

- Big O Complexity of delMax()

- public int delMax(){
- int data = heap\_array[0]; O(1)
- heap\_array[0] = heap\_array[nElems-1]; O(1)
- heap\_array[nElems-1] = 0; O(1)
- nElems--;
- sink(0); O(N Log 2 (n))
- System.out.println("Max Deleted:");
- printArray();
- return data;
- }
- private void sink(int k){
- int temp = heap\_array[k]; O(1)
- int child\_node;
- while (location(k,1)< nElems){ O( log base 2 (n))
- child\_node = findLargestChild(k); O(d)
- if(heap\_array[child\_node] > temp){ O(1)
- heap\_array[k] = heap\_array[child\_node]; O(1)
- }else
- break;
- k = child\_node; O(1)
- }
- heap\_array[k] = temp; O(1)
- }

- The worst case for delMax() is  $O(d \log_2 N)$  where d is equal to number of children
  - highlighted code causes this time complexity

- BIG O COMPLEXITY OF daryHeapsort()

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public int[] daryHeapsort(){ // heapsort function
    int N = nElems-1;
    for (int i = N/2; i >=0; i--){          // O(log2 N )
        sort(heap_array,i); O( log2 N )
    }
    int k = nElems;
    for (int i = k; i > 1; i--){           // O ( N)
        int temp = heap_array[0]; // set temp = to root    // O(1)
        heap_array[0] = heap_array[i-1]; // set root to most recent child    O(1)
        heap_array[i] = temp; // most recent child = root    O(1)
        nElems--; // decrease nElems    O(1)
        sort(heap_array,0); //o( Log2 N )
    }
    System.out.println("Sorted Array:");
    printArray();
    return heap_array;
}

private void sort(int[] arr, int index) {
    int left = 2 * index; // left = 2 * current root O(1)
    int right = 2 * index + 1; // right = 2 * current root plus 1    O (1)
    int max = index; // set max = root index    O(1)
    if (left <= nElems - 1 && arr[left] > arr[index]) // if left child great than parent    O(1)
    {
        max = left; // max = left
    }
    if (right <= nElems - 1 && arr[right] > arr[max]) // if right child great than parent    O(1)
    {
        max = right; // max = right
    }
    if (max != index) // only called if max != root;
    {
        int temp = arr[max]; //swap max and index given O(1)
        arr[max] = arr[index]; O(1)
        arr[index] = temp;
        sort(arr, max); // recursive call sort with arr and new max    log(N)
    }
}

```

- Worst case for dary-heapsort is O ( N log N )
  - This is cause by the for loop which iterates through the array and the recursive call to implement the heapsort.