

Algo

DP:

Longest common subsequence (LCS)

$A = \{1, 2, 3, 4\}$ ,  $B = \{1, 2, 3\}$

sub:  $\{1\}$ ,  $\{2\}$ ,  $\{3\}$ ,  $\{4\}$   
 $\{1, 2\}$ ,  $\{1, 3\}$ ,  $\{1, 4\}$ ,  $\{2, 3\}$  ...  
 $\{1, 2, 4\}$ ,  $\{1, 2, 3\}$  ...

maintain order sequence

$\{1, 4, 3\} \rightarrow$  wrong

step:

$LCS(\{ \underline{1}, 2, 3, 4 \}, \{ \underline{1}, 2, 3 \})$

$\Rightarrow 1 + LCS(\{ \underline{2}, 3, 4 \}, \{ \underline{2}, 3 \})$

$\Rightarrow 2 + LCS(\{ \underline{3}, 4 \}, \{ \underline{3} \})$

Algo TT  
[8 dec]

$$= ) 3 + 0 \quad \therefore \text{Length} = 3$$

$\text{max} \left\{ \begin{array}{l} \text{LCS}("AXY", "AYZX") \\ \text{LCS}("AXYT", "AYZ") \end{array} \right\}$

$lcs(x, y, m, n) \begin{cases} m \rightarrow \text{string size} \\ n \rightarrow \text{current index} \end{cases}$   
 if  $(m=0$   
 ||  $n=0)$  return 0;

if ( $x[m] == y[n]$ ) return  $1 + \text{les}(x, y, m-1, n-1)$

$$\text{defun max} \{ \text{les}(x, y, m-1, n), \text{les}(x, y, m, n-1) \}; \}$$

2D vector  $[m] [n]$

Time:  $O(2^n)$

→ ~~Top-down~~ Bottom-up  
(recursion)

improved code: if (m=0 || n=0) return 0;

if (dp[m][n] != -1)  
return dp[m][n];

if (x[m-1] == y[n-1]) return dp[m][n]  
= 1 + les(x, y, m-1, n-1)

return dp[m][n] = max(les(x, y, m-1, n), les(x, y, m, n-1));

iterative:

		0	0	0	0
A	0	0	0	0	1
C	0	0	0	0	2
A	0	1	1	2	2
D	0	1	2	2	2
B	0	1	2	2	2