Interpoletion formula... Newton's forward Interpoletion formula

$$y(x) = y_0 + u \Delta y_0 + u(u-1) \Delta^2 y_0 + u(u-1)(u-2) \Delta^3 y_0$$



.. yo = Table's most Left side value

$$\mathcal{A} = \frac{x - x_0}{h}$$

: Newton's backward Interpoletion formula

$$y(x) = y_n + u_0 y_n + \frac{u(u-1)}{2!} \Delta y_n + \frac{u(u-1)(u-2)}{3!} \Delta y_n + \frac$$

$$\frac{u(u-1)(u-2)(u-3)}{4!}$$

$$\mathcal{U} = \frac{x - x_{\eta}}{h}$$

using newton formula for interpolation Her 1905 a estimate the population for year 1905 2) the population for year 1925 1931 1921 1901 13110401 Year 1891 1,32,285 246,050 1,68,076 1,95,690 98,752 Population 1) For 1905 = forward Interpolation Year Population 137 142 44 4 14 X2-X1 -10,435 41,358 2,258 1891(XI) 98,752 33,533 30,923 8,177 \$ 1901 (x) 1,32,287 35,791 1,68,076 22,746 27,614 1911 1921 50,360 1.95696 1931 2,46,050

Hene, x = 1905 has a horal with $x = \frac{x - x_0}{h}$ Lear the sale and head $\Delta^{3}_{70} = 98.752$ $\Delta^{3}_{70} = -10.435$ $\Delta^{4}_{70} = 33.533$ $\Delta^{4}_{70} = 41.358$ $\Delta^{4}_{70} = 2258$ $\Delta^{2}_{70} = 2258$ Δ^{2} $\Delta^{0} = 2258$ Δ2y0 46,050 50,0360 22,746 30,923 41,358, 1370 $y(x) = y_0 + u_0 + u(u-1) \alpha y_0 + u(u-1)(u-2)$ + M(M-1) (M-2) (M-3) 2470+... 10+ Hene X! 1925 y(1905) = 1,47,841 (Approximately) 42-14+2 31 A3Jo Δ⁵y.

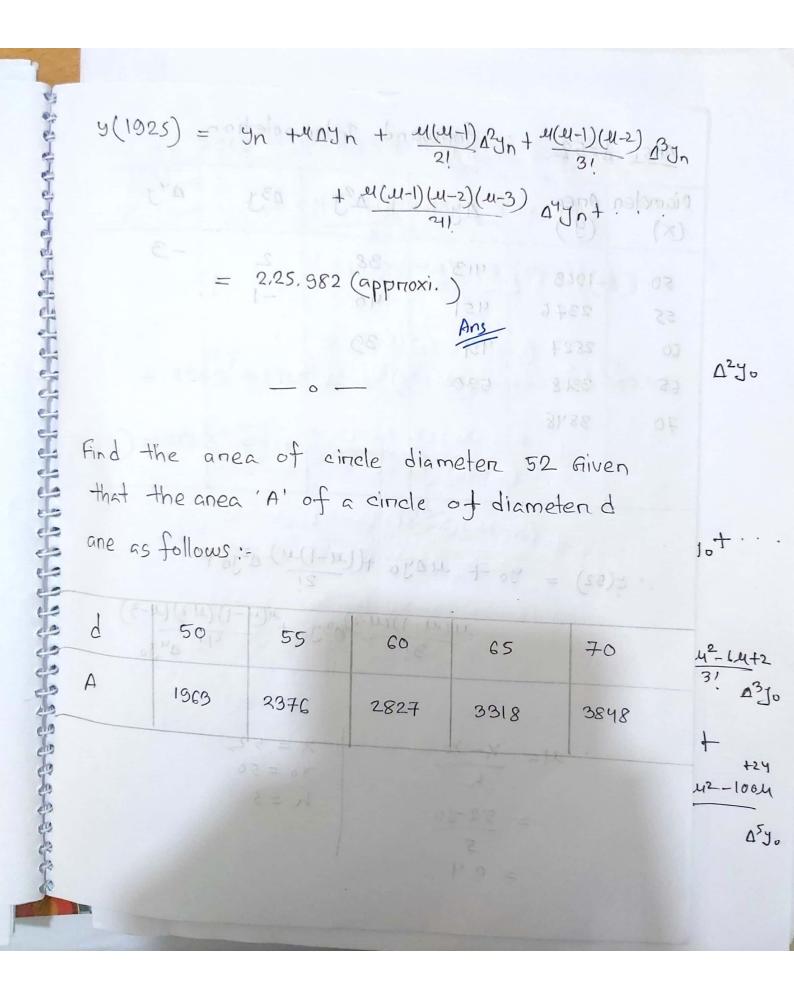
1 for 1925 - backward Intempoletion

Yean	Population	44 79-34	Δ27	ABY AYJ
- 1891 1001	98,752	33.533	18 A 30	124 -3€ = ot .
1911	1,68,676	35,791	2258	Q20 = 2258
- 1921	1,95,690	27,614	-8,177	-10,435
1931	2,46,050	50,0360	22,746	30,923 41,358
	31	21:		on + ot = (x)5.

Hene :
$$X = 1925$$

 $x_n = 1931$

$$H_{1008} = \frac{1}{x - x^{0}}$$



Ans: d=59; Jonwand Interipo	Ans: d=52	Interpoletion
-----------------------------	-----------	---------------

	Diameten (X)	Anea (y)	19	Δ24	139	مع
	50 55	1963	451	38 (200	20.0 =	-3
-	60	2827	991	39		
	65	3318	530			
	70	3848				
	7	52 mu	notomale be at	slonio	onea of	ant bar

$$A = \frac{x - x_0}{h}$$

$$= \frac{52 - 50}{5}$$

$$= 0.4$$

$$X = 52$$

 $X_0 = 50$
 $h = 5$

 $(52) \times \frac{1963 + 0.4 \times 413 + 0.4(.4-1)}{2!} \times 38$ (4-1)(4-2)(4-3) (-3) = 1963 + 165.2 + (-4.56) +x.128 + .1248 Δ2y0 y(52) = 2123.8928 (approx.) Stx (1x-2x) (8x-x) (8x-x) (0x-x) + ERX (hx-xx) (x-xx) (x-xx) (x-xx) (x-xx) 4-14+2 3! 0310

Jo XO Lagrange's Interpolation formula 71 XI y2 33 (for unequal Interval) XY 74 formula for any x . y(x) is given by $J(X) = \frac{(x-x_1)(x-x_2)(x-x_3)(x-x_4)}{(x_0-x_1)(x_0-x_2)(x_0-x_3)(x_0-x_4)}$ $+ \frac{(x-x_0)(x-x_2)(x-x_3)(x-x_4)}{(x_1-x_6)(x_1-x_2)(x_1-x_3)(x_1-x_4)} \times y_1$ $+\frac{(x-x_0)(x-x_1)(x-x_3)(x-x_4)}{(x_2-x_0)(x_2-x_1)(x_2-x_3)(x_2-x_4)}\times y_2$ $+\frac{(x-x_0)(x-x_1)(x-x_2)(x_3-x_4)}{(x_3-x_0)(x_3-x_1)(x_3-x_2)(x_3-x_4)}\times 33$ + (x-x6)(x-x1)(x-x2)(x-x3) (xy-x6)(xy-x1)(xy-x2)(xy-x3)

Given valusoitalog notal a opposited enial x: x_1 x_2 x_3 x_4 x_4 x_5 x_5 x_6 x_7 x_7 x_7 x_8 $\frac{9(9)}{(5-7)(9-1)(9-13)(9-17)} \times 150 \text{ boil}$ $\frac{(5-7)(5-11)(5-13)(5-17)}{(5-7)(5-11)(5-13)(5-17)}$ Δ2y0 $+ \frac{(9-5)(9-11)(9-13)(9-17)}{(7-5)(7-11)(7-13)(7-17)} \times 392$ (x-x)+ (9-5) (9-13) (9-17) × 1452 (11-5)(11-7)(11-13)(11-17) + (9-5)(9-7)(9-11), (9-17) ×2366 (13-5)(13-7)(13-11)(13-17)4-64+2 3! 03jo $+ \frac{(9-5)(9-7)(9-11)(9-13)}{(17-5)(17-7)(17-11)(17-13)} \times 5202$ $\frac{9(9)}{1} = \frac{810}{1}$ 45y. Using Lagrange's Interpolation formula compute the value of log10 321.5

Ans:- find y (10910321.5) using lagrange

$$5(x) = \frac{(x-x_1)(x-x_2)(x-x_3)}{(x_0-x_1)(x_6-x_2)(x_6-x_3)} y_0 + \frac{(x-x_0)(x-x_2)(x_6-x_3)}{(x_1-x_0)(x_1-x_2)(x_1-x_3)} y_1 + \frac{(x-x_0)(x_1-x_2)(x_1-x_3)}{(x_2-x_0)(x_2-x_1)(x_3-x_3)} y_2 + \frac{(x-x_0)(x_2-x_1)(x_3-x_3)}{(x_2-x_0)(x_2-x_1)(x_3-x_3)}$$

$$\frac{(x-x_6)(x-x_1)(x-x_3)}{(x_3-x_6)(x_3-x_1)(x_3-x_2)}$$

of boil slam 12.285000 x 2.5065/ 109 10 321.5 = (23.0400 minds × 2.50893 12y0 = 1.33648 + 2.13829 + (-1.59378) 90 7, XX 43 gum al

(a) Using Lagrange's formula, find the .. Using Lagrange formula 2.8 = [12800] $f(x) = \frac{(x-x_1)(x-x_2)(x-x_3)}{(x_0-x_1)(x_0-x_2)(x_0-x_3)} \times 90$ (x-x0) (x-x1) (x-x3) xy (x-x3) + (x-x0)(x-x1)(x-x3) xy 2 (x3-x0)(x2-x1)(x2-x3) (x-x6)(x-x1)(x-x2) (x3-x6)(x3-x1)(x3-x2)

$$f(x) = \frac{(x-1)(x-3)(x-4)}{(o-1)(o-3)(o-3)(o-3)} \times -12$$

$$+ \frac{(x-0)(x-3)(x-4)}{(o-1)(x-3)(x-4)} \times o$$

$$+ \frac{(x-0)(x-1)(x-4)}{(x-0)(x-1)(x-3)} \times 2^{1/2}$$

$$+ \frac{(x-0)(x-1)(x-3)}{(x-0)(x-1)(x-3)} \times 2^{1/2}$$

$$= (x-1)(x-3)(x-4) + o + 2x(x-1)(x-4) + 2x(x-1)(x-3) = 0$$

$$= (x-1)(x-3)(x-4) + o + 2x(x-1)(x-4) + 2x(x-1)(x-3) = 0$$

$$= (x-1)(x-3)(x-4) + o + 2x(x-1)(x-4) + 2x(x-1)(x-3) = 0$$

$$= (x-1)(x-3)(x-4) + o + 2x(x-1)(x-4) + 2x(x-1)(x-3) = 0$$

$$= (x-1)(x-3)(x-4) + o + 2x(x-1)(x-4) + 2x(x-1)(x-3) = 0$$

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$$= (x-1)(x-3)(x-4) + o + 2x(x-1)(x-4) + 2x(x-1)(x-3) = 0$$

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$$= (x-1)(x-3)(x-4) + o + 2x(x-1)(x-4) + 2x(x-1)(x-3) = 0$$

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$$= (x-1)(x-3)(x-4) + o + 2x(x-1)(x-4) + 2x(x-1)(x-3) = 0$$

$$= (x-1)(x-3)(x-4) + o + 2x(x-1)(x-4) + 2x(x-1)(x-3) = 0$$

$$= (x-1)(x-3)(x-4) + o + 2x(x-1)(x-4) + 2x(x-1)(x-3) = 0$$

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$$= (x-1)(x-3)(x-4) + o + 2x(x-1)(x-4) + 2x(x-1)(x-3) = 0$$

$$= (x-1)(x-3)(x-4) + o + 2x(x-1)(x-4) + 2x(x-1)(x-1)(x-3) = 0$$

$$= (x-1)(x-3)(x-4) + o + 2x(x-1)(x-4) + 2x(x-1)(x-1)(x-3) = 0$$

$$= (x-1)(x-3)(x-4) + o + 2x(x-1)(x-1)(x-1)(x-1)(x-1) = 0$$

$$= (x-1)(x-3)(x-4) + o + 2x(x-1)(x-1)(x-1)(x-1) = 0$$

$$= (x-1)(x-3)(x-4) + o + 2x(x-1)(x-1)(x-1)(x-1) = 0$$

$$= (x-1)(x-3)(x-4) + o + 2x(x-1)(x-1)(x-1)(x-1) = 0$$

$$= (x-1)(x-3)(x-4) + o + 2x(x-1)(x-1)(x-1) = 0$$

$$= (x-1)(x-3)(x-4) + o + 2x(x-1)(x-1)(x-1) = 0$$

$$= (x-1)(x-1)(x-1)(x-1)(x-1) = 0$$

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$$= (x-1)(x-1)(x-1)(x-1)(x-1)(x-1) = 0$$

$$= (x-1)(x-1)(x-1)(x-1)(x-1)(x-1)(x-1) = 0$$

$$= (x-1)(x-1)(x-1)(x-1)(x-1)(x-1)(x-1$$

Newton forward - 0 (1-0) denivative y = yo + μ Δyo + (μ(μ+1) Δ²yo + 3]. $u = \frac{x - x_0}{h} \frac{(C - x)(1 - x)}{(C - x)(1 - y)} \frac{1}{(C - x)}$ (E-X)(X-3)(X-3) + (1-0) = /h (X-1)(X-3)(X-1) + (1-0) = /h dyldx = 0 + Layo + 20-11 x + D2yo + 302-64+2-13J. 1st denivatives 2nd denivatives dy = 1/2 (42 yost (u-1) 43 yot (xz)) 3nd denivatives $\frac{d^3y}{dx^3} = \frac{1}{h^3} \left(\Delta^3 y_0 + \cdots \right)$

Q. find 4st, 2nd, 3nd denivatives of the function tabulated below at x = 1.5

X	1.5	2.0	2.5	3.0	9.5	4.0
((3/F.)]	3.375	7.000	13.625	24.000	38 . 87 5	59.000

Sol Forward Pifference table

0

	P			
X	9	Ayo	Δ ² ,	DBY.
1.5	3.37591	3.635	3.000	0.7.50
2.0	7-000 42	6.635	3.750	0.750
२.ऽ	13.625	10.375	4.500	0.750
3.0	24.000	14.875	5:350	
3.5	38.875	20.135	8 =	
4.0	59.000			
			- In.	Sin 1
		T 4370	t sp	Sont Joins

Hene
$$x = 1.5$$
 $x_0 = 1.5$
 $y_0 = 1.5$
 $y_0 = 0.5$
 $y_0 = 0.5$

$$\frac{dstuctives}{dx} = \frac{1}{h} \left[\Delta y_0 + \frac{2U-1}{2!} \Delta^2 y_0 + \frac{3U^2 - 6U+2}{3!} \Delta^3 y_0 \right]$$

$$= \frac{1}{0.5} \left[3.675 + \frac{0-1}{2!} (3.000) + \frac{0-0+2}{3!} (.750) \right]$$

$$= \frac{1}{0.5} \left[3.675 + \frac{0-1}{2!} (3.000) + \frac{0-0+2}{3!} (.750) \right]$$

$$\frac{2^{nd} + 1^{nuc}}{2^{nd} + 1^{nuc}} = \frac{1}{4^{nuc}} \left[A^{2} + (u-1) A^{3} - \frac{1}{4^{nuc}} \right]$$

$$= \frac{1}{5^{2}} \left(3.000 + (0-1) \cdot 750 \right)$$

$$= 9.000$$

$$3nd \frac{derivatives}{dxz} = \frac{1}{h^3} \Delta^3 y_0$$

$$= \frac{1}{.53} \times .750 = 6.000$$

Thus at
$$x = 1.5$$

$$\frac{dy}{dx} = 4.750$$

$$\frac{dy}{dx^2} = 9.000$$

$$\frac{d^3y}{dx^3} = 1.000$$

Newton's forward Intempolation formula and its derivatives

newton forward formula

 $y(x) = y(x_0 + uh) = y_0 + u \Delta y_0 + \frac{u(u-1)}{21} \Delta^2 y_0$

+ 4(M-1)(M-L) D3J.

(dutor) e-

1st denivatives $y'(x) = 4(x_0 + uh) - \Delta y_0 + \frac{2u - 1}{2!} \Delta^2 y_0 + \frac{3u^2 - u_1 + 2}{3!} \Delta^3 y_0$

+ 443-1842+224-6 A4yo+ 41 +24 8844-46 544-4043+10542-1064

$$y'(x) = \frac{1}{h} \int_{A_{30}}^{A_{30}} + \frac{2u-1}{2!} \Delta y_{0} + \frac{3u^{2}-4u+2}{6} \Delta^{3}y_{0} + \frac{4u^{3}-18u^{2}+22u-4}{4!} \Delta^{3}y_{0} + \frac{4u^{3}-18u^{2}+22u-4}{4!} \Delta^{5}y_{0} + \frac{5u^{4}-40u^{3}+105u^{2}-100u+24}{5!} \Delta^{5}y_{0} + \frac{5u^{4}-40u^{3}+105u^{2}-100u+24}{5!} \Delta^{5}y_{0} + \frac{5u^{4}-40u^{3}+105u^{2}-100u+24}{4!} \Delta^{5}y_{0} + \frac{12u^{2}-3u+22}{4!} \Delta^{4}y_{0} + \frac{12u^{2}-3u+22}{4!} \Delta^{4}y_{0} + \frac{12u^{2}-3u+22}{4!} \Delta^{5}y_{0} + \frac{12u^{2}-3u+22$$

$$=\frac{1}{h^2} \left[\frac{1}{A^2 J_0 + (M-1) \Delta^3 J_0 + \frac{(M^2 - 18M + 11) \Delta^9 J_0}{12} + \frac{2M^3 - 12M^2 + 2JM - 16\Delta^5 J_0 + \frac{1}{12}}{12} \right]$$

$$y'(x) = \frac{1}{h} \int_{0}^{h} A_{j0} + \frac{2u-1}{2!} A_{j0} + \frac{3u^{2}-lu+2}{4!} A_{j0}$$

$$+ \frac{4u^{3}-l8u^{2}+22u-l}{4!} A_{j0}$$

$$+ \frac{5u^{3}-40u^{3}+lt8u^{2}-l0out24}{5!} A_{j0}$$

$$+ \frac{5u^{3}-40u^{3}+lt8u^{2}-l0out24}{5!} A_{j0}$$

$$+ \frac{5u^{3}-40u^{3}+lt8u^{2}-l0out24}{5!} A_{j0}$$

$$+ \frac{2u^{3}-12u^{2}+21u-l0}{10} A_{j0}$$

$$+ \frac{2u^{3}-12u^{2}+21u-l0}{12} A_{j0}$$

$$+ \frac{2u^{3}-12u^{2}+21u-l0}{12} A_{j0}$$

1601-211501+61011-1115 ga- 4KB

Find the first and 2nd, 3nd denivative at poin x = 1.5.

×	1.00	1.05	1.10	1.70	1.20	1.25	1.30
y={x	1.00000	1.02470	1.04881	1.07238	1.8544	1.11803	1.14017