{CH_4}} \quad (7)$$

where  $m_{CH_4}$  is the mass, the  $M_{CH_4}$  is the molecular weight. This equation is deducted by **carbon equilibrium** under complete combustion. Evaluate equation (7) we have  $m_{CO_2} = 1.1419 * 10^{14} \text{ kg}$

## 1.3 Renewables