

Sprawozdanie programu

$$u_{i,j} = u(x_i, t_j) = u(i \cdot h, j \cdot k) \\ h = 0.1, k = 0.005$$

Równanie Burgers'a

$$1. \quad u(x, 0) = \sin(\pi x), \quad 0 < x < 1$$

$$u(0, t) = u(1, t) = t > 0$$

$$2. \quad u(x, t) = -2v \frac{\theta_x}{\theta}$$

$$3. \quad \frac{\delta \theta}{\delta t} = v \frac{\delta^2 \theta}{\delta x^2} \quad 0 < x < 1, \quad t > 0$$

$$4. \quad \theta_x(0, t) = \theta_x(1, t) = 0 \quad t > 0$$

$$5. \quad \theta(x, t) = a_0 + \sum_{n=1}^{\infty} a_n \exp(-n^2 \pi^2 v t) \cos(n \pi x)$$

$$6. \quad a_0 = \int_0^1 \exp\{-2(\pi v)^{-1} (1 - \cos(\pi x))\} dx$$

$$a_n = 2 \int_0^1 \exp\{-(2\pi v)^{-1} [1 - \cos(n \pi x)]\} dx \quad (n = 1, 2, 3, \dots)$$

$$7. \quad u(x, t) = 2\pi v \frac{\sum_{n=1}^{\infty} a_n \exp(-n^2 \pi^2 v t) n \sin(n \pi x)}{a_0 + \sum_{n=1}^{\infty} a_n \exp(-n^2 \pi^2 v t) \cos(n \pi x)}$$