

Root finding Method

Zero function

- 1) Bisection Method
- 2) Method of false position
- 3) Newton Raphson's Method
- 4) Fixed point iteration method

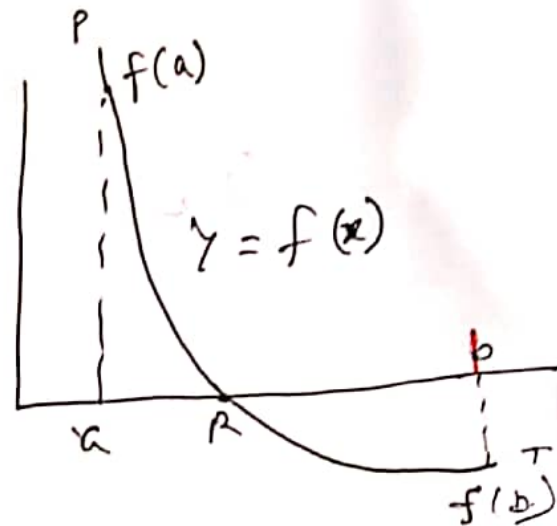
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* Bisection method: If a function $f(x)$ is continuous between a and b , and $f(a) \cdot f(b) < 0$ (or $f(a)$ and $f(b)$ are of opposite sign) then there exists at least one root between a and b .

midpoint, $x_0 = \frac{a+b}{2}$

1) $f(x_0) = 0$ or

2) $f(x_0) \neq 0$



* find a real root of the equation $x^3 - 2x - 4 = 0$

$$f(x) = x^3 - 2x - 4$$

will be
given
in q

$$a = 2$$

$$\rightarrow f(a) = -4$$

$$b = 3$$

$$\rightarrow f(b) = 5$$

$$f(a)f(b) < 0$$

$$x_0 = \frac{a+b}{2} = \frac{2+3}{2} = 2.5$$

* $f(x_0) = -0.875$ neg x₀ 3 b 40
near root or

$f(b) = 5$ pos

* $x_1 = \frac{x_0 + b}{2} = \frac{2.5 + 3}{2} = 2.75$

$$f(x_1) = 1.671875$$

* $x_2 = \frac{x_1 + x_0}{2} = 2.625$

$$f(x_2) = 0.306640625$$

* $x_3 = \frac{x_2 + x_0}{2} = 2.5625$

$$f(x_3) = -0.306396484$$

* $x_4 = \frac{x_3 + x_2}{2} = 2.59375$

$$f(x_4) = -0.00552361$$

* $x_5 = \frac{x_4 + x_2}{2} = 2.609375$ $f(x_5) = 0.149135589$

* $x_6 = \frac{x_5 + x_4}{2} = 2.6015625$ $f(x_6) = 0.071451664$

$$* \quad x_7 = \frac{x_6 + x_4}{2} = 2.59765625$$

$$\therefore f(x_7) = 0.032875597$$

$$x_8 = \frac{x_7 + x_4}{2} = 2.595703125$$

$$f(x_8) = 0.013153881$$

$$x_9 = \frac{x_8 + x_4}{2} = 2.5947265625$$

$$f(x_9) = 0.004655583$$

$$x_{10} = \frac{x_9 + x_4}{2} = 2.594238281 \quad f(x_{10}) = -0.000732427$$

Hence an approximate root is 2.594.

H.W

- 1) $x^3 + x^2 - 1 = 0 \quad (a=0, b=1)$
- 2) $\sin x = 1 - x^2$