Appendix

List of symbols

This list of symbols contain some of the most used symbols in this dissertation. The symbols are grouped into three categories: Vector Spaces and Related Concepts, Mathematical Measures and Operations, and Physical Quantities and Parameters. The first appearance of each symbol is also listed.

Other symbols that are section specific or that are contextually evident might not be in this list.

Vector Spaces and Related Co ncepts

Symbol	Description	First Appearance (Page)
N	set of natural numbers j	??
\mathbb{R}^n	n-dimensional space of real numbers	??
Ω	subset of \mathbb{R}^n , usually representing a	??
	body/reference configuration	
$\partial\Omega$	the boundary of Ω	??
$ar{\Omega}$	the boundary of Ω	??
C^n	set of n-times continuously differen-	??
	tiable functions	
C^{∞}	space of smooth functions	??
C_0^{∞}	space of smooth functions with com-	??
	pact support	
L^n	space of n-power Lebesgue integrable	??
	functions	

H^n	space of functions with weak deriva-	??
	tives up to order n (n'th dimensional	
	Sobolev space)	
X	global space	??
V	inertia space	??
W	energy space	??
$T(\Omega)$	test function space on Ω	??
S^h	finite dimensional subspace	??
\mathcal{P}_{j}	set of all polynomials of degree at most	??
	j	
E_n	space spanned by the orthonormal ba-	??
	sis vectors e_i	

Mathematical Measures and Operations

Symbol	Description	First Appearance (Page)
$a(\cdot,\cdot),b(\cdot,\cdot),c(\cdot,\cdot)$	bilinear forms	??, ??, ??
$(\cdot,\cdot)_X$	innerproduct of X	??
$ \cdot _X$	norm in the space X	??
$\partial_x^n f$	n-th partial derivative of f	??
	with respect to x	
$\mathrm{div}X$	divergence of the matrix X	??
$\operatorname{Tr}(X)$	Trace of the matrix X	??
$\det(M)$	determinant of M	??
$\operatorname{span}(\cdot)$	span of a set	??
dV	volume integral measure	??
dS	surface integral measure	??
dA	area integral measure	??
ds	line integral measure	??
$\mathcal{E}(\cdot)$	energy function	??
$R(\cdot)$	Rayleigh quotient	??
Π	interpolation operator	??
$ar{u}$	another form explicity show-	??
	ing u is a vector	
RE	abbriviation for the relative	??
	error	

Physical Quantities and Parameters

Symbol	Description	First Appearance (Page)
$\overline{\lambda}$	eigenvalue	??
u or w	displacement vector	??
ϕ	arbitrary vector/rotation of cross-	??
	section of Timoshenko beam	
Q	force per unit volume	??
ho	density	??
T	stress tensor	??
σ_{ij}	element of the stress tensor T	??
$\mathcal{E}^{'}$	infinitesimal strain tensor	??
$arepsilon_{ij}$	element of the infinitesimal strain ten-	??
	sor \mathcal{E}	
E	Young's modulus	??
ν	Poisson's ratio	??
t	time	??
ℓ	dimension representing length	??
h	dimension representing height	??
b	dimension representing width	??
G	shear modulus of elasticity	??
A	area of a cross-section	??
V	shear force	??
I	area moment of inertia	??
M	moment	??
f^*	dimensionless form of f	??
au	dimensionless time	??
ξ	dimensionless space	??
α/β	dimensionless constants	??
κ^2	some dimensionless constant/shear	??
	correction factor	
I	identity matrix	??
γ	a dimensionless constant	??
n	a normal vector	??
Σ/Γ	distinct parts of Ω	??
μ	eigenvector	??
e_i	orthonormal basis vector	??

Sobolev spaces

The Space L^2

Consider a measurable space X. The set of square integrable functions is called the L^2 space.

The inner product of L^2 is defined as

$$(f,g) = \int_X fg$$
 for $f,g \in L2$.

The norm can be defined as $||f|| = (f, f)^{\frac{1}{2}}$ for each $f \in L^2(X)$. For reference, see [Rud53].

The Space L^p

Consider a measurable space X. For a real number $p \geq 1$, the set of p-integrable functions is called the L^p space. A function f belongs to $L^p(X)$ if the p-th power of its absolute value is Lebesgue integrable, that is, if

$$\int_X |f|^p < \infty.$$

The L^p norm (or p-norm) is defined as

$$||f||_p = \left(\int_X |f|^p\right)^{\frac{1}{p}}$$

for each $f \in L^p(X)$.

Continuous function spaces

 $C^m(a,b)$ is the space of functions with continuous derivatives up to order m over the open interval (a,b).

 $C^m[a,b]$ is the space of functions in $C^m(a,b)$, with existing right derivatives at a and existing left derivatives at b, up to order m.

 $C_0^m(a,b)$ contains all functions f in $C^m[a,b]$ with the property that there exists numbers $a < \alpha < \beta < b$ such that f is zero on $[a,\alpha] \cup [\beta,b]$. This property is called compact support.

 $C^{\infty}(a,b)$ contains all functions in $C^{m}(a,b)$ for all m.

 $C^{\infty}[a,b]$ contains all functions in $C^m[a,b]$ for all m.

 $C_0^{\infty}(a,b)$ contains all functions in $C_0^m(a,b)$ for all m.

First order weak derivative

Suppose $u \in L^2(a,b)$ and there exist a $v \in L^2(a,b)$ such that

$$(u, \phi') = -(v, \phi)$$
 for each $\phi \in C_0^{\infty}(a, b)$

then v is called the first order weak derivative of u and is denoted by Du.

Higher order weak derivative

Suppose $u \in L^2(a,b)$ and there exist a $v \in L^2(a,b)$ such that

$$(u, \phi^{(m)}) = (-1)^{(m)}(v, \phi)$$
 for each $\phi \in C_0^{\infty}(a, b)$

then v is called the m'th order weak derivative of u and is denoted by $D^{(m)}u$.

Sobolev spaces

 W^n is the space of functions with weak derivatives up to order n. There are also special notation $W^{n,p}$ that indicates that the functions are P-intergrable.

 H^n is the space of functions with weak derivatives up to order n and the functions are square integrable. (i.e. $H^n = W^{n,2}$)

MATLAB Code

The following are the main code used in this dissertation to obtain the eigenvalues and eigenvectors of the models. The code and the dissertation is also available on GitHub at https://github.com/Propagandalf-7/masters.

The code is optimized for performance, and therefore the presentation of the code is not optimized for readability. The code is also not commented.

Example code for Timoshenko beam model

```
function [u,p,Eig] = TimoshenkoEig(alpha)
2 syms A;
  syms B;
  syms C;
5 syms D;
6 syms x;
  syms m;
8 syms o;
9 syms lam;
10 syms k;
11 syms a;
12 syms t;
13 format long;
15 \mid \% gamma = 0.25;
nu = 0.3;
gamma = 1/(2*(1+nu))*5/6;
| delt = 4*gamma/(1+gamma)^2*alpha/lam + (1-gamma)^2/(1+gamma)^2;
omega2 = 1/2*lam*(1+gamma)*(delt^(1/2)+1);
|mu2| = 1/2*lam*(1+gamma)*(delt^(1/2)-1);
22 theta2 = 1/2*lam*(1+gamma)*(1-delt^(1/2));
23
```

```
u = A*sinh(m*x) + B*cosh(m*x) + C*sin(o*x) + D*cos(o*x);
_{26}|_{p} = A*((1am+m^2)/m*\cosh(m*x)) + B*((1am+m^2)/m*\sinh(m*x)) + C
              *(-(lam-o^2)/o*cos(o*x)) + D*((lam-o^2)/o*sin(o*x));
27
u = B + C*sin(o*x) + D*cos(o*x);
29 \mid \%p = A + B*a*x + C*(-(1am-o^2)/o)*cos(o*x) + D*((1am-o^2)/o)*
             sin(o*x);
30
||x|| = A * \sin(t * x) + B * \cos(t * x) + C * \sin(o * x) + D * \cos(o * x);
32 \mid \%p = A*(-(1am-t^2)/t)*cos(t*x) + B*(1am-t^2)/t*sin(t*x) + C*(-(1am-t^2)/t)*cos(t*x) + C*(-
             lam - o^2)/o * cos(o*x) + D*(lam - o^2)/o*sin(o*x);
33
35 subs((u),x,0);
36 subs((p),x,0);
u = subs(u, [D, C], [-B, A*(lam+m^2)/m*o/(lam-o^2)]);
39 p = subs(p,[D,C],[-B,A*(lam+m^2)/m*o/(lam-o^2)]);
40
u = subs(u, [B, C], [-D*((lam-o^2)/a), o/lam*(A + k*(-D*((lam-o^2)/a)))
            /a) +D))]);
42 %p = subs(p,[B,C],[-D*((lam-o^2)/a),o/lam*(A + k*(-D*((lam-o^2)
             /a) +D))]);
44 \mid \%u = subs(u, [D, C], [-B, -o/(o^2-lam)*(t^2-lam)/t*A]);
|| p = subs(p,[D,C],[-B,-o/(o^2-lam)*(t^2-lam)/t*A]);
46
|M1| = (subs(diff(p),x,1));
M2 = (subs(diff(u) - p,x,1));
_{49} M = [subs(M1,[A,B],[1,0]) subs(M1,[A,B],[0,1]);subs(M2,[A,B
             ],[1,0]) subs(M2,[A,B],[0,1])];
51 %latex(simplify(det(M)))
52
L = subs(M,k,sqrt(5/6));
L = subs(L, o, (omega2)^(1/2));
L = subs(L,m,(mu2)^(1/2));
L = subs(L,t,(theta2)^(1/2));
57
_{58} Y = det(L);
59 Y = simplify(subs(Y,lam,x));
61 %ezplot(Y,[0,300])
62 %grid on
_{64} R = 0;
_{65} R = FindRoots(Y, 0.001, 500, 0.1)
_{66} %R = FindRoots (Y, 100, 200, 0.1)
```

```
|RF| = zeros(1, size(R, 2));
RF2 = zeros(1, size(R, 2));
_{69} RF3 = zeros(1, size(R,2));
70 RF4 = zeros(1, size(R, 2));
_{71} for i = 1:size(R,2)
       if(R(i)-0.1>0)
           RF(i) = FindRoots(Y,R(i)-0.1,R(i)+0.1,0.0001);
74
           RF(i) = FindRoots(Y, 0.0001, R(i) + 0.1, 0.0001);
       end
76
77
  end
  for i = 1:size(R,2)
       if (RF(i)-0.0001>0)
           RF2(i) = FindRoots(Y,RF(i)-0.0001,RF(i)+0.0001,0.00001)
80
       else
81
           RF2(i) = FindRoots(Y, 0.0001, RF(i) + 0.0001, 0.00001);
82
       end
83
84
  end
85 for i = 1: size(R, 2)
       if (RF2(i)-0.00001>0)
           RF3(i) = FindRoots(Y,RF2(i)-0.00001,RF2(i)
      +0.00001,0.000001);
       else
           RF3(i) = FindRoots(Y, 0.00001, RF2(i)+0.00001, 0.000001);
89
90
       end
91 end
92 %for i = 1:size(R,2)
       if(RF3(i)-0.00001>0)
            RF4(i) = FindRoots(Y,RF3(i)-0.000001,RF3(i)
      +0.000001,0.0000001);
95 %
      else
            RF4(i) = FindRoots(Y,0.000001,RF3(i)
96
      +0.000001,0.0000001);
  %
        end
97
98 %end
100 Eig = RF3';
101 | % ModeNum = 1;
102 Eig
103 % {
imageDir = fullfile(cd, 'images');
if ~exist(imageDir, 'dir')
     mkdir(imageDir);
106
107 end
108
109 for i = 1:size(Eig,1)
% Get values
```

```
LS = subs(L,lam,RF(i));
       [a,L1] = gauss(LS,[0;0]);
112
       B1 = double(-L1(1,1)/L1(1,2))
113
       us = subs(u,[o,m],[(omega2)^(1/2),(mu2)^(1/2)]);
114
       ps = subs(p,[o,m],[(omega2)^(1/2),(mu2)^(1/2)]);
       us = simplify(subs(us,[lam,A,B,k],[RF(i),1,B1,sqrt(5/6)]));
       ps = simplify(subs(ps,[lam,A,B,k],[RF(i),1,B1,sqrt(5/6)]));
117
118
       xd = 0:0.01:1;
       uss = subs(us,x,xd);
120
       max = norm(uss, Inf);
       us = us/max;
123
       pss = subs(ps,x,xd);
124
       maxp = norm(pss, Inf);
       ps = ps/maxp;
126
       % Displacement
128
       f1 = figure('Name', ['Mode ' num2str(i) ' Displacement']);
129
       clf(f1)
130
       ezplot(us,[0,1])
       title(['Mode ' num2str(i) ' Displacement'])
       xlabel('x (Position)')
       ylabel('Displacement (Normalized)')
134
       legend('Displacement', 'Location', 'best')
135
       % Stress
       f2 = figure('Name', ['Mode ' num2str(i) ' Stress']);
       clf(f2)
139
       ezplot(ps,[0,1])
140
       title(['Mode ' num2str(i) ' Stress Distribution'])
141
       xlabel('x (Position)')
       ylabel('Stress (Normalized)')
143
       legend('Stress Distribution', 'Location', 'best')
145
      % Both
146
      f3 = figure('Name', ['Mode' num2str(i)' Displacement and
147
      Stress']);
       clf(f3)
148
       hold on
149
       ezplot(us,[0,1])
150
       ezplot(ps,[0,1])
       title(['Mode ' num2str(i) ' Displacement and Stress'])
152
       xlabel('x (Position)')
153
       legend('Displacement', 'Stress Distribution', 'Location', '
      best')
      hold off
156
```

```
saveas(f1, fullfile(imageDir, ['Mode_' num2str(i) '
157
      _Displacement.png']));
       saveas(f2, fullfile(imageDir, ['Mode_' num2str(i) '_Stress.
158
      png']));
       saveas(f3, fullfile(imageDir, ['Mode_' num2str(i) '
      _Displacement_and_Stress.png']));
  writeToExcel(Eig, imageDir);
161
162 %}
163 return;
  function writeToExcel(Eig, imageDir)
165
       % Define the name of the Excel file
       excelFileName = 'TimoshenkoResults.xlsx';
167
       % Initialize COM server
169
       Excel = actxserver('Excel.Application');
170
       Excel.Workbooks.Add;
171
172
       % Get active sheet
173
       WorkSheets = Excel.ActiveWorkBook.Sheets;
174
       sheet1 = WorkSheets.get('Item', 1);
       sheet1.Activate;
176
       % Start writing data to Excel
178
       sheet1.Range('A1').Value = 'Mode Number';
179
       sheet1.Range('B1').Value = 'Eigen Value';
180
       for i = 1:size(Eig, 1)
182
           sheet1.Range(['A' num2str(i + 1)]).Value = i; % Mode
      Number
           sheet1.Range(['B' num2str(i + 1)]).Value = Eig(i); %
      Eigen Value
           % Insert images
186
           pic_path = fullfile(imageDir, ['Mode_' num2str(i) '
187
      _Displacement.png']);
           disp(['Image path: ', pic_path]);
188
           Excel.ActiveSheet.Shapes.AddPicture(pic_path, 0, 1,
189
      100, i*100, 200, 200);
           pic_path = fullfile(imageDir, ['Mode_' num2str(i) '
190
      _Stress.png']);
           disp(['Image path: ', pic_path]);
191
           Excel.ActiveSheet.Shapes.AddPicture(pic_path, 0, 1,
192
      100, i*100, 200, 200);
           pic_path = fullfile(imageDir, ['Mode_' num2str(i) '
193
      _Displacement_and_Stress.png']);
           disp(['Image path: ', pic_path]);
194
```

```
Excel.ActiveSheet.Shapes.AddPicture(pic_path, 0, 1,
      100, i*100, 200, 200);
       end
196
197
       \% Save and close the Excel file
198
       Excel.ActiveWorkBook.SaveAs(excelFileName);
199
       pause(1); % waits for 1 second
200
201
       Excel.ActiveWorkbook.Close;
       Excel.Quit;
203
       Excel.delete;
       clear Excel;
205
206
  function I = IntervalDivision(a,b,TOL)
207
  if abs(b-a) >= TOL
      m = abs(b-a)/2;
209
      I = [IntervalDivision(a,a+m,TOL); IntervalDivision(a+m,b,TOL
      )];
211
      return;
  else
212
       I = [a b];
213
214 end
215 return
216
function R = FindRoots(Y,a,b,TOL)
  syms x;
19 I = IntervalDivision(a,b,TOL);
_{220} n = size(I,1);
221 SubsI = zeros(size(I));
222 for i = 1:n
       SubsI(i,1) = subs(Y,x,I(i,1));
223
       SubsI(i,2) = subs(Y,x,I(i,2));
225 end
226
  icount = 1;
227
  for i = 1:n
      if SubsI(i,1) == 0
229
          R(icount) = I(i,1);
230
          icount = icount+1;
231
      elseif SubsI(i,1) == 0
232
          R(icount) = I(i,1);
233
           icount = icount+1;
234
      elseif SubsI(i,1)*SubsI(i,2) < 0</pre>
235
          R(icount) = (I(i,2)+I(i,1))/2;
236
           icount = icount+1;
      end
238
  end
240 return
```

Example code for two-dimensional elastic body using bi-cubics

```
function [E, n, m] = TwoDimensionalCantileverCubic(n,alpha,
      graph)
2 format long g
3 %gpuDevice(2)
4 beta = 1;
5 %alpha = 300;
6 \text{ gamma} = 0.3205;
nu = 0.3;
8 iA = 1/(1-nu^2);
9 | iB = 1/(2*gamma*(1+nu));
ex = sqrt(12/alpha);
12 h=ex
13 \% ex = h
_{14} m = ceil(n*ex);
16 if (m <= 1)
17
      m = 2;
18 end
19 \% if (m >= 15)
m = 15;
21 %end
22 %n
_{23} %m = 2
_{25} a = 0;
_{26} b = 1;
_{27} c = 0;
29 %d = sqrt(12/alpha);
30 d =h
31 deltx = (b-a)/n;
32 delty = (d-c)/m;
34 [MM, Kxx, Kxy, Kyy, D0] = CalMatrix(n,m,deltx,delty);
35 Kyx = Kxy'; %CHECKED
36 All = (n+1)*(m+1);
38 K1 = Kxx + (1-nu)/2*Kyy;
39 K2 = nu*Kyx + (1-nu)/2*Kxy;
```

```
_{40} K3 = nu*Kxy + (1-nu)/2*Kyx;
| K4 = Kyy + (1-nu)/2*Kxx;
42 0 = sparse(size(MM,1), size(MM,2)); % CHECKED
43 MMu = [MM O; %CHECKED
          O MM]; % CHECKED
_{45} Mf = MMu;
|K| = 1/(gamma*(1-nu^2))*[K1 K2; K3 K4];%CHECKED
|x| = [7*All:-1:7*All-(m+1)+1 5*All:-1:5*All-(m+1)+1 3*All:-1:3*
     All-(m+1)+1 1*All:-1:1*All-(m+1)+1];
_{48} | K(x,:) = [];
_{49} K(:,x) = [];
50 | MMu(x,:) = [];
_{51} MMu(:,x) = [];
52 | Mf(x,:) = [];
53 %CHECKED
%eig(Mu,K)
[V,D] = eigs(K,MMu,20,'sm');
E = diag(D);
57 size(K)
58
59 if (graph == 1)
      for i = 1:10
60
           w = V(:,i);
61
           f = -1/200;
63
           F1 = zeros((n+1)*(m+1),1);
           F1(ceil((1+(m+1))/2)) = f;
65
           F = zeros(8*(n+1)*(m+1),1);
           F(4*(n+1)*(m+1)+1:5*(n+1)*(m+1)) = F1;
67
69
           %ueq = K \setminus MMu*(-w);
           tic
71
           %Kg = gpuArray(K);
72
           %Mfg = gpuArray(Mf);
73
           %Fg = gpuArray(F);
74
           toc
75
76
           \%b = Mf * (-F);
77
           %tic
78
           %ueq = K \setminus Mf * (-F);
79
           %toc
80
           b = MMu*(-w);
81
           tic
82
           tol = 0.00001;
83
           maxit = 30000;
84
           alpha1 = max(sum(abs(K),2)./diag(K))-2;
```

```
L = ichol(K,struct('type','ict','droptol',1e-3,'
86
      diagcomp',alpha1));
           ueq = pcg(K,b,tol,maxit,L,L');
87
88
89
           Ep = Positions(m,n,deltx,delty);
90
           %ux = 0;
91
           %uv = 0;
92
93
           ux = [ueq(1:(n+1)*(m+1)-(m+1),1); zeros(m+1,1)] + Ep
      (:,1);
           dxux = [ueq((n+1)*(m+1)-(m+1)+1:2*(n+1)*(m+1)-(m+1),1)
      ];
           dyux = [ueq(2*(n+1)*(m+1)-(m+1)+1:3*(n+1)*(m+1)-2*(m+1)
95
      ,1); zeros(m+1,1)];
           dxyux = [ueq(3*(n+1)*(m+1)-2*(m+1)+1:4*(n+1)*(m+1)-2*(m+1)]
96
      +1),1)];
           uy = [ueq(4*(n+1)*(m+1)-2*(m+1)+1:5*(n+1)*(m+1)-3*(m+1)]
97
      ,1); zeros(m+1,1)] + Ep(:,2);
98
           dxuy = [ueq(5*(n+1)*(m+1)-3*(m+1)+1:6*(n+1)*(m+1)-3*(m+1)]
      +1),1)];
           dyuy = [ueq(6*(n+1)*(m+1)-3*(m+1)+1:7*(n+1)*(m+1)-4*(m+1)]
99
      +1),1); zeros(m+1,1)];
           dxyuy = [ueq(7*(n+1)*(m+1)-4*(m+1)+1:8*(n+1)*(m+1)-4*(m+1)]
100
      +1),1)];
           ux = flip(ux);
           dxux = flip(dxux);
103
           dyux = flip(dyux);
           dxyux = flip(dxyux);
           uy = flip(uy);
           dxuy = flip(dxuy);
107
           dyuy = flip(dyuy);
           dxyuy = flip(dxyuy);
109
110
           uxB = ux(D0(ceil((m+1)/2),:));
111
           uyB = uy(D0(ceil((m+1)/2),:));
112
           dxuxB = dxux(D0(ceil((m+1)/2),:));
113
           dxuyB = dxuy(D0(ceil((m+1)/2),:));
114
           dyuxB = dyux(D0(ceil((m+1)/2),:));
           dyuyB = dyuy(D0(ceil((m+1)/2),:));
116
           dxyuxB = dxyux(D0(ceil((m+1)/2),:));
117
           dxyuyB = dxyuy(D0(ceil((m+1)/2),:));
118
119
           maxs = norm(uy, Inf);
120
           uy = uy/maxs;
           stress = ceil((n+1)/2);
           figure(i);
123
124
```

```
scatter(ux,uy, 'b', 'filled'); % blue filled circles
           hold on;
126
           middleIndex = ceil(size(D0,1)/2); % Find the middle
128
      row of DO
           ux1 = ux(D0(middleIndex,:));
129
           uy1 = uy(D0(middleIndex,:));
130
           maxs2 = norm(uy1,Inf);
           plot(ux1,uy1, 'r', 'LineWidth', 2); % red line with
133
      thicker width
           % Add titles, labels, and legends
           title(['Eigenfunction ' num2str(i)]);
136
           xlabel('Ux');
           ylabel('Uy');
138
           legend('Ux vs. Uy', 'Transformed Ux vs. Uy', 'Location'
139
      , 'best'):
140
           grid on; % Add a grid for better readability
141
            sigma11 = 1/(gamma*(1-nu^2))*(dxuxB + nu*dyuyB);
142
           sigma22 = 1/(gamma*(1-nu^2))*(dyuyB + nu*dxuxB);
143
           sigma12 = 1/(2*gamma*(1+nu))*(dyuxB + dxuyB);
144
145
           T = [sigma11(stress) sigma12(stress); sigma12(stress)
146
      sigma22(stress)]
       end
147
148 end
149 return;
function [Mq, Kxxq, Kxyq, Kyyq] = matrix(deltx, delty)%CHECKED
152 syms x;
syms y;
  Q = [1 \times x^2 \times 3 y \times y \times 2*y \times 3*y y^2 \times y^2 \times 2*y^2 \times 3*y^2 y
155
      ^3 x*y^3 x^2*y^3 x^3*y^3;
  size_num = size(Q,2)/4;
157
T = MATRIX_T(Q);
159
160 Mq = zeros(size(Q,2))*x*y;
Kxxq = zeros(size(Q,2))*x*y;
162 \text{ Kxyq} = \text{zeros}(\text{size}(Q,2))*x*y;
Kyyq = zeros(size(Q,2))*x*y;
for i = 1: size(Q, 2)
       for j = 1:size(Q,2)
           Mq(j,i) = Q(j)*Q(i);
167
```

```
Kxxq(j,i) = diff(Q(j),x)*diff(Q(i),x);
168
           Kxyq(j,i) = diff(Q(j),y)*diff(Q(i),x);
169
           Kyyq(j,i) = diff(Q(j),y)*diff(Q(i),y);
170
171
       end
  end
172
173
Mq = int(int(Mq,x,0,1),y,0,1);
175 | Kxxq = int(int(Kxxq,x,0,1),y,0,1);
176 ||Kxyq|| = int(int(Kxyq,x,0,1),y,0,1);
| Kyyq = int(int(Kyyq,x,0,1),y,0,1);
179 | IT = inv(T);
Mq = (IT)'*Mq*IT;
182 | Kxxq = (IT)'*Kxxq*IT;
183 Kxyq = (IT)'*Kxyq*IT;
|Kyyq = (IT)'*Kyyq*IT;
186 Mg = double(Mg*deltx*delty);
187 Kxxq = double(Kxxq*delty/deltx);
188 Kyyq = double(Kyyq*deltx/delty);
189 Kxyq = double(Kxyq);
190 return;
192 function [Adj, Type, D] = Domain(n,m)
193 D = zeros(m+1, n+1);
194 | icount = 1;
195 for i = n+1:-1:1
     for j = 1:m+1
196
          D(j,i) = icount;
          icount = icount + 1;
198
     end
  end
200
D0 = [zeros(1,n+3); zeros(m+1,1)] D zeros(m+1,1); zeros(1,n+3)];
202 icount = 1;
203 Adj = zeros((n+1)*(m+1),9);
  for i = n+2:-1:2
     for j = 2:m+2
205
     Adj(icount,1) = DO(j,i); %middel
206
     Adj(icount, 2) = DO(j-1, i); %bo
207
     Adj(icount,3) = DO(j-1,i+1); %regsbo
208
     Adj(icount,4) = DO(j,i+1); %regs
209
     Adj(icount,5) = DO(j+1,i+1); %regs onder
     Adj(icount,6) = DO(j+1,i); %onder
211
     Adj(icount,7) = DO(j+1,i-1); %links onder
     Adj(icount,8) = DO(j,i-1); %links
213
     Adj(icount,9) = DO(j-1,i-1); %linksbo
      icount = icount +1;
215
```

```
end
216
   Type= zeros((n+1)*(m+1),2);
   T = [1]
                0
                       0
                              0
                                     0
                                            2
                                                                  0;
219
         2
                1
                       0
                              0
                                     0
                                            3
                                                   6
                                                          5
                                                                  4;
220
                2
                                     0
         3
                       0
                              0
                                            0
                                                   0
                                                           6
                                                                  5;
221
                0
                       0
                                     2
                                                   8
                                                          7
         4
                              1
                                            5
                                                                  0;
                              2
                                                                  7;
         5
                4
                       1
                                     3
                                            6
                                                   9
                                                          8
223
                       2
                                     0
                                                   0
                                                          9
         6
                5
                              3
                                            0
                                                                  8;
         7
                0
                       0
                              4
                                     5
                                            8
                                                   0
                                                          0
                                                                  0;
225
                7
                              5
                                                   0
                                                          0
         8
                       4
                                     6
                                            9
                                                                  0;
         9
                       5
                                                          0
                                            0
                                                                  0];
227
    nnz(T);
228
229
   for i = 1:(n+1)*(m+1)
      Type(i,1) = Adj(i,1);
231
      for j = 1:9
232
           bflag = true;
233
234
           for k = 1:9
                if(any(T(j,k)) ~= any(Adj(i,k)))
                    bflag = false;
236
                end
237
           end
238
           if(bflag == true)
               Type(i,2) = j;
240
           end
      end
242
   end
   return
244
   function [M, Kxx, Kxy, Kyy, D0] = CalMatrix(n, m, deltx, delty)
   [Adj, Type, DO] = Domain(n,m);
   [Mq,Kxxq,Kxyq,Kyyq] = matrix(deltx,delty);
ns = nnz(Adj);
_{251} Ms = zeros (16*ns,1);
252 Kxxs = zeros(16*ns,1);
   Kxys = zeros(16*ns,1);
254 | Kyys = zeros(16*ns,1);
   x = [1:(n+1)*(m+1)]';
   c = sum(Adj^=0,2);
257
258
  ix = repelem(x,c);
259
   x = [ix; ix+(n+1)*(m+1); ix+2*(n+1)*(m+1); ix+3*(n+1)*(m+1);
       ix; ix+(n+1)*(m+1); ix+2*(n+1)*(m+1); ix+3*(n+1)*(m+1);
261
       ix; ix+(n+1)*(m+1); ix+2*(n+1)*(m+1); ix+3*(n+1)*(m+1);
       ix; ix+(n+1)*(m+1); ix+2*(n+1)*(m+1); ix+3*(n+1)*(m+1);];
263
```

```
264
265 iy = nonzeros(Adj');
          y = [iy; iy; iy; iy;
266
                          iy+(n+1)*(m+1);iy+(n+1)*(m+1);iy+(n+1)*(m+1);iy+(n+1)*(m+1)
267
                          iy+2*(n+1)*(m+1);iy+2*(n+1)*(m+1);iy+2*(n+1)*(m+1);iy+2*(n+1)
268
                       +1)*(m+1);
                         iy+3*(n+1)*(m+1); iy+3*(n+1)*(m+1)*(m+1); iy+3*(n+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)
269
                       +1)*(m+1)];
270 B = BMatrix();
271
272 Adj(Adj == 0) = nan;
273 NanAdj = ~isnan(Adj);
274 NanAdj = NanAdj';
276 a = 1:9;
277 b = repelem(a, size(Adj,1),1);
_{278} b = b';
_{279} iz = b(NanAdj);
280
281 for i = 1:ns
                  k = 1;
282
                  while (B(Type(ix(i),2),iz(i),k) ~= 0)
283
                                                       = Ms(i) + Mq(B(Type(ix(i),2),iz(i),k),B(Type(ix(i)
                          Ms(i)
                        ,2),iz(i),k+1));
                         Kxxs(i) = Kxxs(i) + Kxxq(B(Type(ix(i),2),iz(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(
                       (i),2),iz(i),k+1));
                         Kxys(i) = Kxys(i) + Kxyq(B(Type(ix(i),2),iz(i),k),B(Type(ix(i),2),iz(i),k))
286
                       (i),2),iz(i),k+1));
                         Kyys(i) = Kyys(i) + Kyyq(B(Type(ix(i),2),iz(i),k),B(Type(ix(i),2),iz(i),k))
                       (i),2),iz(i),k+1));
                         Ms(ns+i)
                                                                 = Ms(ns+i) + Mq(B(Type(ix(i),2),iz(i),k)+4,B(
289
                       Type(ix(i),2),iz(i),k+1);
                         Kxxs(ns+i) = Kxxs(ns+i) + Kxxq(B(Type(ix(i),2),iz(i),k)+4,B
290
                       (Type(ix(i),2),iz(i),k+1));
                          Kxys(ns+i) = Kxys(ns+i) + Kxyq(B(Type(ix(i),2),iz(i),k)+4,B
291
                       (Type(ix(i),2),iz(i),k+1));
                          292
                       (Type(ix(i),2),iz(i),k+1));
293
                          Ms(2*ns+i)
                                                                           = Ms(2*ns+i) + Mq(B(Type(ix(i),2),iz(i),k)+8,B
294
                       (Type(ix(i),2),iz(i),k+1));
                         Kxxs(2*ns+i) = Kxxs(2*ns+i) + Kxxq(B(Type(ix(i),2),iz(i),k)
295
                       +8,B(Type(ix(i),2),iz(i),k+1));
                          Kxys(2*ns+i) = Kxys(2*ns+i) + Kxyq(B(Type(ix(i),2),iz(i),k)
296
                       +8,B(Type(ix(i),2),iz(i),k+1));
```

```
Kyys(2*ns+i) = Kyys(2*ns+i) + Kyyq(B(Type(ix(i),2),iz(i),k)
297
     +8,B(Type(ix(i),2),iz(i),k+1));
298
      Ms(3*ns+i)
                   = Ms(3*ns+i) + Mq(B(Type(ix(i),2),iz(i),k)+12,
299
     B(Type(ix(i),2),iz(i),k+1));
      Kxxs(3*ns+i) = Kxxs(3*ns+i) + Kxxq(B(Type(ix(i),2),iz(i),k)
300
     +12,B(Type(ix(i),2),iz(i),k+1));
      Kxys(3*ns+i) = Kxys(3*ns+i) + Kxyq(B(Type(ix(i),2),iz(i),k)
301
     +12,B(Type(ix(i),2),iz(i),k+1));
      Kyys(3*ns+i) = Kyys(3*ns+i) + Kyyq(B(Type(ix(i),2),iz(i),k)
302
     +12,B(Type(ix(i),2),iz(i),k+1));
303
   305
      Ms(4*ns+i)
                 = Ms(4*ns+i) + Mq(B(Type(ix(i),2),iz(i),k),B(
     Type(ix(i),2),iz(i),k+1)+4);
      Kxxs(4*ns+i) = Kxxs(4*ns+i) + Kxxq(B(Type(ix(i),2),iz(i),k)
306
      ,B(Type(ix(i),2),iz(i),k+1)+4);
      Kxys(4*ns+i) = Kxys(4*ns+i) + Kxyq(B(Type(ix(i),2),iz(i),k)
307
      ,B(Type(ix(i),2),iz(i),k+1)+4);
      Kyys(4*ns+i) = Kyys(4*ns+i) + Kyyq(B(Type(ix(i),2),iz(i),k)
308
      ,B(Type(ix(i),2),iz(i),k+1)+4);
309
                  = Ms(5*ns+i) + Mq(B(Type(ix(i),2),iz(i),k)+4,B
      Ms(5*ns+i)
310
     (Type(ix(i),2),iz(i),k+1)+4);
      Kxxs(5*ns+i) = Kxxs(5*ns+i) + Kxxq(B(Type(ix(i),2),iz(i),k)
311
     +4, B(Type(ix(i),2), iz(i), k+1)+4);
      Kxys(5*ns+i) = Kxys(5*ns+i) + Kxyq(B(Type(ix(i),2),iz(i),k)
312
     +4, B(Type(ix(i),2),iz(i),k+1)+4);
      Kyys(5*ns+i) = Kyys(5*ns+i) + Kyyq(B(Type(ix(i),2),iz(i),k)
313
     +4, B(Type(ix(i),2), iz(i),k+1)+4);
314
      Ms(6*ns+i)
                   = Ms(6*ns+i) + Mq(B(Type(ix(i),2),iz(i),k)+8,B
     (Type(ix(i),2),iz(i),k+1)+4);
      Kxxs(6*ns+i) = Kxxs(6*ns+i) + Kxxq(B(Type(ix(i),2),iz(i),k)
316
     +8,B(Type(ix(i),2),iz(i),k+1)+4);
      Kxys(6*ns+i) = Kxys(6*ns+i) + Kxyq(B(Type(ix(i),2),iz(i),k)
317
     +8,B(Type(ix(i),2),iz(i),k+1)+4);
      318
     +8,B(Type(ix(i),2),iz(i),k+1)+4);
319
      Ms(7*ns+i)
                  = Ms(7*ns+i) + Mq(B(Type(ix(i),2),iz(i),k)+12,
320
     B(Type(ix(i),2),iz(i),k+1)+4);
      Kxxs(7*ns+i) = Kxxs(7*ns+i) + Kxxq(B(Type(ix(i),2),iz(i),k)
     +12, B(Type(ix(i),2),iz(i),k+1)+4);
      Kxys(7*ns+i) = Kxys(7*ns+i) + Kxyq(B(Type(ix(i),2),iz(i),k)
322
     +12, B(Type(ix(i),2),iz(i),k+1)+4);
      Kyys(7*ns+i) = Kyys(7*ns+i) + Kyyq(B(Type(ix(i),2),iz(i),k)
     +12, B(Type(ix(i),2),iz(i),k+1)+4);
```

```
324
   325
                   = Ms(8*ns+i) + Mq(B(Type(ix(i),2),iz(i),k),B(
326
      Ms(8*ns+i)
     Type(ix(i),2),iz(i),k+1)+8);
      Kxxs(8*ns+i) = Kxxs(8*ns+i) + Kxxq(B(Type(ix(i),2),iz(i),k)
327
      ,B(Type(ix(i),2),iz(i),k+1)+8);
      Kxys(8*ns+i) = Kxys(8*ns+i) + Kxyq(B(Type(ix(i),2),iz(i),k)
      ,B(Type(ix(i),2),iz(i),k+1)+8);
      Kyys(8*ns+i) = Kyys(8*ns+i) + Kyyq(B(Type(ix(i),2),iz(i),k)
      ,B(Type(ix(i),2),iz(i),k+1)+8);
      Ms(9*ns+i)
                  = Ms(9*ns+i) + Mq(B(Type(ix(i),2),iz(i),k)+4,B
      (Type(ix(i),2),iz(i),k+1)+8);
      Kxxs(9*ns+i) = Kxxs(9*ns+i) + Kxxq(B(Type(ix(i),2),iz(i),k)
332
     +4, B(Type(ix(i),2), iz(i),k+1)+8);
      Kxys(9*ns+i) = Kxys(9*ns+i) + Kxyq(B(Type(ix(i),2),iz(i),k)
333
     +4, B(Type(ix(i),2), iz(i),k+1)+8);
      Kyys(9*ns+i) = Kyys(9*ns+i) + Kyyq(B(Type(ix(i),2),iz(i),k)
334
     +4, B(Type(ix(i),2), iz(i),k+1)+8);
335
      Ms(10*ns+i)
                    = Ms(10*ns+i) + Mq(B(Type(ix(i),2),iz(i),k)
336
     +8,B(Type(ix(i),2),iz(i),k+1)+8);
      Kxxs(10*ns+i) = Kxxs(10*ns+i) + Kxxq(B(Type(ix(i),2),iz(i),
     k)+8,B(Type(ix(i),2),iz(i),k+1)+8);
      Kxys(10*ns+i) = Kxys(10*ns+i) + Kxyq(B(Type(ix(i),2),iz(i),
338
     k)+8,B(Type(ix(i),2),iz(i),k+1)+8);
      Kyys(10*ns+i) = Kyys(10*ns+i) + Kyyq(B(Type(ix(i),2),iz(i),
339
     k)+8,B(Type(ix(i),2),iz(i),k+1)+8);
340
                    = Ms(11*ns+i) + Mq(B(Type(ix(i),2),iz(i),k)
      Ms(11*ns+i)
     +12,B(Type(ix(i),2),iz(i),k+1)+8);
      Kxxs(11*ns+i) = Kxxs(11*ns+i) + Kxxq(B(Type(ix(i),2),iz(i),
     k)+12,B(Type(ix(i),2),iz(i),k+1)+8);
      Kxys(11*ns+i) = Kxys(11*ns+i) + Kxyq(B(Type(ix(i),2),iz(i),
343
     k)+12,B(Type(ix(i),2),iz(i),k+1)+8);
      Kyys(11*ns+i) = Kyys(11*ns+i) + Kyyq(B(Type(ix(i),2),iz(i),
344
     k)+12,B(Type(ix(i),2),iz(i),k+1)+8);
       345
                   = Ms(12*ns+i) + Mq(B(Type(ix(i),2),iz(i),k),B
      Ms(12*ns+i)
346
      (Type(ix(i),2),iz(i),k+1)+12);
      Kxxs(12*ns+i) = Kxxs(12*ns+i) + Kxxq(B(Type(ix(i),2),iz(i),
     k), B(Type(ix(i),2),iz(i),k+1)+12);
      Kxys(12*ns+i) = Kxys(12*ns+i) + Kxyq(B(Type(ix(i),2),iz(i),
     k),B(Type(ix(i),2),iz(i),k+1)+12);
      Kyys(12*ns+i) = Kyys(12*ns+i) + Kyyq(B(Type(ix(i),2),iz(i),
349
     k), B(Type(ix(i),2),iz(i),k+1)+12);
350
```

```
Ms(13*ns+i) = Ms(13*ns+i) + Mq(B(Type(ix(i),2),iz(i),k)
351
             +4, B(Type(ix(i),2), iz(i),k+1)+12);
               Kxxs(13*ns+i) = Kxxs(13*ns+i) + Kxxq(B(Type(ix(i),2),iz(i),
352
             k)+4,B(Type(ix(i),2),iz(i),k+1)+12);
               Kxys(13*ns+i) = Kxys(13*ns+i) + Kxyq(B(Type(ix(i),2),iz(i),
353
             k)+4,B(Type(ix(i),2),iz(i),k+1)+12);
               Kyys(13*ns+i) = Kyys(13*ns+i) + Kyyq(B(Type(ix(i),2),iz(i),
             k)+4,B(Type(ix(i),2),iz(i),k+1)+12);
               Ms(14*ns+i)
                                              = Ms(14*ns+i) + Mq(B(Type(ix(i),2),iz(i),k)
356
             +8,B(Type(ix(i),2),iz(i),k+1)+12);
               Kxxs(14*ns+i) = Kxxs(14*ns+i) + Kxxq(B(Type(ix(i),2),iz(i),
357
             k)+8,B(Type(ix(i),2),iz(i),k+1)+12);
              Kxys(14*ns+i) = Kxys(14*ns+i) + Kxyq(B(Type(ix(i),2),iz(i),
358
             k)+8,B(Type(ix(i),2),iz(i),k+1)+12);
               Kyys(14*ns+i) = Kyys(14*ns+i) + Kyyq(B(Type(ix(i),2),iz(i),
359
             k)+8,B(Type(ix(i),2),iz(i),k+1)+12);
360
              Ms(15*ns+i)
                                              = Ms(15*ns+i) + Mq(B(Type(ix(i),2),iz(i),k)
361
             +12, B(Type(ix(i),2),iz(i),k+1)+12);
              Kxxs(15*ns+i) = Kxxs(15*ns+i) + Kxxq(B(Type(ix(i),2),iz(i),
362
             k)+12,B(Type(ix(i),2),iz(i),k+1)+12);
              Kxys(15*ns+i) = Kxys(15*ns+i) + Kxyq(B(Type(ix(i),2),iz(i),
363
            k)+12, B(Type(ix(i),2),iz(i),k+1)+12);
              Kyys(15*ns+i) = Kyys(15*ns+i) + Kyyq(B(Type(ix(i),2),iz(i),
364
             k)+12,B(Type(ix(i),2),iz(i),k+1)+12);
365
               k = k + 2;
               if(k > 8)
367
                      break;
               end
369
          end
     end
               = sparse(x,y,Ms,4*(n+1)*(m+1),4*(n+1)*(m+1));
372 M
373 Kxx = sparse(x,y,Kxxs,4*(n+1)*(m+1),4*(n+1)*(m+1));
||X|| ||X|| = ||S|| ||
375 Kyy = sparse(x,y,Kyys,4*(n+1)*(m+1),4*(n+1)*(m+1));
376 return;
378 function B = BMatrix()
_{379} B = zeros(9,9,8);
B(3,1,:) = [2 2 0 0 0 0 0];
B(3,2,:) = [2 \ 3 \ 0 \ 0 \ 0 \ 0];
B(3,3,:) = [0 \ 0 \ 0 \ 0 \ 0 \ 0];
B(3,4,:) = [0 \ 0 \ 0 \ 0 \ 0 \ 0];
B(3,5,:) = [0 \ 0 \ 0 \ 0 \ 0 \ 0];
B(3,6,:) = [0 \ 0 \ 0 \ 0 \ 0 \ 0];
B(3,7,:) = [0 \ 0 \ 0 \ 0 \ 0 \ 0];
```

```
B(3,8,:) = [2 1 0 0 0 0 0];
  B(3,9,:) = [2 4 0 0 0 0 0 0];
390
  B(2,1,:) = [2 2 3 3 0 0 0 0];
  B(2,2,:) = [2 3 0 0 0 0 0 0];
391
B(2,3,:) = [0 \ 0 \ 0 \ 0 \ 0]
  B(2,4,:) = [0 \ 0 \ 0 \ 0 \ 0 \ 0];
  B(2,5,:) = [0 \ 0 \ 0 \ 0 \ 0 \ 0];
394
B(2,6,:) = [3 2 0 0 0 0 0];
  B(2,7,:) = [3 1 0 0 0 0 0 0];
396
  B(2,8,:) = [2 1 3 4 0 0 0 0];
  B(2,9,:) = [2 4 0 0 0 0 0 0];
398
B(1,1,:) = [3 \ 3 \ 0 \ 0 \ 0 \ 0];
B(1,2,:) = [0 \ 0 \ 0 \ 0 \ 0 \ 0];
A_{02} B(1,3,:) = [0 0 0 0 0 0 0];
B(1,4,:) = [0 \ 0 \ 0 \ 0 \ 0 \ 0];
B(1,5,:) = [0 \ 0 \ 0 \ 0 \ 0 \ 0];
  B(1,6,:) = [3 2 0 0 0 0 0 0];
405
B(1,7,:) = [3 1 0 0 0 0 0];
407 B(1,8,:) = [3 4 0 0 0 0 0 0];
B(1,9,:) = [0 \ 0 \ 0 \ 0 \ 0 \ 0];
409
B(6,1,:) = [1 1 2 2 0 0 0 0];
B(6,2,:) = [1 \ 4 \ 2 \ 3 \ 0 \ 0 \ 0];
B(6,3,:) = [1 \ 3 \ 0 \ 0 \ 0 \ 0];
B(6,4,:) = [1 2 0 0 0 0 0];
B(6,5,:) = [0 \ 0 \ 0 \ 0 \ 0 \ 0];
B(6,6,:) = [0 \ 0 \ 0 \ 0 \ 0 \ 0];
B(6,7,:) = [0 \ 0 \ 0 \ 0 \ 0 \ 0];
  B(6,8,:) = [2 1 0 0 0 0 0];
417
B(6,9,:) = [2 4 0 0 0 0 0];
  B(5,1,:) = [1 1 2 2 3 3 4 4];
420
B(5,2,:) = [1 4 2 3 0 0 0 0];
422 B(5,3,:) = [1 3 0 0 0 0 0];
B(5,4,:) = [1 2 4 3 0 0 0 0];
  B(5,5,:) = [4 2 0 0 0 0 0];
B(5,6,:) = [4 1 3 2 0 0 0 0];
426 B(5,7,:) = [3 1 0 0 0 0 0 0];
  B(5,8,:) = [3 4 2 1 0 0 0 0];
427
B(5,9,:) = [2 4 0 0 0 0 0];
B(4,1,:) = [3 3 4 4 0 0 0 0];
B(4,2,:) = [0 \ 0 \ 0 \ 0 \ 0 \ 0];
B(4,3,:) = [0 0 0 0 0 0 0];
B(4,4,:) = [4 \ 3 \ 0 \ 0 \ 0 \ 0];
B(4,5,:) = [4 2 0 0 0 0 0];
```

```
B(4,6,:) = [4 1 3 2 0 0 0 0];
436 B(4,7,:) = [3 1 0 0 0 0 0];
B(4,8,:) = [3 4 0 0 0 0 0];
B(4,9,:) = [0 \ 0 \ 0 \ 0 \ 0 \ 0];
B(9,1,:) = [1 \ 1 \ 0 \ 0 \ 0 \ 0];
  B(9,2,:) = [1 4 0 0 0 0 0 0];
  B(9,3,:) = [1 \ 3 \ 0 \ 0 \ 0 \ 0
                              0];
B(9,4,:) = [1 2 0 0 0 0 0];
B(9,5,:) = [0 \ 0 \ 0 \ 0 \ 0 \ 0];
  B(9,6,:) = [0 \ 0 \ 0 \ 0 \ 0 \ 0];
B(9,7,:) = [0 \ 0 \ 0 \ 0 \ 0 \ 0];
447 B(9,8,:) = [0 0 0 0 0 0 0 0];
B(9,9,:) = [0 \ 0 \ 0 \ 0 \ 0 \ 0];
B(8,1,:) = [1 1 4 4 0 0 0 0];
B(8,2,:) = [1 4 0 0 0 0 0];
B(8,3,:) = [1 \ 3 \ 0 \ 0 \ 0 \ 0];
  B(8,4,:) = [1 2 4 3 0 0]
453
                            0 0];
B(8,5,:) = [4 2 0 0 0 0 0];
B(8,6,:) = [4 1 0 0 0 0 0];
B(8,7,:) = [0 \ 0 \ 0 \ 0 \ 0 \ 0];
  B(8,8,:) = [0 \ 0 \ 0 \ 0 \ 0 \ 0];
B(8,9,:) = [0 \ 0 \ 0 \ 0 \ 0 \ 0];
459
  B(7,1,:) = [4 \ 4 \ 0 \ 0 \ 0 \ 0 \ 0];
460
B(7,2,:) = [0 \ 0 \ 0 \ 0 \ 0 \ 0];
B(7,3,:) = [0 0 0 0 0 0 0];
B(7,4,:) = [4 \ 3 \ 0 \ 0 \ 0 \ 0];
B(7,5,:) = [4 2 0 0 0 0 0];
  B(7,6,:) = [4 1 0 0 0 0 0 0];
B(7,7,:) = [0 \ 0 \ 0 \ 0 \ 0 \ 0];
  B(7,8,:) = [0 \ 0 \ 0 \ 0 \ 0 \ 0];
467
  B(7,9,:) = [0 \ 0 \ 0 \ 0 \ 0 \ 0];
468
469 return;
471 function T = MATRIX_T(Q)
  syms x;
472
  syms y;
473
474
  n = size(Q,2);
475
476
T = zeros(n);
  for j = 1:n
478
     T(j,1) = subs(Q(j),[x,y],[0,0]);
479
     T(j,2) = subs(Q(j),[x,y],[1,0]);
480
     T(j,3) = subs(Q(j),[x,y],[1,1]);
     T(j,4) = subs(Q(j),[x,y],[0,1]);
482
```

```
if(n > 4)
      T(j,5) = subs(diff(Q(j),x),[x,y],[0,0]);
484
      T(j,6) = subs(diff(Q(j),x),[x,y],[1,0]);
      T(j,7) = subs(diff(Q(j),x),[x,y],[1,1]);
486
      T(j,8) = subs(diff(Q(j),x),[x,y],[0,1]);
488
      if(n > 8)
      T(j,9) = subs(diff(Q(j),y),[x,y],[0,0]);
490
      T(j,10) = subs(diff(Q(j),y),[x,y],[1,0]);
      T(j,11) = subs(diff(Q(j),y),[x,y],[1,1]);
492
      T(j,12) = subs(diff(Q(j),y),[x,y],[0,1]);
      end
494
      if(n > 12)
496
      T(j,13) = subs(diff(diff(Q(j),y),x),[x,y],[0,0]);
      T(j,14) = subs(diff(diff(Q(j),y),x),[x,y],[1,0]);
      T(j,15) = subs(diff(diff(Q(j),y),x),[x,y],[1,1]);
      T(j,16) = subs(diff(diff(Q(j),y),x),[x,y],[0,1]);
      end
500
501
  end
502 T = T';
  return
504
   function E = Positions(m,n,dx,dy)
       E = zeros((n+1)*(m+1),2);
       ix = n+1;
507
       iy = m+1;
       for i = 1:(n+1)*(m+1)
509
           E(i,:) = [dx*(ix-1),dy*(iy-1)];
           iy = iy-1;
           if(iy == 0)
               iy = m+1;
               ix = ix -1;
           end
       %[Cubes, CubeNumbers] = CreateCubes(E,N);
       %Plot(E,N,Cubes)
  return
```

Example code for Reissner-Mindlin plate model using bi-cubics

```
%function [E,wP,xP,yP,size_c] = PlateCantileverCubic(d,n,h,inum, numEig)

function [E,n,m] = PlateCantileverCubic(d,n,h,inum,numEig)
```

```
3 format long g
_{4} m = ceil(n*d);
5 a = 0;
_{6} b = 1;
  c = 0;
9 %h = sqrt(12/alpha);
_{10} %d = 1;
deltx = (b-a)/n;
delty = (d-c)/m;
14 | size_c = (n+1)*(m+1);
_{16} nu = 0.3;
18 \text{ kappa_b} = (5/6);
^{19} kappa_p = 0.9554; ^{\circ}0.29738*nu + 0.763932;
20
_{21}|I = (h^3)/12;
22 beta = kappa_b/((2*(1+nu))*I); %*alpha; %0.3846*kappa_p/I
23 A = 1/(beta*(1-nu^2));
_{24} B = 1/(2*beta*(1+nu));
[MM, Kxx, Kxy, Kyy, Lx, Ly, Edge] = CalMatrix(n, m, deltx, delty);
_{27} LxT = Lx';
_{28} LyT = Ly';
29 Kyx = Kxy'; %CHECKED
30 0 = sparse(size(MM,1), size(MM,2));
Mu = [MM \ O \ O; \ O \ I*MM \ O; \ O \ O \ I*MM];
32 Ku = [Kxx+Kyy LxT LyT; h*Lx A*Kxx+B*Kyy+h*MM A*nu*Kyx+B*Kxy; h*
     Ly A*nu*Kxy+B*Kyx A*Kyy+B*Kxx+h*MM]; %The correct one!
33 Ku = [Kxx+Kyy Lx Ly; h*LxT A*Kxx+B*Kyy+h*MM A*nu*Kxy+B*Kyx; h*
      LyT A*nu*Kyx+B*Kxy A*Kyy+B*Kxx+h*MM];%The not correct one!
34 \mid \%Ku = [h*(Kxx+Kyy) h*Lx h*Ly; h*LxT A*Kxx+B*Kyy+h*MM A*nu*Kxy+B
      *Kyx; h*LyT A*nu*Kyx+B*Kxy A*Kyy+B*Kxx+h*MM];
Mq = [MM \ O \ O; \ O \ O; \ O \ O];
_{36}|F = zeros(size(Mu,1),1);
F(1:(m+1),1) = 0.01;
38 \times = [];
_{40} for i = [0 2 4 6 8 10]
      x = [x; Edge+(i)*(m+1)*(n+1)];
41
43 | Mu(x,:) = [];
44 | Mu(:,x) = [];
45 | Ku(x,:) = [];
_{46} | Ku(:,x) = [];
47 | Mq(x,:) = [];
```

```
49 [R,p,s] = chol(Mu,'vector');
[V,DE,flag] = eigs(Ku,R,numEig,'smallestabs','IsCholesky',true,
      'CholeskyPermutation',s,'Tolerance',1e-4);
51 E = diag(DE);
52
53 %[V,D] = eigs(Ku,Mu,numEig,'sm');
54 \%E = diag(D);
55 | \%V = V(:,E>=0);
56 | \%E = E(E>=0);
58 %tic
59 %Kug = gpuArray(Ku);
60 %bg = gpuArray(Mq*(F));
62 %ueq = gather(u);
64 %toc
65 \text{WP} = [\text{ueq}(1:(m+1)*(n+1)-(m+1),1); zeros(m+1,1)];
67 %inum = 1
68 WP = zeros(inum, (m+1)*(n+1));
69 \% wP(1,:) = [ueq(1:(m+1)*(n+1)-(m+1),1); zeros(m+1,1)];
_{70} for i = inum:-1:1
v_1 | w = V(:,i);
72 tic
73 Kug = gpuArray(Ku);
74 bg = gpuArray(Mu*(w));
u = gmres(Kug, bg, 30, 1e-4, 30);
76 ueq = gather(u);
78 \mid \% bg = Mu*(w);
79 %ueq = gmres(Ku,bg,30,1e-4,30);
80
P(i,:) = [ueq(1:(m+1)*(n+1)-(m+1),1); zeros(m+1,1)];
83 end
85 icx = b;
s_6 icy = d;
87 icount = 1;
88 xP = zeros(1,(n+1)*(m+1));
89 yP = zeros(1,(n+1)*(m+1));
90 | for i = 1:n+1
     for j = 1:m+1
        xP(1,icount) = icx;
92
        yP(1, icount) = icy;
        icy = icy - delty;
94
```

```
icount = icount + 1;
96
      icx = icx - deltx;
97
98
      icy = d;
   end
99
100
101 %for i = inum:-1:1
102 %figure();
103 %scatter3(xP(1,:),yP(1,:),wP(i,:));
104 %end
105
106
107 %}
108 \% W = V(:,8);
110 Kyx = Kxy'; %CHECKED
^{111} %All = (n+1)*(m+1);
113 \% K1 = Kxx + (1-nu)/2*Kyy;
114 %K2 = nu*Kyx + (1-nu)/2*Kxy;
_{115} %K3 = nu*Kxy + (1-nu)/2*Kyx;
116 \% K4 = Kyy + (1-nu)/2*Kxx;
117 %0 = sparse(size(MM,1),size(MM,2)); %CHECKED
118 %MMu = [MM O; %CHECKED
119 %
            O MM]; % CHECKED
_{120} %Mf = MMu;
121 %K = 1/(gamma*(1-nu^2))*[K1 K2; K3 K4];%CHECKED
122 \%x = [7*All:-1:7*All-(m+1)+1 5*All:-1:5*All-(m+1)+1 3*All:-1:3*
      All-(m+1)+1 1*All:-1:1*All-(m+1)+1];
123 \% K(x,:) = [];
_{124} %K(:,x) = [];
125 \% MMu(x,:) = [];
126 \% MMu(:,x) = [];
127 \text{ %Mf(x,:)} = [];
128 %CHECKED
129 %eig(Mu,K)
130 %[V,D] = eigs(K,MMu,10,'sm');
131 %E = diag(D);
_{132} %w = V(:,8);
133
134
135
136
137 %ueq = Ku\Mu*(-w)
_{139} %b = Mf * (-F);
140 %tic
```

```
142 %toc
143
144 % {
145 tic
146 tol = 0.0001;
_{147} maxit = 300000;
alpha1 = \max(sum(abs(K), 2)./diag(K))-2;
149 L = ichol(K, struct('type', 'ict', 'droptol', 1e-3, 'diagcomp',
      alpha1));
150 | %ueq = pcg(K,b,tol,maxit,L,L');
151 toc
Ep = Positions(m,n,deltx,delty);
154 \text{ %ux} = 0;
155 \% uy = 0;
ux = [ueq(1:(n+1)*(m+1)-(m+1),1); zeros(m+1,1)] + Ep(:,1);
|| dxux = [ueq((n+1)*(m+1)-(m+1)+1:2*(n+1)*(m+1)-(m+1),1)];
dyux = [ueq(2*(n+1)*(m+1)-(m+1)+1:3*(n+1)*(m+1)-2*(m+1),1);
      zeros (m+1,1)];
| dxyux = [ueq(3*(n+1)*(m+1)-2*(m+1)+1:4*(n+1)*(m+1)-2*(m+1),1)];
160 uy = [ueq(4*(n+1)*(m+1)-2*(m+1)+1:5*(n+1)*(m+1)-3*(m+1),1);
      zeros(m+1,1)] + Ep(:,2);
161 dxuy = [ueq(5*(n+1)*(m+1)-3*(m+1)+1:6*(n+1)*(m+1)-3*(m+1),1)];
162 dyuy = [ueq(6*(n+1)*(m+1)-3*(m+1)+1:7*(n+1)*(m+1)-4*(m+1),1);
      zeros(m+1,1)];
  dxyuy = [ueq(7*(n+1)*(m+1)-4*(m+1)+1:8*(n+1)*(m+1)-4*(m+1),1)];
164
ux = flip(ux);
166 dxux = flip(dxux);
dyux = flip(dyux);
168 dxyux = flip(dxyux);
uy = flip(uy);
170 dxuy = flip(dxuy);
dyuy = flip(dyuy);
dxyuy = flip(dxyuy);
173
stress = ceil((n+1)/2);
175 figure();
scatter(ux,uy);
|sigma11| = 1/(gamma*(1-nu^2))*(dxux + nu*dyuy);
| sigma22 = 1/(gamma*(1-nu^2))*(dyuy + nu*dxux);
| sigma12 = 1/(2*gamma*(1+nu))*(dyux + dyux);
180
  T = [sigma11(stress) sigma12(stress); sigma12(stress) sigma22(
181
      stress)];
182 %}
183 return;
184
```

```
185 function [Mq, Kxxq, Kxyq, Kyyq, Lxq, Lyq] = matrix(deltx, delty)%
                         CHECKED
186
           syms x;
           syms y;
187
188
           Q = [1 \times x^2 \times x^3 \times x^2 \times x^2 \times x^3 \times y^2 \times x^2 \times y^2 \times x^3 \times y^2 \times y^3 \times y
189
                         ^3 x*y^3 x^2*y^3 x^3*y^3];
190
191 \%size_num = size(Q,2)/4;
_{192} T = MATRIX_T(Q);
193
                            = zeros(size(Q,2))*x*y;
194 Mq
195 Kxxq = zeros(size(Q,2))*x*y;
196 Kxyq = zeros(size(Q,2))*x*y;
197 Kyyq = zeros(size(Q,2))*x*y;
198 Lxq = zeros(size(Q,2))*x*y;
Lyq = zeros(size(Q,2))*x*y;
200
           for i = 1: size(Q, 2)
201
                            for j = 1:size(Q,2)
202
                                             Mq(j,i)
                                                                               = Q(j)*Q(i);
203
                                              Kxxq(j,i) = diff(Q(j),x)*diff(Q(i),x);
204
                                              Kxyq(j,i) = diff(Q(j),y)*diff(Q(i),x);
205
                                              Kyyq(j,i) = diff(Q(j),y)*diff(Q(i),y);
                                              Lxq(j,i) = Q(j)*diff(Q(i),x);
207
                                              Lyq(j,i) = Q(j)*diff(Q(i),y);
                            end
209
210 end
211 Mq = int(int(Mq,x,0,1),y,0,1);
212 | Kxxq = int(int(Kxxq,x,0,1),y,0,1);
213 Kxyq = int(int(Kxyq,x,0,1),y,0,1);
214 Kyyq = int(int(Kyyq,x,0,1),y,0,1);
Lxq = int(int(Lxq,x,0,1),y,0,1);
216 Lyq = int(int(Lyq,x,0,1),y,0,1);
217
218 IT = inv(T);
219
_{220} Mq = (IT) '*Mq*IT;
221 | Kxxq = (IT)'*Kxxq*IT;
222 | Kxyq = (IT)'*Kxyq*IT;
223 Kyyq = (IT) '*Kyyq*IT;
224 Lxq = (IT) '*Lxq*IT;
Lyq = (IT)'*Lyq*IT;
226
227 Mq = double(Mq*deltx*delty);
228 Kxxq = double(Kxxq*delty/deltx);
229 Kyyq = double(Kyyq*deltx/delty);
230 Kxyq = double(Kxyq);
```

```
Lxq = double(Lxq*delty);
232 Lyq = double(Lyq*deltx);
233 return;
234
function [Adj, Type, Edge] = Domain(n,m)
_{236} D = zeros(m+1, n+1);
237 icount = 1;
  for i = n+1:-1:1
238
      for j = 1:m+1
          D(j,i) = icount;
240
          icount = icount + 1;
      end
242
243 end
244 %D
245 Edge1 = [];
246 Edge2 = [];
247 Edge3 = [];
248 \text{ Edge4} = [];
249 Edge1 = (D(:,1));
250 %Edge2 = (D(m+1,:)');
251 %Edge3 = (D(:,n+1));
252 %Edge4 = (D(1,:)');
Edge = sort(unique([Edge1; Edge2; Edge3; Edge4]));
255 %Edge
  D0 = [zeros(1,n+3); zeros(m+1,1) D zeros(m+1,1); zeros(1,n+3)];
257
259 icount = 1;
  Adj = zeros((n+1)*(m+1),9);
  for i = n+2:-1:2
      for j = 2:m+2
      Adj(icount,1) = DO(j,i); %middel
263
      Adj(icount,2) = DO(j-1,i); %bo
      Adj(icount,3) = DO(j-1,i+1); %regsbo
265
      Adj(icount,4) = DO(j,i+1); %regs
266
      Adj(icount,5) = DO(j+1,i+1); %regs onder
267
      Adj(icount,6) = DO(j+1,i); %onder
268
      Adj(icount,7) = DO(j+1,i-1); %links onder
269
      Adj(icount,8) = DO(j,i-1); %links
270
      Adj(icount,9) = DO(j-1,i-1); %linksbo
      icount = icount +1;
272
      end
273
  Type= zeros((n+1)*(m+1),2);
_{276} | T = [1]
                                   0
                                          2
                                                5
                                                       4
                                                              0;
               0
                     0
                            0
                     0
                            0
                                   0
                                                       5
        2
               1
                                          3
                                                6
                                                              4;
        3
               2
                     0
                                   0
                                                       6
                                                              5;
278
```

```
4
                0
                       0
                              1
                                     2
                                            5
                                                    8
                                                           7
                                                                  0;
279
         5
                4
                              2
                                     3
                                                    9
                       1
                                             6
                                                           8
                                                                  7;
280
         6
                5
                       2
                              3
                                     0
                                             0
                                                    0
                                                           9
                                                                  8;
281
         7
                0
                       0
                              4
                                     5
                                            8
                                                    0
                                                           0
                                                                  0;
282
         8
                7
                       4
                              5
                                     6
                                            9
                                                    0
                                                           0
                                                                  0;
283
                       5
                              6
         9
                                     0
                                             0
                                                    0
                                                           0
                                                                  0];
284
    nnz(T);
285
286
   for i = 1:(n+1)*(m+1)
      Type(i,1) = Adj(i,1);
288
      for j = 1:9
289
           bflag = true;
290
           for k = 1:9
                if(any(T(j,k)) ~= any(Adj(i,k)))
292
                     bflag = false;
                end
294
           end
           if(bflag == true)
296
297
               Type(i,2) = j;
           end
298
      end
299
   end
300
   return
301
   function [M, Kxx, Kxy, Kyy, Lx, Ly, Edge] = CalMatrix(n, m, deltx, delty
303
   [Adj, Type, Edge] = Domain(n,m);
304
   [Mq, Kxxq, Kxyq, Kyyq, Lxq, Lyq] = matrix(deltx, delty);
306
  ns = nnz(Adj);
308 Ms = zeros(16*ns,1);
_{309} | Kxxs = zeros(16*ns,1);
_{310} Kxys = _{zeros}(16*ns,1);
   Kyys = zeros(16*ns,1);
311
| Lxs = zeros(16*ns,1); 
313 Lys = zeros(16*ns,1);
   x = [1:(n+1)*(m+1)]';
315
   c = sum(Adj^-=0,2);
316
317
   ix = repelem(x,c);
   x = [ix; ix+(n+1)*(m+1); ix+2*(n+1)*(m+1); ix+3*(n+1)*(m+1);
319
       ix; ix+(n+1)*(m+1); ix+2*(n+1)*(m+1); ix+3*(n+1)*(m+1);
       ix; ix+(n+1)*(m+1); ix+2*(n+1)*(m+1); ix+3*(n+1)*(m+1);
321
       ix; ix+(n+1)*(m+1); ix+2*(n+1)*(m+1); ix+3*(n+1)*(m+1);];
323
324 iy = nonzeros(Adj');
325 y = [iy;iy;iy;iy;
```

```
iy+(n+1)*(m+1);iy+(n+1)*(m+1);iy+(n+1)*(m+1);iy+(n+1)*(m+1)
326
                                          iy+2*(n+1)*(m+1); iy+2*(n+1)*(m+1); iy+2*(n+1)*(m+1); iy+2*(n+1)*(m+1)
327
                                      +1)*(m+1);
                                           iy+3*(n+1)*(m+1); iy+3*(n+1)*(m+1)*(m+1); iy+3*(n+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)*(m+1)
                                      +1)*(m+1)];
                B = BMatrix();
330
331 Adj(Adj == 0) = nan;
332 NanAdj = ~isnan(Adj);
333 NanAdj = NanAdj';
334
335 a = 1:9;
b = repelem(a, size(Adj, 1), 1);
337 b = b';
iz = b(NanAdj);
_{340} for i = 1:ns
341
                             k = 1;
                              while (B(Type(ix(i),2),iz(i),k) = 0)
                                                                                         = Ms(i) + Mq(B(Type(ix(i),2),iz(i),k),B(Type(ix(i))
343
                                        ,2),iz(i),k+1));
                                           Kxxs(i) = Kxxs(i) + Kxxq(B(Type(ix(i),2),iz(i),k),B(Type(ix
                                      (i),2),iz(i),k+1));
                                         Kxys(i) = Kxys(i) + Kxyq(B(Type(ix(i),2),iz(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(
345
                                      (i),2),iz(i),k+1));
                                          Kyys(i) = Kyys(i) + Kyyq(B(Type(ix(i),2),iz(i),k),B(Type(ix(i),2),iz(i),k))
346
                                       (i),2),iz(i),k+1));
                                          Lxs(i) = Lxs(i) + Lxq(B(Type(ix(i),2),iz(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),
                                        ,2),iz(i),k+1));
                                         Lys(i) = Lys(i) + Lyq(B(Type(ix(i),2),iz(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),k),B(Type(ix(i),
348
                                        ,2),iz(i),k+1));
349
                                          Ms(ns+i)
                                                                                                                 = Ms(ns+i) + Mq(B(Type(ix(i),2),iz(i),k)+4,B(
350
                                      Type(ix(i),2),iz(i),k+1);
                                          Kxxs(ns+i) = Kxxs(ns+i) + Kxxq(B(Type(ix(i),2),iz(i),k)+4,B
351
                                      (Type(ix(i),2),iz(i),k+1));
                                           Kxys(ns+i) = Kxys(ns+i) + Kxyq(B(Type(ix(i),2),iz(i),k)+4,B
352
                                      (Type(ix(i),2),iz(i),k+1));
                                           Kyys(ns+i) = Kyys(ns+i) + Kyyq(B(Type(ix(i),2),iz(i),k)+4,B
353
                                       (Type(ix(i),2),iz(i),k+1));
                                          Lxs(ns+i) = Lxs(ns+i) + Lxq(B(Type(ix(i),2),iz(i),k)+4,B(
354
                                      Type(ix(i),2),iz(i),k+1);
                                         Lys(ns+i) = Lys(ns+i) + Lyq(B(Type(ix(i),2),iz(i),k)+4,B(
355
                                      Type(ix(i),2),iz(i),k+1);
356
                                           Ms(2*ns+i)
                                                                                                                            = Ms(2*ns+i) + Mq(B(Type(ix(i),2),iz(i),k)+8,B
                                       (Type(ix(i),2),iz(i),k+1));
```

```
Kxxs(2*ns+i) = Kxxs(2*ns+i) + Kxxq(B(Type(ix(i),2),iz(i),k)
358
     +8,B(Type(ix(i),2),iz(i),k+1));
      Kxys(2*ns+i) = Kxys(2*ns+i) + Kxyq(B(Type(ix(i),2),iz(i),k)
359
     +8,B(Type(ix(i),2),iz(i),k+1));
      360
     +8,B(Type(ix(i),2),iz(i),k+1));
      Lxs(2*ns+i) = Lxs(2*ns+i) + Lxq(B(Type(ix(i),2),iz(i),k)+8,
     B(Type(ix(i),2),iz(i),k+1));
      Lys(2*ns+i) = Lys(2*ns+i) + Lyq(B(Type(ix(i),2),iz(i),k)+8,
     B(Type(ix(i),2),iz(i),k+1));
                 = Ms(3*ns+i) + Mq(B(Type(ix(i),2),iz(i),k)+12,
      Ms(3*ns+i)
364
     B(Type(ix(i),2),iz(i),k+1));
      Kxxs(3*ns+i) = Kxxs(3*ns+i) + Kxxq(B(Type(ix(i),2),iz(i),k)
365
     +12,B(Type(ix(i),2),iz(i),k+1));
      Kxys(3*ns+i) = Kxys(3*ns+i) + Kxyq(B(Type(ix(i),2),iz(i),k)
366
     +12,B(Type(ix(i),2),iz(i),k+1));
      Kyys(3*ns+i) = Kyys(3*ns+i) + Kyyq(B(Type(ix(i),2),iz(i),k)
367
     +12,B(Type(ix(i),2),iz(i),k+1));
      Lxs(3*ns+i) = Lxs(3*ns+i) + Lxq(B(Type(ix(i),2),iz(i),k)
     +12,B(Type(ix(i),2),iz(i),k+1));
      Lys(3*ns+i) = Lys(3*ns+i) + Lyq(B(Type(ix(i),2),iz(i),k)
369
     +12,B(Type(ix(i),2),iz(i),k+1));
370
   371
                   = Ms(4*ns+i) + Mq(B(Type(ix(i),2),iz(i),k),B(
      Ms(4*ns+i)
     Type(ix(i),2),iz(i),k+1)+4);
      Kxxs(4*ns+i) = Kxxs(4*ns+i) + Kxxq(B(Type(ix(i),2),iz(i),k)
     ,B(Type(ix(i),2),iz(i),k+1)+4);
      Kxys(4*ns+i) = Kxys(4*ns+i) + Kxyq(B(Type(ix(i),2),iz(i),k)
     ,B(Type(ix(i),2),iz(i),k+1)+4);
      Kyys(4*ns+i) = Kyys(4*ns+i) + Kyyq(B(Type(ix(i),2),iz(i),k)
375
     ,B(Type(ix(i),2),iz(i),k+1)+4);
      Lxs(4*ns+i) = Lxs(4*ns+i) + Lxq(B(Type(ix(i),2),iz(i),k),B(
376
     Type(ix(i),2),iz(i),k+1)+4);
      Lys(4*ns+i) = Lys(4*ns+i) + Lyq(B(Type(ix(i),2),iz(i),k),B(
377
     Type(ix(i),2),iz(i),k+1)+4);
378
                  = Ms(5*ns+i) + Mq(B(Type(ix(i),2),iz(i),k)+4,B
      Ms(5*ns+i)
379
     (Type(ix(i),2),iz(i),k+1)+4);
      Kxxs(5*ns+i) = Kxxs(5*ns+i) + Kxxq(B(Type(ix(i),2),iz(i),k)
380
     +4, B(Type(ix(i),2),iz(i),k+1)+4);
      Kxys(5*ns+i) = Kxys(5*ns+i) + Kxyq(B(Type(ix(i),2),iz(i),k)
     +4, B(Type(ix(i),2),iz(i),k+1)+4);
      Kyys(5*ns+i) = Kyys(5*ns+i) + Kyyq(B(Type(ix(i),2),iz(i),k)
382
     +4, B(Type(ix(i),2), iz(i),k+1)+4);
      Lxs(5*ns+i) = Lxs(5*ns+i) + Lxq(B(Type(ix(i),2),iz(i),k)+4,
     B(Type(ix(i),2),iz(i),k+1)+4);
```

```
Lys(5*ns+i) = Lys(5*ns+i) + Lyq(B(Type(ix(i),2),iz(i),k)+4,
     B(Type(ix(i),2),iz(i),k+1)+4);
385
      Ms(6*ns+i)
                  = Ms(6*ns+i) + Mq(B(Type(ix(i),2),iz(i),k)+8,B
386
     (Type(ix(i),2),iz(i),k+1)+4);
      Kxxs(6*ns+i) = Kxxs(6*ns+i) + Kxxq(B(Type(ix(i),2),iz(i),k)
387
     +8,B(Type(ix(i),2),iz(i),k+1)+4);
      Kxys(6*ns+i) = Kxys(6*ns+i) + Kxyq(B(Type(ix(i),2),iz(i),k)
388
     +8,B(Type(ix(i),2),iz(i),k+1)+4);
      Kyys(6*ns+i) = Kyys(6*ns+i) + Kyyq(B(Type(ix(i),2),iz(i),k)
389
     +8,B(Type(ix(i),2),iz(i),k+1)+4);
      Lxs(6*ns+i) = Lxs(6*ns+i) + Lxq(B(Type(ix(i),2),iz(i),k)+8,
390
     B(Type(ix(i),2),iz(i),k+1)+4);
      Lys(6*ns+i) = Lys(6*ns+i) + Lyq(B(Type(ix(i),2),iz(i),k)+8,
391
     B(Type(ix(i),2),iz(i),k+1)+4);
392
      Ms(7*ns+i)
                  = Ms(7*ns+i) + Mq(B(Type(ix(i),2),iz(i),k)+12,
393
     B(Type(ix(i),2),iz(i),k+1)+4);
      Kxxs(7*ns+i) = Kxxs(7*ns+i) + Kxxq(B(Type(ix(i),2),iz(i),k)
394
     +12, B(Type(ix(i),2), iz(i),k+1)+4);
      Kxys(7*ns+i) = Kxys(7*ns+i) + Kxyq(B(Type(ix(i),2),iz(i),k)
395
     +12, B(Type(ix(i),2),iz(i),k+1)+4);
      396
     +12, B(Type(ix(i),2), iz(i),k+1)+4);
      Lxs(7*ns+i) = Lxs(7*ns+i) + Lxq(B(Type(ix(i),2),iz(i),k)
397
     +12,B(Type(ix(i),2),iz(i),k+1)+4);
      Lys(7*ns+i) = Lys(7*ns+i) + Lyq(B(Type(ix(i),2),iz(i),k)
398
     +12, B(Type(ix(i),2),iz(i),k+1)+4);
399
   Ms(8*ns+i)
                  = Ms(8*ns+i) + Mq(B(Type(ix(i),2),iz(i),k),B(
401
     Type(ix(i),2),iz(i),k+1)+8);
      Kxxs(8*ns+i) = Kxxs(8*ns+i) + Kxxq(B(Type(ix(i),2),iz(i),k)
402
     ,B(Type(ix(i),2),iz(i),k+1)+8);
      Kxys(8*ns+i) = Kxys(8*ns+i) + Kxyq(B(Type(ix(i),2),iz(i),k)
403
     ,B(Type(ix(i),2),iz(i),k+1)+8);
      404
     ,B(Type(ix(i),2),iz(i),k+1)+8);
      Lxs(8*ns+i) = Lxs(8*ns+i) + Lxq(B(Type(ix(i),2),iz(i),k),B(
405
     Type(ix(i), 2), iz(i), k+1)+8);
      Lys(8*ns+i) = Lys(8*ns+i) + Lyq(B(Type(ix(i),2),iz(i),k),B(i,k))
406
     Type (ix(i), 2), iz(i), k+1)+8);
407
      Ms(9*ns+i)
                  = Ms(9*ns+i) + Mq(B(Type(ix(i),2),iz(i),k)+4,B
408
     (Type(ix(i),2),iz(i),k+1)+8);
      Kxxs(9*ns+i) = Kxxs(9*ns+i) + Kxxq(B(Type(ix(i),2),iz(i),k)
409
     +4, B(Type(ix(i),2), iz(i),k+1)+8);
```

```
Kxys(9*ns+i) = Kxys(9*ns+i) + Kxyq(B(Type(ix(i),2),iz(i),k)
410
     +4, B(Type(ix(i),2), iz(i),k+1)+8);
      Kyys(9*ns+i) = Kyys(9*ns+i) + Kyyq(B(Type(ix(i),2),iz(i),k)
411
     +4,B(Type(ix(i),2),iz(i),k+1)+8);
      Lxs(9*ns+i) = Lxs(9*ns+i) + Lxq(B(Type(ix(i),2),iz(i),k)+4,
412
     B(Type(ix(i),2),iz(i),k+1)+8);
      Lys(9*ns+i) = Lys(9*ns+i) + Lyq(B(Type(ix(i),2),iz(i),k)+4,
     B(Type(ix(i),2),iz(i),k+1)+8);
      Ms(10*ns+i)
                    = Ms(10*ns+i) + Mq(B(Type(ix(i),2),iz(i),k)
415
     +8,B(Type(ix(i),2),iz(i),k+1)+8);
      Kxxs(10*ns+i) = Kxxs(10*ns+i) + Kxxq(B(Type(ix(i),2),iz(i),
416
     k)+8,B(Type(ix(i),2),iz(i),k+1)+8);
      Kxys(10*ns+i) = Kxys(10*ns+i) + Kxyq(B(Type(ix(i),2),iz(i),
417
     k)+8,B(Type(ix(i),2),iz(i),k+1)+8);
      Kyys(10*ns+i) = Kyys(10*ns+i) + Kyyq(B(Type(ix(i),2),iz(i),
418
     k)+8,B(Type(ix(i),2),iz(i),k+1)+8);
      Lxs(10*ns+i) = Lxs(10*ns+i) + Lxq(B(Type(ix(i),2),iz(i),k)
419
     +8,B(Type(ix(i),2),iz(i),k+1)+8);
      Lys(10*ns+i) = Lys(10*ns+i) + Lyq(B(Type(ix(i),2),iz(i),k)
420
     +8,B(Type(ix(i),2),iz(i),k+1)+8);
421
                    = Ms(11*ns+i) + Mq(B(Type(ix(i),2),iz(i),k)
      Ms(11*ns+i)
422
     +12, B(Type(ix(i),2),iz(i),k+1)+8);
      Kxxs(11*ns+i) = Kxxs(11*ns+i) + Kxxq(B(Type(ix(i),2),iz(i),
423
     k)+12,B(Type(ix(i),2),iz(i),k+1)+8);
      Kxys(11*ns+i) = Kxys(11*ns+i) + Kxyq(B(Type(ix(i),2),iz(i),
424
     k)+12,B(Type(ix(i),2),iz(i),k+1)+8);
      425
     k)+12,B(Type(ix(i),2),iz(i),k+1)+8);
      Lxs(11*ns+i) = Lxs(11*ns+i) + Lxq(B(Type(ix(i),2),iz(i),k)
426
     +12,B(Type(ix(i),2),iz(i),k+1)+8);
      Lys(11*ns+i) = Lys(11*ns+i) + Lyq(B(Type(ix(i),2),iz(i),k)
427
     +12, B(Type(ix(i),2), iz(i), k+1)+8);
       428
      Ms(12*ns+i)
                    = Ms(12*ns+i) + Mq(B(Type(ix(i),2),iz(i),k),B
429
     (Type(ix(i),2),iz(i),k+1)+12);
      Kxxs(12*ns+i) = Kxxs(12*ns+i) + Kxxq(B(Type(ix(i),2),iz(i),
430
     k), B(Type(ix(i),2),iz(i),k+1)+12);
      Kxys(12*ns+i) = Kxys(12*ns+i) + Kxyq(B(Type(ix(i),2),iz(i),
431
     k), B(Type(ix(i),2),iz(i),k+1)+12);
      Kyys(12*ns+i) = Kyys(12*ns+i) + Kyyq(B(Type(ix(i),2),iz(i),
432
     k),B(Type(ix(i),2),iz(i),k+1)+12);
      Lxs(12*ns+i) = Lxs(12*ns+i) + Lxq(B(Type(ix(i),2),iz(i),k),
433
     B(Type(ix(i),2),iz(i),k+1)+12);
      Lys(12*ns+i) = Lys(12*ns+i) + Lyq(B(Type(ix(i),2),iz(i),k),
434
     B(Type(ix(i),2),iz(i),k+1)+12);
435
```

```
Ms(13*ns+i) = Ms(13*ns+i) + Mq(B(Type(ix(i),2),iz(i),k)
436
      +4, B(Type(ix(i),2), iz(i),k+1)+12);
       Kxxs(13*ns+i) = Kxxs(13*ns+i) + Kxxq(B(Type(ix(i),2),iz(i),
437
      k)+4,B(Type(ix(i),2),iz(i),k+1)+12);
       Kxys(13*ns+i) = Kxys(13*ns+i) + Kxyq(B(Type(ix(i),2),iz(i),
438
      k)+4,B(Type(ix(i),2),iz(i),k+1)+12);
       439
      k)+4, B(Type(ix(i),2),iz(i),k+1)+12);
       Lxs(13*ns+i) = Lxs(13*ns+i) + Lxq(B(Type(ix(i),2),iz(i),k)
      +4, B(Type(ix(i),2), iz(i),k+1)+12);
       Lys(13*ns+i) = Lys(13*ns+i) + Lyq(B(Type(ix(i),2),iz(i),k)
441
      +4, B(Type(ix(i),2), iz(i),k+1)+12);
       Ms(14*ns+i)
                       = Ms(14*ns+i) + Mq(B(Type(ix(i),2),iz(i),k)
443
      +8,B(Type(ix(i),2),iz(i),k+1)+12);
       Kxxs(14*ns+i) = Kxxs(14*ns+i) + Kxxq(B(Type(ix(i),2),iz(i),
444
      k)+8,B(Type(ix(i),2),iz(i),k+1)+12);
       Kxys(14*ns+i) = Kxys(14*ns+i) + Kxyq(B(Type(ix(i),2),iz(i),
445
      k)+8,B(Type(ix(i),2),iz(i),k+1)+12);
       Kyys(14*ns+i) = Kyys(14*ns+i) + Kyyq(B(Type(ix(i),2),iz(i),
446
      k)+8,B(Type(ix(i),2),iz(i),k+1)+12);
       Lxs(14*ns+i) = Lxs(14*ns+i) + Lxq(B(Type(ix(i),2),iz(i),k)
447
      +8,B(Type(ix(i),2),iz(i),k+1)+12);
       Lys(14*ns+i) = Lys(14*ns+i) + Lyq(B(Type(ix(i),2),iz(i),k)
448
      +8,B(Type(ix(i),2),iz(i),k+1)+12);
449
       Ms(15*ns+i)
                       = Ms(15*ns+i) + Mq(B(Type(ix(i),2),iz(i),k)
450
      +12,B(Type(ix(i),2),iz(i),k+1)+12);
       \texttt{Kxxs}(15*ns+i) = \texttt{Kxxs}(15*ns+i) + \texttt{Kxxq}(\texttt{B}(\texttt{Type}(\texttt{ix}(\texttt{i}),2),\texttt{iz}(\texttt{i}),
451
      k)+12,B(Type(ix(i),2),iz(i),k+1)+12);
       \texttt{Kxys}(15*ns+i) = \texttt{Kxys}(15*ns+i) + \texttt{Kxyq}(\texttt{B}(\texttt{Type}(\texttt{ix}(\texttt{i}),2),\texttt{iz}(\texttt{i}),
452
      k)+12,B(Type(ix(i),2),iz(i),k+1)+12);
       Kyys(15*ns+i) = Kyys(15*ns+i) + Kyyq(B(Type(ix(i),2),iz(i),
453
      k)+12,B(Type(ix(i),2),iz(i),k+1)+12);
       Lxs(15*ns+i) = Lxs(15*ns+i) + Lxq(B(Type(ix(i),2),iz(i),k)
454
      +12, B(Type(ix(i),2),iz(i),k+1)+12);
       Lys(15*ns+i) = Lys(15*ns+i) + Lyq(B(Type(ix(i),2),iz(i),k)
      +12,B(Type(ix(i),2),iz(i),k+1)+12);
456
       k = k + 2;
457
       if(k > 8)
          break:
459
       end
460
     end
461
462
  end
463 M
       = sparse(x,y,Ms,4*(n+1)*(m+1),4*(n+1)*(m+1));
_{464}| \text{Kxx} = \text{sparse}(x,y,\text{Kxxs},4*(n+1)*(m+1),4*(n+1)*(m+1));
465 | \text{Kxy} = \text{sparse}(x, y, \text{Kxys}, 4*(n+1)*(m+1), 4*(n+1)*(m+1));
```

```
466 Kyy = sparse(x,y,Kyys,4*(n+1)*(m+1),4*(n+1)*(m+1));
|Lx| = |Sparse(x,y,Lxs,4*(n+1)*(m+1),4*(n+1)*(m+1));
Ly = sparse(x,y,Lys,4*(n+1)*(m+1),4*(n+1)*(m+1));
469 return;
470
471 function B = BMatrix()
_{472} B = zeros(9,9,8);
B(3,1,:) = [2 2 0 0 0 0 0];
B(3,2,:) = [2 \ 3 \ 0 \ 0 \ 0 \ 0];
B(3,3,:) = [0 \ 0 \ 0 \ 0 \ 0 \ 0]
  B(3,4,:) = [0 \ 0 \ 0 \ 0 \ 0
                             0
476
  B(3,5,:) = [0 \ 0 \ 0 \ 0 \ 0
                             0
_{478} | B(3,6,:) = [0 \ 0 \ 0 \ 0 \ 0]
                            0 0];
B(3,7,:) = [0 \ 0 \ 0 \ 0 \ 0 \ 0];
B(3,8,:) = [2 1 0 0 0 0 0];
B(3,9,:) = [2 4 0 0 0 0 0];
B(2,1,:) = [2 2 3 3 0 0 0 0];
  B(2,2,:) = [2 \ 3 \ 0 \ 0 \ 0]
484
                            0
B(2,3,:) = [0 \ 0 \ 0 \ 0 \ 0]
                            0 01:
B(2,4,:) = [0 \ 0 \ 0 \ 0 \ 0]
B(2,5,:) = [0 \ 0 \ 0 \ 0 \ 0]
                            0 0];
  B(2,6,:) = [3 2 0 0 0]
                          0
|B(2,7,:)| = [3 1 0 0 0 0]
                            0
490 \mid B(2,8,:) = [2 1 3 4 0 0 0 0];
491 B(2,9,:) = [2 4 0 0 0 0 0 0];
492
B(1,1,:) = [3 \ 3 \ 0 \ 0 \ 0 \ 0];
494 B(1,2,:) = [0 0 0 0 0 0 0 0];
B(1,3,:) = [0 \ 0 \ 0 \ 0 \ 0 \ 0];
496 B(1,4,:) = [0 0 0 0 0 0]
                            0
                               01:
B(1,5,:) = [0 \ 0 \ 0 \ 0 \ 0]
                            0
B(1,6,:) = [3 2 0 0 0 0 0 0];
  B(1,7,:) = [3 1 0 0 0 0
                            0 0];
B(1,8,:) = [3 4 0 0 0 0 0];
B(1,9,:) = [0 \ 0 \ 0 \ 0 \ 0 \ 0];
502
  B(6,1,:) = [1 1 2 2 0 0 0 0];
503
B(6,2,:) = [1 \ 4 \ 2 \ 3 \ 0 \ 0]
                              0];
B(6,3,:) = [1 \ 3 \ 0 \ 0 \ 0]
  B(6,4,:) = [1 2 0 0 0 0
                            0
506
  B(6,5,:) = [0 \ 0 \ 0 \ 0 \ 0
                             0
507
  B(6,6,:) = [0 \ 0 \ 0 \ 0 \ 0
                            0 0];
B(6,7,:) = [0 \ 0 \ 0 \ 0 \ 0 \ 0];
B(6,8,:) = [2 1 0 0 0 0 0];
  B(6,9,:) = [2 4 0 0 0 0 0 0];
B(5,1,:) = [1 1 2 2 3 3 4 4];
```

```
B(5,2,:) = [1 \ 4 \ 2 \ 3 \ 0 \ 0 \ 0];
B(5,3,:) = [1 \ 3 \ 0 \ 0 \ 0 \ 0];
B(5,4,:) = [1 2 4 3 0 0 0 0];
517
  B(5,5,:) = [4 2 0 0 0 0 0 0];
B(5,6,:) = [4 1 3 2 0 0 0 0];
B(5,7,:) = [3 1 0 0 0 0 0];
  B(5,8,:) = [3 4 2 1 0 0 0 0];
520
  B(5,9,:) = [2 4 0 0 0 0 0 0];
521
B(4,1,:) = [3 \ 3 \ 4 \ 4 \ 0 \ 0 \ 0];
524 B(4,2,:) = [0 0 0 0 0 0 0 0];
525 B(4,3,:) = [0 0 0 0 0 0 0 0];
526 B(4,4,:) = [4 3 0 0 0 0 0 0];
527 B(4,5,:) = [4 2 0 0 0 0 0 0];
  B(4,6,:) = [4 1 3 2 0 0 0 0];
B(4,7,:) = [3 1 0 0 0 0 0];
B(4,8,:) = [3 4 0 0 0 0 0];
B(4,9,:) = [0 \ 0 \ 0 \ 0 \ 0 \ 0];
B(9,1,:) = [1 1 0 0 0 0 0];
B(9,2,:) = [1 \ 4 \ 0 \ 0 \ 0 \ 0];
B(9,3,:) = [1 \ 3 \ 0 \ 0 \ 0 \ 0];
  B(9,4,:) = [1 2 0 0 0 0 0];
B(9,5,:) = [0 \ 0 \ 0 \ 0 \ 0 \ 0];
B(9,6,:) = [0 \ 0 \ 0 \ 0 \ 0 \ 0];
  B(9,7,:) = [0 \ 0 \ 0 \ 0 \ 0 \ 0];
540 B(9,8,:) = [0 0 0 0 0 0 0];
B(9,9,:) = [0 \ 0 \ 0 \ 0 \ 0 \ 0];
542
B(8,1,:) = [1 1 4 4 0 0 0 0];
B(8,2,:) = [1 4 0 0 0 0 0];
B(8,3,:) = [1 \ 3 \ 0 \ 0 \ 0 \ 0];
B(8,4,:) = [1 2 4 3 0 0 0 0];
  B(8,5,:) = [4 2 0 0 0 0 0 0];
B(8,6,:) = [4 1 0 0 0 0 0];
B(8,7,:) = [0 \ 0 \ 0 \ 0 \ 0 \ 0];
B(8,8,:) = [0 \ 0 \ 0 \ 0 \ 0 \ 0];
  B(8,9,:) = [0 \ 0 \ 0 \ 0 \ 0 \ 0];
B(7,1,:) = [4 \ 4 \ 0 \ 0 \ 0 \ 0];
B(7,2,:) = [0 \ 0 \ 0 \ 0 \ 0 \ 0];
  B(7,3,:) = [0 \ 0 \ 0 \ 0 \ 0 \ 0];
  B(7,4,:) = [4 \ 3 \ 0 \ 0 \ 0 \ 0 \ 0];
B(7,5,:) = [4 2 0 0 0 0 0];
  B(7,6,:) = [4 1 0 0 0 0 0 0];
B(7,7,:) = [0 \ 0 \ 0 \ 0 \ 0 \ 0];
B(7,8,:) = [0 \ 0 \ 0 \ 0 \ 0 \ 0];
B(7,9,:) = [0 \ 0 \ 0 \ 0 \ 0 \ 0];
```

```
562 return;
563
  function T = MATRIX_T(Q)
564
  syms x;
565
  syms y;
566
567
  n = size(Q,2);
569
  T = zeros(n);
  for j = 1:n
      T(j,1) = subs(Q(j),[x,y],[0,0]);
      T(j,2) = subs(Q(j),[x,y],[1,0]);
      T(j,3) = subs(Q(j),[x,y],[1,1]);
575
      T(j,4) = subs(Q(j),[x,y],[0,1]);
      if(n > 4)
      T(j,5) = subs(diff(Q(j),x),[x,y],[0,0]);
      T(j,6) = subs(diff(Q(j),x),[x,y],[1,0]);
578
      T(j,7) = subs(diff(Q(j),x),[x,y],[1,1]);
580
      T(j,8) = subs(diff(Q(j),x),[x,y],[0,1]);
      end
581
      if(n > 8)
582
      T(j,9) = subs(diff(Q(j),y),[x,y],[0,0]);
583
      T(j,10) = subs(diff(Q(j),y),[x,y],[1,0]);
584
      T(j,11) = subs(diff(Q(j),y),[x,y],[1,1]);
585
      T(j,12) = subs(diff(Q(j),y),[x,y],[0,1]);
586
587
      end
      if(n > 12)
588
      T(j,13) = subs(diff(diff(Q(j),y),x),[x,y],[0,0]);
      T(j,14) = subs(diff(diff(Q(j),y),x),[x,y],[1,0]);
590
      T(j,15) = subs(diff(diff(Q(j),y),x),[x,y],[1,1]);
      T(j,16) = subs(diff(diff(Q(j),y),x),[x,y],[0,1]);
      end
  end
  T = T';
  return
596
   function E = Positions(m,n,dx,dy)
598
       E = zeros((n+1)*(m+1),2);
599
       ix = n+1;
600
       iy = m+1;
601
       for i = 1:(n+1)*(m+1)
           E(i,:) = [dx*(ix-1),dy*(iy-1)];
603
604
           iy = iy-1;
605
           if(iy == 0)
606
                iy = m+1;
607
                ix = ix -1;
           end
609
```

```
end
%[Cubes, CubeNumbers] = CreateCubes(E,N);
%Plot(E,N,Cubes)
return
```

Example code for three-dimensional elastic body using tri-cubics

```
%function [Eig,uxB,uyB,uzB,sz] = Copy_of_CubePC(s,n1,h,inum,
                   numEig)
 plant of the state of the 
 3 format long g
       warning off;
     method =2;
 9 %mkdir(strcat('\Plots\', sprintf('%.6f',s)));
10 %gpuDevice(1);
                      %mwb = MultiWaitBar(3, 1, '3-Dimensional Beam Eigenvalue
                    Calculator', 'g');
                      %mwb.Update(1, 1, 0, 'Total Progress - Setting parameters')
                      %mwb.Update(2, 1, 0, ['Matrix Creation ' num2str(0) '%']);
                      %mwb.Update(3, 1, 0, 'Plot');
14
                      %alpha = 1200;
                      %d2 = sqrt(s/alpha);
16
                      d1 = sqrt((12*s^2)/(alpha*(1+s^2)));
17
                      %d1 = sqrt(12/(alpha));
18
19
                       d1 = h;
                      d2 = s;
20
                       %d2 = 1;
21
                      n2 = ceil(n1*h);
23
                      if (n2 <= 10)
24
                                      n2 = 6;
25
                       end
                       n3 = ceil(n2*s);
                       %n3 = ceil(n1/s);
                       if (n3 <= 10)
29
                                      n3 = 6;
                      end
                      %n2 = 3;
32
33
                       sz = n1*n2*n3;
```

```
35
      S = [0 \ 1 \ 0 \ d1 \ 0 \ d2]; %Set size of the beam
36
      N = [n1 n2 n3]; %Number of elements
37
38
      Delta = [(S(2)-S(1))/N(1) (S(4)-S(3))/N(2) (S(6)-S(5))/N(3)
     ]; %space step size
      nu = 0.3;
39
      gamma = 1/(2*(1+nu))*5/6
40
      %A = 1/(gamma*(1+nu)*(1-2*nu));
41
42
      B = 1/(2*gamma*(1+nu));
      for i = inum: -1:50
43
          h(i) = figure(i);
44
           movegui(h(i),'west')
45
46
      end
47
      %A = 1/(1-nu^2);
      B = 1/(2*gamma*(1+nu));
      %mwb.Update(1, 1, 0.1, 'Total Progress - Creating Matrices
49
      [K11, K12, K13, K22, K23, K33, M0, Dom, E] = Matrices(Delta, N,
50
     method);
      %mwb.Update(1, 1, 0.3, 'Total Progress - Admissible Basis
     functions');
      %Om = Omega(N, Dom);
      %F = Initial(N,f);
53
      Mf = MO;
54
     %K11(1:(N(2)+1)*(N(3)+1),:) = [];
56
     %K11(:,1:(N(2)+1)*(N(3)+1)) = [];
57
     %K12(1:(N(2)+1)*(N(3)+1),:) = [];
     %K12(:,1:(N(2)+1)*(N(3)+1)) = [];
     %K13(1:(N(2)+1)*(N(3)+1),:) = [];
60
     %K13(:,1:(N(2)+1)*(N(3)+1)) = [];
61
     %K22(1:(N(2)+1)*(N(3)+1),:) = [];
     %K22(:,1:(N(2)+1)*(N(3)+1)) = [];
63
     %K23(1:(N(2)+1)*(N(3)+1),:) = [];
64
     %K23(:,1:(N(2)+1)*(N(3)+1)) = [];
65
     %K33(1:(N(2)+1)*(N(3)+1),:) = [];
66
     %K33(:,1:(N(2)+1)*(N(3)+1)) = [];
67
68
     %MO(1:(N(2)+1)*(N(3)+1),:) = [];
69
     %MO(:,1:(N(2)+1)*(N(3)+1)) = [];
70
     %Mf(1:(N(2)+1)*(N(3)+1),:) = [];
71
72
      %mwb.Update(1, 1, 0.4, 'Total Progress - Concatinating
73
     matrices');
      Of = sparse(size(Mf,1), size(Mf,2));
74
      MF = [Mf Of Of; Of Mf Of; Of Of Mf];
75
      0 = sparse(size(M0,1), size(M0,2));
76
      %M = sparse(3*size(M0,1),3*size(M0,2));
77
```

```
M = [MO \ O \ O; \ O \ MO \ O; \ O \ MO];
       M([1:size(M0,1)],[1:size(M0,2)]) = M0;
79
       M(2*[1:size(M0,1)],2*[1:size(M0,2)]) = M0;
80
       %M(3*[1:size(M0,1)],3*[1:size(M0,2)]) = M0;
81
       Mf = M;
82
       FS = size(M);
83
       %M = [MO O; O MO];
       K21 = K12';
85
       K31 = K13';
       K32 = K23';
87
       a1 = 1/(gamma*(1+nu));
89
       a2 = nu/(gamma*(1+nu)*(1-2*nu));
91
       a3 = 1/(2*gamma*(1+nu));
92
       K1 = a1*K11 + a2*K11 + a3*K22 + a3*K33;
93
       K2 = a3*K12 + a2*K21;
94
       K3 = a3*K13 + a2*K31;
95
96
       K4 = a2*K12 + a3*K21;
       K5 = a1*K22 + a2*K22 + a3*K11 + a3*K33;
97
       K6 = a3*K23 + a2*K32;
98
       K7 = a2*K13 + a3*K31;
99
       K8 = a2*K23 + a3*K32;
100
       K9 = a1*K33 + a2*K33 + a3*K11 + a3*K22;
101
103
       %K = sparse(size(K1,1)*3, size(K1,2)*3);
104
       %K([1:size(K1,1)],[1:size(K1,2)]) = K1;
       %K([1:size(K1,1)],2*[1:size(K1,2)]) = K2;
106
       %K([1:size(K1,1)],3*[1:size(K1,2)]) = K3;
       K(2*[1:size(K1,1)],[1:size(K1,2)]) = K4;
108
       %K(2*[1:size(K1,1)],2*[1:size(K1,2)]) = K5;
       K(2*[1:size(K1,1)],3*[1:size(K1,2)]) = K6;
110
       %K(3*[1:size(K1,1)],[1:size(K1,2)]) = K7;
111
       %K(3*[1:size(K1,1)],2*[1:size(K1,2)]) = K8;
112
       %K(3*[1:size(K1,1)],3*[1:size(K1,2)]) = K9;
113
114
       K = [K1 \ K2 \ K3; \ K4 \ K5 \ K6; \ K7 \ K8 \ K9];
       All = (N(1)+1)*(N(2)+1)*(N(3)+1);
117
       x = [22*All+(N(2)+1)*(N(3)+1):-1:22*All+1
118
            19*All+(N(2)+1)*(N(3)+1):-1:19*All+1
119
            18*All+(N(2)+1)*(N(3)+1):-1:18*All+1
            16*All+(N(2)+1)*(N(3)+1):-1:16*All+1
            14*All+(N(2)+1)*(N(3)+1):-1:14*All+1
123
            11*All+(N(2)+1)*(N(3)+1):-1:11*All+1
            10*All+(N(2)+1)*(N(3)+1):-1:10*All+1
125
```

```
8*All+(N(2)+1)*(N(3)+1):-1:8*All+1
126
                                                                              6*All+(N(2)+1)*(N(3)+1):-1:6*All+1
                                                                             3*All+(N(2)+1)*(N(3)+1):-1:3*All+1
129
                                                                             2*All+(N(2)+1)*(N(3)+1):-1:2*All+1
130
                                                                             0*All+(N(2)+1)*(N(3)+1):-1:0*All+1];
                                            K(x,:) = [];
133
                                            K(:,x) = [];
                                            M(x,:) = [];
135
                                            M(:,x) = [];
                                            Mf(x,:) = [];
                                    % K = [1/(gamma*(1+nu))*K11+nu/(gamma*(1+nu)*(1-2*nu))*(K11+
139
                                     K22+K33) 1/(gamma*(1+nu))*K12 1/(gamma*(1+nu))*K13;
                                                                                    1/(gamma*(1+nu))*K12 1/(gamma*(1+nu))*K22+nu/(gamma
140
                                       *(1+nu)*(1-2*nu))*(K11+K22+K33) 1/(gamma*(1+nu))*K23;
                                                                                     1/(gamma*(1+nu))*K13 1/(gamma*(1+nu))*K23 1/(gamma
141
                                       *(1+nu))*K33+nu/(gamma*(1+nu)*(1-2*nu))*(K11+K22+K33)];
142
                                    \% K33 = (-nu/((1-2*nu)+nu))*(K11+K22);
                                    % K = [1/(gamma*(1+nu))*K11+nu/(gamma*(1+nu)*(1-2*nu))*(K11+
                                     K22+K33) 1/(gamma*(1+nu))*K12;
                                                                                 1/(gamma*(1+nu))*K12 1/(gamma*(1+nu))*K22+nu/(gamma
                                       *(1+nu)*(1-2*nu))*(K11+K22+K33);
147
                                           K = [2*(1-nu)*K11+(1-2*nu)*K22+(1-2*nu)*K33 2*nu*K12+(1-2*nu)*K31 2*nu*K12+(1-2*nu)*K3
                                      nu)*K21 2*nu*K13+(1-2*nu)*K31;
                                                                            2*nu*K21+(1-2*nu)*K12 (1-2*nu)*K11+2*(1-nu)*K22+(1-2*nu)*K11+2*(1-nu)*K22+(1-2*nu)*K11+2*(1-nu)*K22+(1-2*nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-nu)*K11+2*(1-
                                      nu)*K33 2*nu*K23+(1-2*nu)*K32;
                                                                             2*nu*K31+(1-2*nu)*K13 2*nu*K32+(1-2*nu)*K23 (1-2*nu)*
                                       K11+(1-2*nu)*K22+2*(1-nu)*K33;
                                          %K = 1/(2*gamma*(1+nu)*(1-2*nu))*K;
                                           K = [K11+(1-nu)/2*K22+(1-nu)/2*K33 (1-nu)/2*K12+nu*K21 (1-nu)/2*K12+nu*K12+nu*K21 (1-nu)/2*K12+nu*K21 (1-nu)/2*K12+nu*K21 (1-nu)/2*K12+nu*K21 (1-nu)/2*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*K12+nu*
                                      nu)/2*K13+nu*K31;
                                                                             (1-nu)/2*K21+nu*K12 (1-nu)/2*K11+K22+(1-nu)/2*K33 (1-nu)/2*K21+nu*K12 (1-nu)/2*K33 (1-nu)/2*K31+nu*K12 (1-nu)/2*K33 (1-nu)/2*K31+nu*K32+(1-nu)/2*K33 (1-nu)/2*K31+nu*K32+(1-nu)/2*K33 (1-nu)/2*K31+nu*K32+(1-nu)/2*K33 (1-nu)/2*K31+nu*K32+(1-nu)/2*K33 (1-nu)/2*K31+nu*K32+(1-nu)/2*K33 (1-nu)/2*K31+nu*K32+(1-nu)/2*K33 (1-nu)/2*K31+nu*K32+(1-nu)/2*K33 (1-nu)/2*K31+nu*K32+(1-nu)/2*K33 (1-nu)/2*K33+(1-nu)/2*K33+(1-nu)/2*K33+(1-nu)/2*K33+(1-nu)/2*K33+(1-nu)/2*K33+(1-nu)/2*K33+(1-nu)/2*K33+(1-nu)/2*K33+(1-nu)/2*K33+(1-nu)/2*K33+(1-nu)/2*K33+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+(1-nu)/2*K31+
154
                                      nu)/2*K23+nu*K32;
                                                                          (1-nu)/2*K31+nu*K13 (1-nu)/2*K32+nu*K23 (1-nu)/2*K11
                                       +(1-nu)/2*K22+K33;
                                            % K = 1/(gamma*(1-nu^2))*K;
156
                                                  whos k
159 %numEig = 100;
160 % {
alpha = \max(\text{sum}(\text{abs}(K), 2)./\text{diag}(K))-2;
```

```
L = ichol(K,struct('type','ict','droptol',1e-3,'diagcomp',alpha
                 ));
n = size(K, 1);
[V,D] = eigs(@(x)pcg(K,x,1e-3,200,L,L'),n,M,numEig,'sm');
166 %mwb.Update(1, 1, 0.5, 'Total Progress - Cholsky Decomposition
                 <sup>'</sup>);
[R,p,s] = chol(M,'vector');
%mwb.Update(1, 1, 0.55, 'Total Progress - Eigs');
%Rand = sprand(K);
||x|| ||x|
[V,DE,flag] = eigs(K,R,numEig,'smallestabs','IsCholesky',true,'
                  CholeskyPermutation',s,'Tolerance',1e-4);
174 flag;
%mwb.Update(1, 1, 0.6, 'Total Progress');
176 Eig = diag(DE);
177 % Mg = gpuArray(M);
178 % Kg = gpuArray(K);
179
180 %{
sV = size(Eig, 1);
182 R = zeros(sV, sV);
_{183} for i = 1:sV
                 for j = 1:sV
                    X = K*V(:,i) - M*V(:,i)*D(j);
185
                    NORMX = norm(X, Inf);
                    R(j,i) = NORMX;
                 end
189 end
_{190} \mid R = K*V-M*V*D;
191 xlswrite('CompareEigenValues.xlsx',R)
192 %}
193
194 u1p = 0;
u2p = 0;
196 u3p = 0;
197 u1s = 0;
198 u2s = 0;
199 u3s = 0;
200 \text{ uplx} = 0;
201 | uply = 0;
202 Psize = 0;
_{203} T = 0;
204 %%{
|uxB| = |zeros(inum, (N(1)+1), (N(2)+1), (N(3)+1));
```

```
uyB = zeros(inum, (N(1)+1), (N(2)+1), (N(3)+1));
            uzB = zeros(inum, (N(1)+1), (N(2)+1), (N(3)+1));
209
_{210} f = 0.3;
211
212 [D,E] = Domain(N,Delta);
213 %TD = D(:,ceil((N(2)+1)/2),ceil((N(3)+1)/2));
^{214} %TD = D(:,ceil((N(2)+1)/2),:);
215 TD = D(:,:, ceil((N(3)+1)/2));
_{216} TD = TD(:);
217 TDV = sort(TD(:));
218 OD = D(:, ceil((N(2)+1)/2), ceil((N(3)+1)/2));
219
220 F1 = zeros((N(1)+1)*(N(2)+1)*(N(3)+1),1);
F1(D(N(1)+1, ceil((N(2)+2)/2), ceil((N(3)+2)/2))) = f;
F = zeros(24*(N(1)+1)*(N(2)+1)*(N(3)+1),1);
           F(8*(N(1)+1)*(N(2)+1)*(N(3)+1)+1:9*(N(1)+1)*(N(2)+1)*(N(3)+1))
                            = F1:
226
227
228 Kug = gpuArray(K);
229 %bg = gpuArray(Mf*(F));
230 %u = gmres(Kug, bg, 30, 1e-4, 30);
231 %ueq = gather(u);
232
234 for i = inum:-1:1
235
            w = V(:,i);
236
238 Kug = gpuArray(K);
239 %bg = gpuArray(M*(-w));
\frac{1}{240} %u = gmres(Kug, bg, 30, 1e-4, 30);
\frac{1}{241} % ueq = gather(u);
            %ueq = K \setminus (Mf*F);
243
244
245
_{246} b = M*(-w);
ueq = gmres(K,b,30,1e-4,30);
 249 \ \text{ux} = \left[ \text{zeros} ((N(2)+1)*(N(3)+1),1); \ \text{ueq} (1:(N(1)+1)*(N(2)+1)*(N(3)+1); \ \text{ueq} (1:(N(1)+1)*(N(3)+1)*(N(3)+1); \ \text{ueq} (1:(N(1)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N
                            +1)-(N(2)+1)*(N(3)+1),1)]+E(:,1);
250 dxux = [ueq((N(1)+1)*(N(2)+1)*(N(3)+1)-(N(2)+1)*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1:2*(N(3)+1)+1*(N(3)+1)+1*(N(3)+1)+1*(N(3)+1)+1*(N(3)+1)+1*(N(3)+1)+1*(N(3)+1)+1*(N(3)+1)+1*(N(3)+1)+1*(N(3)+1)+1*(N(3)+1)+1*(N(3)+1)+1*(N(3)+1)+1*(N(3)+1)+1*(N(3)+1)+1*(N(3)+1)+1*(N(3)+1)+1*(N(3)+1)+1*(N(3)+1)+1*(N(3)+1)+1*(N(3)+1)+1*(N(3)+1)+1*(N(3)+1)+1*(N(3)+1)+1*(N(3)+1)+1*(N(3)+1)+1*(N(3)+1)+1*(N(3)+1)+1*(N(3)+1)+1*(N(3)+1)+1*(N(3)+1)+1*
                             (1)+1)*(N(2)+1)*(N(3)+1)-(N(2)+1)*(N(3)+1),1)];
```

```
251 \, dyux = \left[ zeros((N(2)+1)*(N(3)+1),1); ueq(2*(N(1)+1)*(N(2)+1)*(N(3)+1),1) \right]
          (3)+1)-(N(2)+1)*(N(3)+1)+1:3*(N(1)+1)*(N(2)+1)*(N(3)+1)-2*(
          N(2)+1)*(N(3)+1),1)];
    dzux = [zeros((N(2)+1)*(N(3)+1),1); ueg(3*(N(1)+1)*(N(2)+1)*(N(2)+1)]
          (3)+1)-2*(N(2)+1)*(N(3)+1)+1:4*(N(1)+1)*(N(2)+1)*(N(3)+1)
          -3*(N(2)+1)*(N(3)+1),1)];
    dxyux = [ueq(4*(N(1)+1)*(N(2)+1)*(N(3)+1)-3*(N(2)+1)*(N(3)+1)
          +1:5*(N(1)+1)*(N(2)+1)*(N(3)+1)-3*(N(2)+1)*(N(3)+1),1);
    dxzux = [ueq(5*(N(1)+1)*(N(2)+1)*(N(3)+1)-3*(N(2)+1)*(N(3)+1)
          +1:6*(N(1)+1)*(N(2)+1)*(N(3)+1)-3*(N(2)+1)*(N(3)+1),1)];
    dyzux = [zeros((N(2)+1)*(N(3)+1),1); ueq(6*(N(1)+1)*(N(2)+1)*(N(2)+1)]
          (3)+1)-3*(N(2)+1)*(N(3)+1)+1:7*(N(1)+1)*(N(2)+1)*(N(3)+1)
          -4*(N(2)+1)*(N(3)+1),1);
    dxyzux = [ueq(7*(N(1)+1)*(N(2)+1)*(N(3)+1)-4*(N(2)+1)*(N(3)+1)
          +1:8*(N(1)+1)*(N(2)+1)*(N(3)+1)-4*(N(2)+1)*(N(3)+1),1)];
    uy = [zeros((N(2)+1)*(N(3)+1),1); ueq(8*(N(1)+1)*(N(2)+1)*(N(3)+1),1); ueq(8*(N(1)+1)*(N(2)+1)*(N(3)+1); ueq(8*(N(1)+1)*(N(2)+1)*(N(3)+1); ueq(8*(N(1)+1)*(N(3)+1); ueq(8*(N(1)+1)*(N(3)+1); ueq(8*(N(1)+1)*(N(3)+1); ueq(8*(N(1)+1)*(N(3)+1); ueq(8*(N(1)+1)*(N(3)+1); ueq(8*(N(1)+1)*(N(3)+1); ueq(8*(N(1)+1)*(N(2)+1)*(N(3)+1); ueq(8*(N(1)+1)*(N(2)+1)*(N(3)+1); ueq(8*(N(1)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+1)*(N(2)+
          +1) -4*(N(2)+1)*(N(3)+1)+1:9*(N(1)+1)*(N(2)+1)*(N(3)+1)-5*(N(3)+1)
          (2)+1)*(N(3)+1),1)]+E(:,2);
    dxuy = [ueq(9*(N(1)+1)*(N(2)+1)*(N(3)+1)-5*(N(2)+1)*(N(3)+1)
258
          +1:10*(N(1)+1)*(N(2)+1)*(N(3)+1)-5*(N(2)+1)*(N(3)+1),1)];
    dyuy = [zeros((N(2)+1)*(N(3)+1),1); ueq(10*(N(1)+1)*(N(2)+1)*(N(2)+1)]
          (3)+1)-5*(N(2)+1)*(N(3)+1)+1:11*(N(1)+1)*(N(2)+1)*(N(3)+1)
          -6*(N(2)+1)*(N(3)+1),1);
    dzuy = [zeros((N(2)+1)*(N(3)+1),1); ueq(11*(N(1)+1)*(N(2)+1)*(N(2)+1)]
          (3)+1)-6*(N(2)+1)*(N(3)+1)+1:12*(N(1)+1)*(N(2)+1)*(N(3)+1)
          -7*(N(2)+1)*(N(3)+1),1);
    dxyuy = [ueq(12*(N(1)+1)*(N(2)+1)*(N(3)+1)-7*(N(2)+1)*(N(3)+1)
          +1:13*(N(1)+1)*(N(2)+1)*(N(3)+1)-7*(N(2)+1)*(N(3)+1),1)];
262 | dxzuy = [ueq(13*(N(1)+1)*(N(2)+1)*(N(3)+1)-7*(N(2)+1)*(N(3)+1)]
          +1:14*(N(1)+1)*(N(2)+1)*(N(3)+1)-7*(N(2)+1)*(N(3)+1),1);
    dyzuy = [zeros((N(2)+1)*(N(3)+1),1); ueq(14*(N(1)+1)*(N(2)+1)*(
          N(3)+1 -7* (N(2)+1)*(N(3)+1)+1:15*(N(1)+1)*(N(2)+1)*(N(3)+1)
          -8*(N(2)+1)*(N(3)+1),1);
    dxyzuy = [ueq(15*(N(1)+1)*(N(2)+1)*(N(3)+1)-8*(N(2)+1)*(N(3)+1)
          +1:16*(N(1)+1)*(N(2)+1)*(N(3)+1)-8*(N(2)+1)*(N(3)+1),1)];
uz = [zeros((N(2)+1)*(N(3)+1),1); ueq(16*(N(1)+1)*(N(2)+1)*(N(2)+1)]
          (3)+1)-8*(N(2)+1)*(N(3)+1)+1:17*(N(1)+1)*(N(2)+1)*(N(3)+1)
          -9*(N(2)+1)*(N(3)+1),1)]+E(:,3);
266 | dxuz = [ueq(17*(N(1)+1)*(N(2)+1)*(N(3)+1)-9*(N(2)+1)*(N(3)+1)
          +1:18*(N(1)+1)*(N(2)+1)*(N(3)+1)-9*(N(2)+1)*(N(3)+1),1)];
    dyuz = [zeros((N(2)+1)*(N(3)+1),1); ueq(18*(N(1)+1)*(N(2)+1)*(N(2)+1)]
          (3)+1)-9*(N(2)+1)*(N(3)+1)+1:19*(N(1)+1)*(N(2)+1)*(N(3)+1)
          -10*(N(2)+1)*(N(3)+1),1);
268 dzuz = [zeros((N(2)+1)*(N(3)+1),1); ueq(19*(N(1)+1)*(N(2)+1)*(N(2)+1)]
          (3)+1)-10*(N(2)+1)*(N(3)+1)+1:20*(N(1)+1)*(N(2)+1)*(N(3)+1)
          -11*(N(2)+1)*(N(3)+1),1);
269 \text{ dxyuz} = [\text{ueq}(20*(N(1)+1)*(N(2)+1)*(N(3)+1)-11*(N(2)+1)*(N(3)+1)]
          +1:21*(N(1)+1)*(N(2)+1)*(N(3)+1)-11*(N(2)+1)*(N(3)+1),1);
```

```
dxzuz = [ueq(21*(N(1)+1)*(N(2)+1)*(N(3)+1)-11*(N(2)+1)*(N(3)+1)
              +1:22*(N(1)+1)*(N(2)+1)*(N(3)+1)-11*(N(2)+1)*(N(3)+1),1)];
      dyzuz = [zeros((N(2)+1)*(N(3)+1),1); ueq(22*(N(1)+1)*(N(2)+1)*(
              N(3)+1)-11*(N(2)+1)*(N(3)+1)+1:23*(N(1)+1)*(N(2)+1)*(N(3)
              +1)-12*(N(2)+1)*(N(3)+1),1)];
272 dxyzuz = [ueq(23*(N(1)+1)*(N(2)+1)*(N(3)+1)-12*(N(2)+1)*(N(3)+1)-12*(N(2)+1)*(N(3)+1)-12*(N(2)+1)*(N(3)+1)-12*(N(2)+1)*(N(3)+1)-12*(N(2)+1)*(N(3)+1)-12*(N(2)+1)*(N(3)+1)-12*(N(2)+1)*(N(3)+1)-12*(N(2)+1)*(N(3)+1)-12*(N(3)+1)*(N(3)+1)-12*(N(3)+1)*(N(3)+1)-12*(N(3)+1)*(N(3)+1)-12*(N(3)+1)*(N(3)+1)-12*(N(3)+1)*(N(3)+1)-12*(N(3)+1)*(N(3)+1)-12*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1
              +1)+1:24*(N(1)+1)*(N(2)+1)*(N(3)+1)-12*(N(2)+1)*(N(3)+1),1)
273
274
      f = figure(i);
275
276 movegui(f,'west')
      scatter3(ux(TD),uy(TD),uz(TD),5,uz(TD))
278 title(Eig(i));
280
281 \text{%uxB}(i,1:N(1)+1,1,1:N(3)+1) = ux(TD);
282 \text{%uyB}(i,1:N(1)+1,1,1:N(3)+1) = uy(TD);
283 \text{%uzB}(i,1:N(1)+1,1,1:N(3)+1) = uz(TD);
284
286 %dxuxB(i,1:N(1)+1,1,1) = dxux(TD);
^{287} %dxuyB(i,1:N(1)+1,1,1) = dxuy(TD);
288 \%dxuzB(i,1:N(1)+1,1,1) = dxuz(TD);
289 \%dyuxB(i,1:N(1)+1,1,1) = dyux(TD);
290 \% dyuyB(i,1:N(1)+1,1,1) = dyuy(TD);
291 \mid \text{%dyuzB}(i,1:N(1)+1,1,1) = dyuz(TD);
292 %dzuxB(i,1:N(1)+1,1,1) = dzux(TD);
^{293} %dzuyB(i,1:N(1)+1,1,1) = dzuy(TD);
294 \mid \% dzuzB(i,1:N(1)+1,1,1) = dzuz(TD);
^{295} %dxyuxB(i,1:N(1)+1,1,1) = dxyux(TD);
^{296} %dxyuyB(i,1:N(1)+1,1,1) = dxyuy(TD);
^{297} \( \lambda \text{dxyuzB}(i,1:N(1)+1,1,1) = \text{dxyuz}(TD);
298 \mid \text{%dxzuxB(i,1:N(1)+1,1,1)} = \text{dxzux(TD)};
299 \% dxzuyB(i,1:N(1)+1,1,1) = dxzuy(TD);
300 \%dxzuzB(i,1:N(1)+1,1,1) = dxzuz(TD);
301 \text{ %dyzuxB(i,1:N(1)+1,1,1)} = \text{dyzux(TD)};
302 \mid \text{%dyzuyB(i,1:N(1)+1,1,1)} = \text{dyzuy(TD)};
303 \% dyzuzB(i,1:N(1)+1,1,1) = dyzuz(TD);
304 \mid \text{%dxyzuxB}(i,1:N(1)+1,1,1) = dxyzux(TD);
305 \mid % dxyzuyB(i,1:N(1)+1,1,1) = dxyzuy(TD);
307 %set(0, 'CurrentFigure', h(i));
308 %scatter3(ux,uy,uz)
309 %title(Eig(i));
310 %scatter3(ux,uy,uz,5,uz)
312 %scatter3(uxB,uyB,uzB,5,uzB)
```

```
313 %hold on
%scatter3(ux,uy,zeros(size(uz)));
316 %hold on
317 %ux2 = ux(D(:,1,1));
318 | \%uy2 = uy(D(:,1,1));
319 %uz2 = uz(D(:,1,1));
320
321 %max2 = norm(uy2, Inf);
322 | \%uy2 = uy2/max2*0.8;
323 %scatter3(ux2,uy2,uz2)
325 hold off
326 %axis([0 1.1 -0.025 0.05 -0.025 0.025])
327 %dxux2 = dxux(TDV);
328 %dxuy2 = dxuy(TDV);
329 %dxuz2 = dxuz(TDV);
330 %dyux2 = dyux(TDV);
331 %dyuy2 = dyuy(TDV);
332 %dyuz2 = dyuz(TDV);
333 %dzux2 = dzux(TDV);
334 %dzuy2 = dzuy(TDV);
% = \frac{1}{335}  % dzuz2 = dzuz(TDV);
336
337
  sigma11 = 1/(gamma*(1+nu))*dxuxB + nu/(gamma*(1+nu)*(1-2*nu))
      *(dxuxB+dyuyB+dzuzB);
339 %sigma22 = 1/(gamma*(1+nu))*dyuyB + nu/(gamma*(1+nu)*(1-2*nu))
     *(dxuxB+dyuyB+dzuzB);
340 %sigma33 = 1/(gamma*(1+nu))*dzuzB + nu/(gamma*(1+nu)*(1-2*nu))
      *(dxuxB+dyuyB+dzuzB);
342 %sigma31 = 1/(2*gamma*(1+nu))*(dzuxB + dxuzB);
343 \%sigma12 = 1/(2*gamma*(1+nu))*(dyuxB + dxuyB);
_{345} %stress = ceil((N(1)+1)/2);
346
_{348} %Ty = [0.5*(dxux(stress) + dxux(stress)) 0.5*(dxuy(stress) +
      dyux(stress)); 0.5*(dyux(stress) + dxuy(stress)) 0.5*(dyuy(
      stress) + dyuy(stress))]
  %Tz = [0.5*(dxux(stress) + dxux(stress)) 0.5*(dxuz(stress) +
      dzux(stress)); 0.5*(dzux(stress) + dxuz(stress)) 0.5*(dzuz(
      stress) + dzuz(stress))]
  %T = [sigma11(stress) sigma12(stress) sigma31(stress); sigma12(
      stress) sigma22(stress) sigma23(stress); sigma31(stress)
      sigma23(stress) sigma33(stress)]
351
```

```
352 | \%ux1 = ux(OD);
353 \text{ %uy1} = \text{uy(OD)};
354 | \%uz1 = uz(OD);
355
356
357 %f = figure();
358 %movegui(f,pos);
359 %scatter3(ux,uy,uz);
360 %hold on
361 %grid on
362 %plot3(ux1,uy1,uz1);
363 %title(strcat(num2str(i),' - ',num2str(Eig(i))))
364 %view(2)
365 end
366 %}
367 % {
368 %[KM, KMPat] = sparseinv(K);
_{369} %KM = KM*M;
370 %smallest = 0;
371 %bestEig = 0;
372
373 for i = 20:-1:1
     %smallest = 100;
     plot_fig = figure('NumberTitle', 'off', 'Name', strcat('
      Eigenvalue: ',int2str(i),' - ',num2str(s)));
     w = V(:,i);
377
     for j = 1:numEig
        X = K*w - M*w*Eig(j);
379
        if norm(X) < smallest
380
  %
             smallest = norm(X);
381
382 %
             bestEig = Eig(j);
383 %
        end
      end
      %plot_fig.suptitle(strcat(int2str(i),' - ',num2str(s)));
385
   %mwb.Update(3, 1, 0.1, 'Plot');
386
       %wg = gpuArray(w);
387
       alpha = max(sum(abs(K),2)./diag(K))-2;
388
       L = ichol(K,struct('type','ict','droptol',1e-3,'diagcomp',
389
       u = pcg(K, M*w, 1e-1, 2000000, L, L');
391
392
       %normalize = norm(w,Inf);
393
       %u = normalize*u;
      u = (K) \setminus MF * F;
395
       %alpha = max(sum(abs(K),2)./diag(K))-2;
397
```

```
%L = ichol(K,struct('type','ict','droptol',1e-3,'diagcomp',
398
                alpha));
                  u = pcg(K, MF*F, 1e-3, 200000, L, L');
399
               % mwb.Update(3, 1, 0.3, 'Plot');
400
                  u1 = [zeros((N(2)+1)*(N(3)+1),1); u(1:size(u,1)/3)] + E
401
                (:,1);
                  u2 = [zeros((N(2)+1)*(N(3)+1),1); u(size(u,1)/3+1:2*size(u,1))]
                 ,1)/3)] + E(:,2);
                 u3 = [zeros((N(2)+1)*(N(3)+1),1); u(2*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3+1:3*size(u,1)/3*size(u,1)/3*size(u,1)/3*size(u,1)/3*size(u,1)/3*size(u,1)/3*size(u,1)/3*size(u,1)/3*size(u,1)/3*size(u,1)/3*size(u,1)/3*si
                u,1)/3)]+ E(:,3);
405
                  u1 = 1/norm(u1, Inf)*u1;
406
407
                  u2 = 1/norm(u2, Inf)*u2;
                  u3 = 1/norm(u3, Inf)*u3;
408
409
                   [D,E] = Domain(N,Delta);
410
                  plane = D(:,:,ceil((N(3)+1)/2));
411
                  plane = plane(:);
412
                  uplx = u1(plane);
413
                  uply = u2(plane);
414
415
               % w1 = w(1:size(w,1)/3);
416
               \% w2 = w(size(w,1)/3+1:2*size(w,1)/3);
417
               \% w3 = w(2*size(w,1)/3+1:3*size(w,1)/3);
418
419
            % mwb.Update(3, 1, 0.4, 'Plot');
420
                  ix = [];
421
                  if(N(1)+1 > 200)
422
                           \% iy = [1 (N(2)+2)/2 (N(2)+1) (N(2)+1)*(N(3)+1)-(N(2)+1)
                +1 (N(2)+1)*(N(3)+1)];
                             ih = ((N(2)+1)-1)/2;
                              iv = 1 + ((N(3) + 1) - 1)/2 * (N(2) + 1);
425
                              iy = iv + ih; %[1  1 + ih  1 + 2 * ih  iv  iv + ih  iv + 2 * ih  2 * iv - 1  2 *
426
                iv+ih-1 2*iv+2*ih-1]; %[iv+ih]; %
                              icount = 1;
427
                             div = floor((N(1)+1)/200);
                              for k = 1:div:(N(1)+1)
429
                                         for j = 1:size(iy,2)
430
                                                    ix(icount) = iy(j) + (k-1)*(N(2)+1)*(N(3)+1);
431
                                                     icount = icount +1;
                                         end
433
                              end
                              u1p = u1(ix);
435
                             u2p = u2(ix);
                             u3p = u3(ix);
437
                           % w1p = w1(ix);
                           % w2p = w2(ix);
439
```

```
% w3p = w3(ix);
440
441
           E1p = E(ix,1);
442
           E2p = E(ix,2);
443
           E3p = E(ix,3);
444
           Psize = size(iy,2);
445
       else
446
            u1p = u1;
447
            u2p = u2;
            u3p = u3;
449
            w1p = w1;
451
         %
            w2p = w2;
            w3p = w3;
453
           E1p = E(:,1);
455
           E2p = E(:,2);
456
           E3p = E(:,3);
457
458
           Psize = (N(2)+1)*(N(3)+1);
459
       end
460
       %mwb.Update(3, 1, 0.7, 'Plot');
461
462
       u1p = 1/norm(u1p, Inf)*u1p;
463
       u2p = 1/norm(u2p, Inf)*u2p;
464
       %u3p = 1/norm(u3p, Inf)*u3p;
465
466
       %umx = u1p(size(u1p,1)/2
468
469
       scatter3(u1p,u2p,u3p);
470
       hold on
       %scatter3(E1p,E2p,E3p,0.1);
472
       hold on
473
       %scatter3(w1p,w2p,w3p);
474
       %mwb.Update(3, 1, 1, 'Plot');
475
       u1s = size(u1p);
476
       u2s = size(u2p);
477
       u3s = size(u3p);
478
       for k = 1:Psize
479
            hold on
480
            plot3(u1p(k:Psize:k+u1s-2*Psize),u2p(k:Psize:k+u2s-2*
481
      Psize),u3p(k:Psize:k+u3s-2*Psize),'-');
482
  temp_png = strcat('\Plots\', sprintf('%.6f', n1), '\PNG\Plot',
      sprintf('%.6f',i),'.png');
484 temp_fig = strcat('\Plots\', sprintf('%.6f', n1), '\Fig\Plot',
      sprintf('%.6f',i),'.fig');
```

```
485 view([0 0 90])
486 | %legend(['Eigenvalue: 'num2str(Eig(i))]);
487 %saveas(plot_fig, strcat(pwd, temp_png))
488 %savefig(plot_fig, strcat(pwd, temp_fig))
489 %close(plot_fig)
490 end
491 clear u
492
494 %mwb.Update(1, 1, 1, 'Total Progress');
       mwb.Close();
  return;
496
497
   function [D,E] = Domain(N,Delta)
498
       D = zeros(N(1)+1,N(2)+1,N(3)+1);
       icount = 1;
500
501
       for i = 1:N(1)+1
502
          for k = 1:N(3)+1
503
              for j = 1:N(2)+1
504
                 D(i,j,k) = icount;
505
                 icount = icount + 1;
506
              end
507
          end
508
       end
509
       E = zeros((N(1)+1)*(N(2)+1)*(N(3)+1),3);
       ix = 1;
       iy = 1;
       iz = 1;
       ixt = 0;
       for i = 1:(N(1)+1)*(N(2)+1)*(N(3)+1)
           E(i,:) = [Delta(1)*(ix-1), Delta(2)*(iy-1), Delta(3)*(iz)]
      -1)];
517
            iy = iy+1;
518
519
            if(ix == N(1)+2)
520
                ix = 1;
521
            end
            if(iy == N(2) + 2)
                iy = 1;
                ixt = ixt +1;
                iz = iz+1;
            end
            if(ixt == N(3)+1)
                ix = ix+1;
                ixt = 0;
            end
531
```

```
if(iz == N(3)+2)
532
                iz = 1;
533
534
            end
       end
536
       %[Cubes, CubeNumbers] = CreateCubes(E,N);
537
       %Plot(E,N,Cubes)
539
   return
   function Next = Adjacent(N,D)
541
       Next = zeros((N(1)+1)*(N(2)+1)*(N(3)+1),27);
       %1 - Itself
543
       %2 - Forward
       %3 - Backward
545
       %4 - Forward + Left
       %5 - Forward + Right
547
       %6 - Left
548
       %7 - Right
549
       %8 - Backward + Left
       %9 - Backward + Right
       for i = 1:N(1)+1
552
          for j = 1:N(2)+1
553
              for k = 1:N(3)+1
554
                 Next(D(i,j,k),1) = D(i,j,k);
555
                 if(i < N(1) + 1)
556
                    Next(D(i,j,k),2) = D(i+1,j,k);
                 else
558
                     Next(D(i,j,k),2) = nan;
                 end
560
                 if(i>1)
                    Next(D(i,j,k),3) = D(i-1,j,k);
562
                 else
                     Next(D(i,j,k),3) = nan;
564
                 end
565
                 if(i < N(1) + 1 & & j < N(2) + 1)
566
                    Next(D(i,j,k),4) = D(i+1,j+1,k);
567
568
                 else
                      Next(D(i,j,k),4) = nan;
569
                 end
570
                 Next(D(i,j,k),5) = D(i+1,j-1,k);
                 else
                     Next(D(i,j,k),5) = nan;
574
                 end
575
                 if(j < N(2)+1)
576
                    Next(D(i,j,k),6) = D(i,j+1,k);
                 else
                     Next(D(i,j,k),6) = nan;
579
```

```
end
580
                  if(j>1)
581
                     Next(D(i,j,k),7) = D(i,j-1,k);
583
                      Next(D(i,j,k),7) = nan;
584
585
                  if(i>1 && j < N(2)+1)
586
                     Next(D(i,j,k),8) = D(i-1,j+1,k);
587
                  else
                      Next(D(i,j,k),8) = nan;
589
                  end
                  if(i>1 && j>1)
                     Next(D(i,j,k),9) = D(i-1,j-1,k);
593
                      Next(D(i,j,k),9) = nan;
                  end
595
596
                  if(k < N(3)+1)
597
                      Next(D(i,j,k),10) = D(i,j,k+1);
598
                      if (i<N(1)+1)</pre>
599
                          Next(D(i,j,k),11) = D(i+1,j,k+1);
600
                      else
601
                           Next(D(i,j,k),11) = nan;
602
603
                      end
                      if(i>1)
604
                          Next(D(i,j,k),12) = D(i-1,j,k+1);
605
                      else
606
                           Next(D(i,j,k),12) = nan;
                      end
608
                      if(i < N(1) + 1 & & j < N(2) + 1)
                          Next(D(i,j,k),13) = D(i+1,j+1,k+1);
610
                      else
                           Next(D(i,j,k),13) = nan;
612
613
                      if(i < N(1) + 1 &  j > 1)
614
                          Next(D(i,j,k),14) = D(i+1,j-1,k+1);
615
616
                      else
                           Next(D(i,j,k),14) = nan;
617
                      end
618
                      if(j < N(2) + 1)
619
                          Next(D(i,j,k),15) = D(i,j+1,k+1);
620
                      else
621
                           Next(D(i,j,k),15) = nan;
                      end
623
                      if(j>1)
                          Next(D(i,j,k),16) = D(i,j-1,k+1);
625
                           Next(D(i,j,k),16) = nan;
627
```

```
end
628
                      if(i>1 && j < N(2)+1)
629
                          Next(D(i,j,k),17) = D(i-1,j+1,k+1);
630
631
                           Next(D(i,j,k),17) = nan;
632
                      end
633
                      if(i>1 && j>1)
634
                          Next(D(i,j,k),18) = D(i-1,j-1,k+1);
635
                           Next(D(i,j,k),18) = nan;
637
                      end
638
                  else
639
                      Next(D(i,j,k),10) = nan;
                      Next(D(i,j,k),11) = nan;
641
                      Next(D(i,j,k),12) = nan;
                      Next(D(i,j,k),13) = nan;
643
                      Next(D(i,j,k),14) = nan;
644
                      Next(D(i,j,k),15) = nan;
645
646
                      Next(D(i,j,k),16) = nan;
                      Next(D(i,j,k),17) = nan;
647
                      Next(D(i,j,k),18) = nan;
648
                  end
649
650
                  if(k>1)
651
                      Next(D(i,j,k),19) = D(i,j,k-1);
652
                      if(i < N(1) + 1)
                          Next(D(i,j,k),20) = D(i+1,j,k-1);
654
                           Next(D(i,j,k),20) = nan;
656
                      end
                      if(i>1)
658
                          Next(D(i,j,k),21) = D(i-1,j,k-1);
                      else
660
                           Next(D(i,j,k),21) = nan;
661
662
                      if(i < N(1) + 1 && j < N(2) + 1)
663
                          Next(D(i,j,k),22) = D(i+1,j+1,k-1);
664
665
                           Next(D(i,j,k),22) = nan;
666
667
                      if(i < N(1) + 1 &   i > 1)
668
                          Next(D(i,j,k),23) = D(i+1,j-1,k-1);
669
                      else
                           Next(D(i,j,k),23) = nan;
671
                      end
                      if(j < N(2)+1)
673
                          Next(D(i,j,k),24) = D(i,j+1,k-1);
674
                      else
675
```

```
Next(D(i,j,k),24) = nan;
676
                end
677
678
                if(j>1)
                   Next(D(i,j,k),25) = D(i,j-1,k-1);
679
                else
680
                    Next(D(i,j,k),25) = nan;
681
                end
682
                if(i>1 && j < N(2)+1)
683
                   Next(D(i,j,k),26) = D(i-1,j+1,k-1);
685
                    Next(D(i,j,k),26) = nan;
686
                end
687
                if(i>1 && j>1)
                   Next(D(i,j,k),27) = D(i-1,j-1,k-1);
689
690
                    Next(D(i,j,k),27) = nan;
691
                end
692
             else
693
694
                Next(D(i,j,k),19) = nan;
                Next(D(i,j,k),20) = nan;
695
                Next(D(i,j,k),21) = nan;
696
                Next(D(i,j,k),22) = nan;
697
                Next(D(i,j,k),23) = nan;
698
                Next(D(i,j,k),24) = nan;
699
                Next(D(i,j,k),25) = nan;
700
                Next(D(i,j,k),26) = nan;
                Next(D(i,j,k),27) = nan;
702
             end
          end
704
        end
705
     end
706
  return
708
  function B = AdjacentType()%CHECKED
709
     B = zeros(27, 27, 16);
710
     %CHECKED
711
     B(1,1,:) = [2 2 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Itself
712
     713
     714
     715
     Left
     B(1,5,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; Forward +
716
     Right
     B(1,6,:) = [2 1 0 0 0 0 0 0 0 0 0 0 0 0]; Left
717
     718
     719
     Left
```

```
B(1,9,:) = [0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0]; Backward +
720
    Right
     %Up%CHECKED
721
     B(1,10,:) = [2 6 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Itself
722
     B(1,11,:) = [2 7 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward
723
     724
     B(1,13,:) = [2 8 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
    Left
     B(1,14,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
    Right
     B(1,15,:) = [2 5 0 0 0 0 0 0 0 0 0 0 0 0]; Left
     B(1,16,:) = [0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0];Right
728
     B(1,17,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
     B(1,18,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; "Backward +
730
    Right
     %Down%CHECKED
731
     732
     B(1,20,:) = [0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0]; Forward
733
     734
     B(1,22,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
735
    Left
     B(1,23,:) = [0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0]; Forward +
736
    Right
     737
     B(1,25,:) = [0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0];Right
     B(1,26,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; "Backward +
739
     B(1,27,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; "Backward +
740
    Right
741
     %CHECKED
742
     B(2,1,:) = [1 1 2 2 0 0 0 0 0 0 0 0 0 0]; %Itself
743
     744
     745
     B(2,4,:) = [2 4 0 0 0 0 0 0 0 0 0 0 0 0 0]; "Forward +
746
    Left
     B(2,5,:) = [1 3 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
747
    Right
     B(2,6,:) = [2 1 0 0 0 0 0 0 0 0 0 0 0 0]; Left
748
     B(2,7,:) = [1 2 0 0 0 0 0 0 0 0 0 0 0 0]; Right
749
     750
    Left
     751
    Right
    %Up%CHECKED
752
```

```
B(2,10,:) = [2 6 1 5 0 0 0 0 0 0 0 0 0 0]; %Itself
753
    B(2,11,:) = [2 7 1 8 0 0 0 0 0 0 0 0 0 0];%Forward
754
    755
    B(2,13,:) = [2 8 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
756
   Left
    B(2,14,:) = [1 7 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
757
   Right
    B(2,15,:) = [2 5 0 0 0 0 0 0 0 0 0 0 0 0 0]; Left
758
    B(2,16,:) = [1 6 0 0 0 0 0 0 0 0 0 0 0 0];%Right
    B(2,17,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; "Backward +
760
   Left
    B(2,18,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
761
   Right
    %Down%CHECKED
762
    B(2,19,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; "Itself
763
    764
    765
    B(2,22,:) = [0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0]; Forward +
766
   Left
    B(2,23,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
767
   Right
    768
    B(2,25,:) = [0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0];Right
769
    B(2,26,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; "Backward +
   Left
    B(2,27,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
771
   Right
    %
772
    %CHECKED
773
    B(3,1,:) = [1 1 0 0 0 0 0 0 0 0 0 0 0 0]; %Itself
774
    775
    776
    777
   Left
    Right
    779
    B(3,7,:) = [1 2 0 0 0 0 0 0 0 0 0 0 0 0]; Right
780
    781
    Right
    %Up%CHECKED
783
    B(3,10,:) = [1 5 0 0 0 0 0 0 0 0 0 0 0 0];%Itself
784
    B(3,11,:) = [1 8 0 0 0 0 0 0 0 0 0 0 0 0];%Forward
    786
```

```
B(3,13,:) = [0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0]; Forward +
787
    B(3,14,:) = [1 7 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
788
    Right
    789
    B(3,16,:) = [1 6 0 0 0 0 0 0 0 0 0 0 0 0];%Right
790
    B(3,17,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; "Backward +
    Left
    B(3,18,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
    Right
    %Down%CHECKED
    794
    B(3,20,:) = [0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0]; Forward
    B(3,21,:) = [0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0]; Backward
796
    B(3,22,:) = [0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0]; "Forward +
797
    Left
    B(3,23,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
798
    Right
    B(3,24,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0]; "Left"
799
    800
    B(3,26,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
801
    Left
    B(3,27,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
802
    Right
    %
803
    %CHECKED
    B(4,1,:) = [2 2 6 6 0 0 0 0 0 0 0 0 0 0]; %Itself
805
    807
    Left
    B(4,5,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0]; Forward +
809
    Right
    B(4,6,:) = [2 1 6 5 0 0 0 0 0 0 0 0 0 0]; Left
810
    811
    812
    Left
    813
    Right
    %Up%CHECKED
814
815
    B(4,10,:) = [2 6 0 0 0 0 0 0 0 0 0 0 0 0]; %Itself
    B(4,11,:) = [2 7 0 0 0 0 0 0 0 0 0 0 0 0];%Forward
816
    817
    B(4,13,:) = [2 8 0 0 0 0 0 0 0 0 0 0 0 0];%Forward +
818
    Left
```

```
B(4,14,:) = [0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0]; Forward +
819
    Right
    B(4,15,:) = [2 5 0 0 0 0 0 0 0 0 0 0 0 0]; Left
820
    B(4,16,:) = [0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0];Right
821
    822
    Left
    B(4,18,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; "Backward +
    Right
    %Down%CHECKED
    B(4,19,:) = [6 2 0 0 0 0 0 0 0 0 0 0 0 0];%Itself
825
    B(4,20,:) = [6\ 3\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0]; Forward
826
    827
    Left
    B(4,23,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
829
    Right
    B(4,24,:) = [6 1 0 0 0 0 0 0 0 0 0 0 0 0]; "Left"
830
    831
832
    Left
    B(4,27,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
833
    Right
834
    %CHECKED
    B(5,1,:) = [1 \ 1 \ 2 \ 2 \ 5 \ 6 \ 6 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0]; %Itself
836
    B(5,2,:) = [2 \ 3 \ 1 \ 4 \ 5 \ 8 \ 6 \ 7 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0]; Forward
    838
    Left
    B(5,5,:) = [1 3 5 7 0 0 0 0 0 0 0 0 0 0]; Forward +
    Right
    B(5,6,:) = [2 1 6 5 0 0 0 0 0 0 0 0 0 0]; Left
841
    B(5,7,:) = [1 2 5 6 0 0 0 0 0 0 0 0 0 0]; %Right
842
    B(5,8,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0]; "Backward +
843
    Left
    844
    Right
    %Up%CHECKED
845
    B(5,10,:) = [2 6 1 5 0 0 0 0 0 0 0 0 0 0];%Itself
846
    B(5,11,:) = [2 7 1 8 0 0 0 0 0 0 0 0 0 0];%Forward
847
    B(5,13,:) = [2 8 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
849
    Left
    B(5,14,:) = [1 7 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
850
    Right
    B(5,15,:) = [2 5 0 0 0 0 0 0 0 0 0 0 0 0]; Left
851
```

```
B(5,16,:) = [1 6 0 0 0 0 0 0 0 0 0 0 0 0]; %Right
852
    B(5,17,:) = [0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0]; Backward +
853
   Left
    B(5,18,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
854
   Right
    %Down%CHECKED
855
    B(5,19,:) = [5 1 6 2 0 0 0 0 0 0 0 0 0 0];%Itself
    857
    859
   Left
    B(5,23,:) = [5 3 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
860
   Right
    B(5,24,:) = [6 1 0 0 0 0 0 0 0 0 0 0 0 0]; %Left
861
    B(5,25,:) = [5 2 0 0 0 0 0 0 0 0 0 0 0 0];Right
    B(5,26,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; "Backward +
863
   Left
    864
   Right
    %
865
    %CHECKED
866
    B(6,1,:) = [1 1 5 5 0 0 0 0 0 0 0 0 0 0]; %Itself
867
    868
    B(6,3,:) = [0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0]; Backward
869
    870
   Left
    871
   Right
    872
    B(6,7,:) = [1 2 5 6 0 0 0 0 0 0 0 0 0 0];%Right
873
    874
   Left
    875
   Right
    %Up%CHECKED
876
    B(6,10,:) = [1 5 0 0 0 0 0 0 0 0 0 0 0 0];%Itself
877
    B(6,11,:) = [1 8 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward
878
    879
    B(6,13,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
880
   Left
    B(6,14,:) = [1 7 0 0 0 0 0 0 0 0 0 0 0 0];%Forward +
   Right
    882
    B(6,16,:) = [1 6 0 0 0 0 0 0 0 0 0 0 0 0]; %Right
883
    B(6,17,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
   Left
```

```
885
   Right
    %Down%CHECKED
886
    B(6,19,:) = [5 1 0 0 0 0 0 0 0 0 0 0 0 0]; %Itself
887
    888
    889
    B(6,22,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
   Left
    Right
    892
    B(6,25,:) = [5 2 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Right
893
    B(6,27,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; "Backward +
   Right
    %
896
    %CHECKED
897
    B(7,1,:) = [6 6 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Itself
898
    B(7,2,:) = [6 7 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward
899
    900
    B(7,4,:) = [6\ 8\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0]; %Forward +
901
   Left
    B(7,5,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; Forward +
   Right
    B(7,6,:) = [6 5 0 0 0 0 0 0 0 0 0 0 0 0]; Left
    904
    B(7,8,:) = [0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0];
Backward +
   Left
    B(7,9,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0]; "Backward +
906
   Right
    %Up%CHECKED
907
    908
    B(7,11,:) = [0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0]; "Forward
909
    910
    911
   Left
    B(7,14,:) = [0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0]; Forward +
912
   Right
    913
    B(7,16,:) = [0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0];Right
914
    B(7,17,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
915
   Left
    916
   Right
    %Down %CHECKED
917
```

```
B(7,19,:) = [6 2 0 0 0 0 0 0 0 0 0 0 0 0];%Itself
918
     B(7,20,:) = [6\ 3\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0]; Forward
919
     920
     B(7,22,:) = [6 4 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
921
    Left
     B(7,23,:) = [0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0]; Forward +
922
    Right
     923
     B(7,25,:) = [0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0];Right
     925
    Left
     B(7,27,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; "Backward +
926
    Right
     %
927
     %CHECKED
     B(8,1,:) = [5 5 6 6 0 0 0 0 0 0 0 0 0 0 0]; %Itself
929
     B(8,2,:) = [6 7 5 8 0 0 0 0 0 0 0 0 0 0];%Forward
930
     931
     B(8,4,:) = [6\ 8\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0]; "Forward +
932
    Left
     B(8,5,:) = [5 7 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
933
    Right
     B(8,6,:) = [6 5 0 0 0 0 0 0 0 0 0 0 0 0]; Left
934
     B(8,7,:) = [5 6 0 0 0 0 0 0 0 0 0 0 0 0 0]; Right
935
     936
     B(8,9,:) = [0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ ]; Backward +
937
    Right
     %Up%CHECKED
938
     B(8,10,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; "Itself
     940
     B(8,13,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
942
    Left
     B(8,14,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
943
    Right
     944
     B(8,16,:) = [0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0];Right
945
     B(8,17,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; "Backward +
946
     B(8,18,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
    Right
     %Down%CHECKED
948
     B(8,19,:) = [5 1 6 2 0 0 0 0 0 0 0 0 0 0]; %Itself
949
     B(8,21,:) = [0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0]; Backward
951
```

```
952
    B(8,23,:) = [5 3 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
953
    Right
    B(8,24,:) = [6 1 0 0 0 0 0 0 0 0 0 0 0 0]; Left
954
    B(8,25,:) = [5 2 0 0 0 0 0 0 0 0 0 0 0 0];%Right
955
    B(8,26,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; "Backward +
956
    Left
    B(8,27,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
    Right
    %
958
    %CHECKED
959
    B(9,1,:) = [5 5 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Itself
960
    B(9,2,:) = [5 8 0 0 0 0 0 0 0 0 0 0 0 0];%Forward
961
    962
    B(9,4,:) = [0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0]; "Forward +
963
    Left
    B(9,5,:) = [5 7 0 0 0 0 0 0 0 0 0 0 0 0];%Forward +
964
    Right
    965
    B(9,7,:) = [5 6 0 0 0 0 0 0 0 0 0 0 0 0]; Right
966
    967
    Left
    Right
    %Up%CHECKED
    970
    B(9,11,:) = [0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0]; Forward
    972
    B(9,13,:) = [0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0]; "Forward +
    Left
    B(9,14,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
974
    Right
    B(9,15,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0]; "Left"
975
    976
    B(9,17,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
977
    Left
    B(9,18,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; "Backward +
978
    Right
    %Down%CHECKED
979
    B(9,19,:) = [5 1 0 0 0 0 0 0 0 0 0 0 0 0]; "Itself
980
    981
    982
    B(9,22,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
983
    Left
```

```
984
     Right
     985
     B(9,25,:) = [5 2 0 0 0 0 0 0 0 0 0 0 0 0]; %Right
986
     987
     Left
     B(9,27,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; "Backward +
     Right
     %
     %CHECKED
990
     B(10,1,:) = [2 2 3 3 0 0 0 0 0 0 0 0 0 0]; %Itself
991
     992
     B(10,3,:) = [3 2 0 0 0 0 0 0 0 0 0 0 0 0];
*Backward
993
     B(10,4,:) = [2 4 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
994
     Left
     B(10,5,:) = [0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0]; Forward +
995
     Right
     B(10,6,:) = [2 1 3 4 0 0 0 0 0 0 0 0 0 0 0]; Left
996
     B(10,7,:) = [0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0];Right
997
     B(10,8,:) = [3 1 0 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
998
     Left
     B(10,9,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; "Backward +
999
     Right
     %Up%CHECKED
1000
     B(10,10,:) = [2 6 3 7 0 0 0 0 0 0 0 0 0 0]; %Itself
1001
     B(10,11,:) = [2 7 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward
1002
     B(10,12,:) = [3 6 0 0 0 0 0 0 0 0 0 0 0 0]; "Backward
1003
     B(10,13,:) = [2 8 0 0 0 0 0 0 0 0 0 0 0 0];%Forward +
1004
     Left
     B(10,14,:) = [0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0]; Forward +
     Right
     B(10,15,:) = [2 5 3 8 0 0 0 0 0 0 0 0 0 0]; Left
1006
     1007
     B(10,17,:) = [3 5 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
1008
     Left
     B(10,18,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
1009
     Right
     %Down%CHECKED
1010
     B(10,19,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Itself
1011
     B(10,20,:) = [0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0]; Forward
1012
     B(10,21,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0]; "Backward
1013
     B(10,22,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
1014
     Left
     Right
     B(10,24,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Left
1016
```

```
1017
     B(10,26,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
1018
     Left
     B(10,27,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
1019
     Right
     %
1021
     %CHECKED
     B(11,1,:) = [1 1 2 2 3 3 4 4 0 0 0 0 0 0 0]; %Itself
     B(11,3,:) = [3 2 4 1 0 0 0 0 0 0 0 0 0 0]; Backward
1024
     1025
     Left
     B(11,5,:) = [1 3 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
     Right
     B(11,6,:) = [2 1 3 4 0 0 0 0 0 0 0 0 0 0]; Left
1027
     B(11,7,:) = [1 2 4 3 0 0 0 0 0 0 0 0 0 0]; Right
1028
1029
     B(11,8,:) = [3 1 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
     Left
     B(11,9,:) = [4 2 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
1030
     Right
     %Up%CHECKED
     B(11,10,:) = [2 6 1 5 3 7 4 8 0 0 0 0 0 0 0]; %Itself
1032
     B(11,11,:) = [2 7 1 8 0 0 0 0 0 0 0 0 0 0]; %Forward
     B(11,12,:) = [3 6 4 5 0 0 0 0 0 0 0 0 0 0]; "Backward
1034
     B(11,13,:) = [2 8 0 0 0 0 0 0 0 0 0 0 0 0];%Forward +
     Left
     B(11,14,:) = [1 7 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
1036
     Right
     B(11,15,:) = [2 5 3 8 0 0 0 0 0 0 0 0 0 0]; %Left
1037
     B(11,16,:) = [1 6 4 7 0 0 0 0 0 0 0 0 0 0];%Right
     B(11,17,:) = [3 5 0 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
1039
     Left
     B(11,18,:) = [4 6 0 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
1040
     Right
     %Down%CHECKED
1041
     B(11,19,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Itself
1042
     1043
     B(11,21,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0]; "Backward
1044
     1045
     Left
     B(11,23,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
1046
     Right
     B(11,24,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Left
     1048
     B(11,26,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
1049
     Left
```

```
B(11,27,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
1050
     Right
1051
      %
      %CHECKED
      B(12,1,:) = [1 1 4 4 0 0 0 0 0 0 0 0 0 0 0]; %Itself
1053
      1054
      1056
     Left
      B(12,5,:) = [1 3 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
     Right
      B(12,6,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Left
1058
      B(12,7,:) = [1 2 4 3 0 0 0 0 0 0 0 0 0 0];%Right
      B(12,8,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; "Backward +
1060
     Left
      B(12,9,:) = [4 2 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
1061
     Right
      %Up%CHECKED
1062
      B(12,10,:) = [1 5 4 8 0 0 0 0 0 0 0 0 0 0]; %Itself
1063
      B(12,11,:) = [1 8 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward
1064
      B(12,12,:) = [4 5 0 0 0 0 0 0 0 0 0 0 0 0]; "Backward
1065
      B(12,13,:) = [0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0]; Forward +
1066
     Left
      B(12,14,:) = [1 7 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
1067
     Right
      B(12,15,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Left
      B(12,16,:) = [1 6 4 7 0 0 0 0 0 0 0 0 0 0];%Right
1069
      B(12,17,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
1070
     Left
      B(12,18,:) = [4 6 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
     Right
      %Down%CHECKED
1072
      1073
      1074
      B(12,21,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; "Backward
1075
      B(12,22,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
     Left
      B(12,23,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
1077
     Right
      B(12,24,:) = [0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0]; %Left
1078
      B(12,25,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; "Right
1079
      B(12,26,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
1080
     Left
      B(12,27,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Backward +
1081
     Right
```

```
%
1082
      %CHECKED
1083
      B(13,1,:) = [2 2 3 3 6 6 7 7 0 0 0 0 0 0 0]; %Itself
1084
      1085
      B(13,3,:) = [3 2 7 6 0 0 0 0 0 0 0 0 0 0]; Backward
1086
      B(13,4,:) = [2\ 4\ 6\ 8\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0]; Forward +
1087
     Left
      B(13,5,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
1088
     Right
      B(13,6,:) = [2 1 6 5 3 4 7 8 0 0 0 0 0 0 0]; "Left
1089
      B(13,7,:) = [0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0];Right
1090
      B(13,8,:) = [3 1 7 5 0 0 0 0 0 0 0 0 0 0 0]; "Backward +
     Left
      B(13,9,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; "Backward +
1092
     Right
      %Up%CHECKED
1093
      B(13,10,:) = [2 6 3 7 0 0 0 0 0 0 0 0 0 0]; % Itself
1094
      B(13,11,:) = [2 7 0 0 0 0 0 0 0 0 0 0 0 0]; Forward
1095
      B(13,12,:) = [3 6 0 0 0 0 0 0 0 0 0 0 0 0]; "Backward
1096
      B(13,13,:) = [2 8 0 0 0 0 0 0 0 0 0 0 0 0];%Forward +
1097
     Left
      1098
     Right
      B(13,15,:) = [2 5 3 8 0 0 0 0 0 0 0 0 0 0]; %Left
1099
      1100
      B(13,17,:) = [3 5 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Backward +
     Left
      B(13,18,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
1102
     Right
      %Down%CHECKED
1103
      B(13,19,:) = [6 2 7 3 0 0 0 0 0 0 0 0 0 0]; %Itself
1104
      B(13,20,:) = [6\ 3\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0];%Forward
1105
      B(13,21,:) = [7 2 0 0 0 0 0 0 0 0 0 0 0 0 0]; "Backward
1106
      1107
     Left
      B(13,23,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
1108
     Right
      B(13,24,:) = [6 1 7 4 0 0 0 0 0 0 0 0 0 0]; %Left
1109
      1110
      B(13,26,:) = [7 1 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
1111
     Left
      B(13,27,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
1112
     Right
      %
1113
```

```
%CHECKED
1114
       B(14,1,:) = [1 1 2 2 3 3 4 4 5 5 6 6 7 7 8 8]; %Itself
1115
       B(14,2,:) = [1 \ 4 \ 2 \ 3 \ 5 \ 8 \ 6 \ 7 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0]; Forward
1116
1117
       B(14,3,:) = [4 \ 1 \ 3 \ 2 \ 8 \ 5 \ 7 \ 6 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0]; Backward
       B(14,4,:) = [2 4 6 8 0 0 0 0 0 0 0 0 0 0]; %Forward +
1118
      Left
      B(14,5,:) = [1 3 5 7 0 0 0 0 0 0 0 0 0 0]; "Forward +
1119
      Right
       B(14,6,:) = [2 1 6 5 3 4 7 8 0 0 0 0 0 0 0]; Left
1120
       B(14,7,:) = [1 2 5 6 4 3 8 7 0 0 0 0 0 0 0]; %Right
1121
       B(14,8,:) = [3 1 7 5 0 0 0 0 0 0 0 0 0 0 0]; "Backward +
      Left
       B(14,9,:) = [4 2 8 6 0 0 0 0 0 0 0 0 0 0]; Backward +
1123
      Right
      %Up%CHECKED
1124
       B(14,10,:) = [1 5 2 6 3 7 4 8 0 0 0 0 0 0 0]; %Itself
1125
       B(14,11,:) = [2 7 1 8 0 0 0 0 0 0 0 0 0 0]; %Forward
1126
       B(14,12,:) = [3 6 4 5 0 0 0 0 0 0 0 0 0 0]; "Backward
1127
1128
      B(14,13,:) = [2 8 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
      Left
      B(14,14,:) = [1 7 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
1129
      Right
       B(14,15,:) = [2 5 3 8 0 0 0 0 0 0 0 0 0 0]; %Left
1130
       B(14,16,:) = [1 6 4 7 0 0 0 0 0 0 0 0 0 0]; %Right
1131
       B(14,17,:) = [3 5 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
1132
      Left
       B(14,18,:) = [4 6 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Backward +
1133
      Right
      %Down%CHECKED
       B(14,19,:) = [5 1 6 2 7 3 8 4 0 0 0 0 0 0 0]; %Itself
1135
       B(14,20,:) = [5 \ 4 \ 6 \ 3 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0]; Forward
1136
       B(14,21,:) = [8 1 7 2 0 0 0 0 0 0 0 0 0 0];%Backward
1137
       1138
      Left
      1139
      Right
       B(14,24,:) = [6 1 7 4 0 0 0 0 0 0 0 0 0 0]; Left
1140
       B(14,25,:) = [5 2 8 3 0 0 0 0 0 0 0 0 0 0]; Right
1141
      B(14,26,:) = [7 1 0 0 0 0 0 0 0 0 0 0 0 0]; "Backward +
1142
      B(14,27,:) = [8 2 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Backward +
1143
      Right
      %
1144
       B(15,1,:) = [1 1 4 4 5 5 8 8 0 0 0 0 0 0 0]; %Itself
1145
       1146
       B(15,3,:) = [4 \ 1 \ 8 \ 5 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0]; Backward
1147
```

```
B(15,4,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
1148
      1149
      Right
      1150
      B(15,7,:) = [1 \ 2 \ 5 \ 6 \ 4 \ 3 \ 8 \ 7 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0]; Right
1151
      B(15,8,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; "Backward +
1152
      Left
      B(15,9,:) = [4 2 8 6 0 0 0 0 0 0 0 0 0 0]; Backward +
1153
      Right
      %Up
1154
      B(15,10,:) = [1 5 4 8 0 0 0 0 0 0 0 0 0 0]; %Itself
      B(15,11,:) = [1 8 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward
1156
1157
      B(15,12,:) = [4 5 0 0 0 0 0 0 0 0 0 0 0 0];%Backward
      B(15,13,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; Forward +
1158
      Left
      B(15,14,:) = [1 7 0 0 0 0 0 0 0 0 0 0 0 0 0]; Forward +
1159
      Right
      B(15,15,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Left
1160
      B(15,16,:) = [1 6 4 7 0 0 0 0 0 0 0 0 0 0]; %Right
1161
      B(15,17,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
1162
      Left
      B(15,18,:) = [4 6 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
1163
      Right
      %Down
1164
      B(15,19,:) = [5 1 8 4 0 0 0 0 0 0 0 0 0 0]; %Itself
1165
      B(15,20,:) = [5 4 0 0 0 0 0 0 0 0 0 0 0 0];%Forward
1166
      B(15,21,:) = [8 1 0 0 0 0 0 0 0 0 0 0 0 0]; "Backward
1167
      B(15,22,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
1168
      Left
      B(15,23,:) = [5 3 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
1169
      Right
      1170
      B(15,25,:) = [5 2 8 3 0 0 0 0 0 0 0 0 0 0]; %Right
1171
      B(15,26,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
1172
     Left
      B(15,27,:) = [8 2 0 0 0 0 0 0 0 0 0 0 0 0 0]; "Backward +
1173
      Right
      %
1174
      B(16,1,:) = [6 6 7 7 0 0 0 0 0 0 0 0 0 0 0]; %Itself
1175
      B(16,2,:) = [6 7 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward
1176
      B(16,3,:) = [7 6 0 0 0 0 0 0 0 0 0 0 0 0];%Backward
1177
      B(16,4,:) = [6 8 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
1178
      Left
      B(16,5,:) = [0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0]; Forward +
1179
      Right
```

```
B(16,6,:) = [6 5 7 8 0 0 0 0 0 0 0 0 0 0]; Left
1180
     B(16,7,:) = [0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0];Right
1181
     B(16,8,:) = [7 5 0 0 0 0 0 0 0 0 0 0 0 0 0]; "Backward +
1182
     Left
     1183
     Right
     %Up
1184
     B(16,10,:) = [0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0]; %Itself
1185
     B(16,11,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward
1186
     B(16,12,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; "Backward
1187
     1188
     Left
     B(16,14,:) = [0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0]; Forward +
1189
     Right
     B(16,15,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Left
1190
     1191
     B(16,17,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
1192
     Left
1193
     Right
     %Down
1194
     B(16,19,:) = [6 2 7 3 0 0 0 0 0 0 0 0 0 0]; %Itself
1195
     B(16,20,:) = [6\ 3\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0];%Forward
1196
     B(16,21,:) = [7 2 0 0 0 0 0 0 0 0 0 0 0 0]; "Backward
1197
     1198
     Left
     1199
     Right
     B(16,24,:) = [6 1 7 4 0 0 0 0 0 0 0 0 0 0 0]; %Left
     1201
     B(16,26,:) = [7 1 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
1202
     Left
     B(16,27,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
1203
     Right
     %
1204
     B(17,1,:) = [5 5 6 6 7 7 8 8 0 0 0 0 0 0 0]; %Itself
1205
     B(17,2,:) = [5 8 6 7 0 0 0 0 0 0 0 0 0 0]; %Forward
1206
     B(17,3,:) = [8 5 7 6 0 0 0 0 0 0 0 0 0 0];%Backward
1207
     B(17,4,:) = [6 8 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
1208
     Left
     B(17,5,:) = [5 7 0 0 0 0 0 0 0 0 0 0 0 0]; "Forward +
1209
     Right
     B(17,6,:) = [6 5 7 8 0 0 0 0 0 0 0 0 0 0]; Left
1210
     B(17,7,:) = [5 6 8 7 0 0 0 0 0 0 0 0 0 0]; %Right
1211
     B(17,8,:) = [7 5 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
1212
     Left
```

```
B(17,9,:) = [8 6 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
1213
     Right
1214
      %Up
      B(17,10,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Itself
1215
      1216
      B(17,12,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0]; "Backward
1217
      B(17,13,:) = [0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0]; Forward +
1218
     Left
      B(17,14,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
1219
     Right
      1220
      B(17,16,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0]; Right
      B(17,17,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
      B(17,18,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
1223
     Right
      %Down
1224
      B(17,19,:) = [5 1 6 2 7 3 8 4 0 0 0 0 0 0 0]; %Itself
      B(17,20,:) = [5 \ 4 \ 6 \ 3 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0]; %Forward
1226
      B(17,21,:) = [8 1 7 2 0 0 0 0 0 0 0 0 0 0]; "Backward"
1227
      B(17,22,:) = [6 4 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
1228
     Left
      B(17,23,:) = [5 3 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
     Right
      B(17,24,:) = [6 1 7 4 0 0 0 0 0 0 0 0 0 0]; Left
1230
      B(17,25,:) = [5 2 8 3 0 0 0 0 0 0 0 0 0 0]; Right
1231
      B(17,26,:) = [7 1 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
1232
      B(17,27,:) = [8 2 0 0 0 0 0 0 0 0 0 0 0 0]; "Backward +
     Right
      %
1234
      B(18,1,:) = [5 5 8 8 0 0 0 0 0 0 0 0 0 0 0]; %Itself
      B(18,2,:) = [5 8 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward
1236
      B(18,3,:) = [8 5 0 0 0 0 0 0 0 0 0 0 0 0];
*Backward
1237
      1238
     Left
      B(18,5,:) = [5 7 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
1239
     Right
      1240
      B(18,7,:) = [5 6 8 7 0 0 0 0 0 0 0 0 0 0]; %Right
      B(18,8,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
      B(18,9,:) = [8 6 0 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
1243
     Right
      %Up
      B(18,10,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0]; % Itself
1245
```

```
1246
     1247
     1248
    Left
     B(18,14,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
1249
    Right
     B(18,15,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Left
     B(18,16,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0]; Right
1251
     B(18,17,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
    Left
     B(18,18,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
1253
    Right
     %Down
1254
     B(18,19,:) = [5 1 8 4 0 0 0 0 0 0 0 0 0 0 0]; "Itself
     B(18,20,:) = [5 4 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward
     B(18,21,:) = [8 1 0 0 0 0 0 0 0 0 0 0 0 0 0]; "Backward
1257
     1258
    Left
1259
     B(18,23,:) = [5 3 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
    Right
     B(18,24,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Left
1260
     B(18,25,:) = [5 2 8 3 0 0 0 0 0 0 0 0 0 0]; %Right
1261
     B(18,26,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
1262
    Left
     B(18,27,:) = [8 2 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
1263
    Right
     %
1264
    1265
     B(19,1,:) = [3 3 0 0 0 0 0 0 0 0 0 0 0 0]; %Itself
1266
     1267
     B(19,3,:) = [3 2 0 0 0 0 0 0 0 0 0 0 0 0 0]; Backward
1268
     B(19,4,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
1269
    Left
     B(19,5,:) = [0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0]; Forward +
1270
    Right
     B(19,6,:) = [3 4 0 0 0 0 0 0 0 0 0 0 0 0]; Left
1271
     1272
     B(19,8,:) = [3 1 0 0 0 0 0 0 0 0 0 0 0 0]; "Backward +
1273
    Left
     B(19,9,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; "Backward +
1274
    Right
     %Up
1275
     B(19,10,:) = [3 7 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Itself
1276
     1277
     B(19,12,:) = [3 6 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Backward
```

```
B(19,13,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
1279
      B(19,14,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
1280
      Right
      B(19,15,:) = [3 8 0 0 0 0 0 0 0 0 0 0 0 0 0]; "Left
1281
      B(19,16,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0]; Right
1282
      B(19,17,:) = [3 5 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Backward +
1283
      Left
      B(19,18,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
1284
      Right
      %Down
1285
      B(19,19,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Itself
1286
      B(19,20,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward
1287
      1288
      B(19,22,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; Forward +
1289
      Left
      B(19,23,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; Forward +
1290
      Right
      B(19,24,:) = [0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0]; %Left
1291
      1292
      B(19,26,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
1293
      Left
      B(19,27,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
1294
      Right
      %
1295
      B(20,1,:) = [3 3 4 4 0 0 0 0 0 0 0 0 0 0]; %Itself
      B(20,2,:) = [0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0]; Forward
1298
      B(20,3,:) = [3 2 4 1 0 0 0 0 0 0 0 0 0 0]; Backward
1299
      B(20,4,:) = [0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0]; "Forward +
1300
      Left
      B(20,5,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
1301
      Right
      B(20,6,:) = [3 4 0 0 0 0 0 0 0 0 0 0 0 0]; "Left"
1302
      1303
      B(20,8,:) = [3 1 0 0 0 0 0 0 0 0 0 0 0 0]; "Backward +
1304
      Left
      B(20,9,:) = [4 2 0 0 0 0 0 0 0 0 0 0 0 0]; "Backward +
1305
      Right
      qU%
1306
      B(20,10,:) = [4 8 3 7 0 0 0 0 0 0 0 0 0 0]; %Itself
1307
      B(20,11,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward
1308
      B(20,12,:) = [3 6 4 5 0 0 0 0 0 0 0 0 0 0]; Backward
      B(20,13,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
      Left
```

```
B(20,14,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
1311
   Right
    B(20,15,:) = [3 8 0 0 0 0 0 0 0 0 0 0 0 0 0]; Left
1312
    B(20,16,:) = [4 7 0 0 0 0 0 0 0 0 0 0 0 0];%Right
1313
    B(20,17,:) = [3 5 0 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
1314
   Left
    B(20,18,:) = [4 6 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
   Right
    %Down
    1317
    1318
    B(20,21,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0]; "Backward
    B(20,22,:) = [0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0]; Forward +
   Left
    B(20,23,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
1321
   Right
    B(20,24,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Left
1322
    1324
    Left
    1325
   Right
1326
    1328
    1330
    Left
    B(21,5,:) = [0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0]; Forward +
   Right
    1333
    1334
    1335
    B(21,9,:) = [4 2 0 0 0 0 0 0 0 0 0 0 0 0]; "Backward +
1336
   Right
    %Up
    B(21,10,:) = [4 8 0 0 0 0 0 0 0 0 0 0 0 0]; %Itself
1338
    B(21,12,:) = [4 5 0 0 0 0 0 0 0 0 0 0 0 0]; "Backward
1340
    B(21,13,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
1341
   Left
    B(21,14,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
   Right
    B(21,15,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Left
1343
```

```
B(21,16,:) = [4 7 0 0 0 0 0 0 0 0 0 0 0 0]; %Right
1344
     B(21,17,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
1345
    Left
     B(21,18,:) = [4 6 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
1346
    Right
     %Down
     B(21,19,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Itself
1348
     1349
     B(21,21,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0]; "Backward
     1351
    Left
     B(21,23,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
    Right
     B(21,24,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Left
1353
     B(21,26,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; "Backward +
1355
    Left
     B(21,27,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
1356
    Right
     %
1357
1358
     B(22,1,:) = [3 3 7 7 0 0 0 0 0 0 0 0 0 0 0]; %Itself
1359
     1360
     B(22,3,:) = [3 2 7 6 0 0 0 0 0 0 0 0 0 0]; Backward
1361
     B(22,4,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
1362
    Left
     1363
    Right
     B(22,6,:) = [7 8 3 4 0 0 0 0 0 0 0 0 0 0]; %Left
1364
     B(22,7,:) = [0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0];Right
     B(22,8,:) = [3 1 7 5 0 0 0 0 0 0 0 0 0 0 0]; "Backward +
1366
    Left
     B(22,9,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; "Backward +
1367
    Right
     %Up
1368
     B(22,10,:) = [3 7 0 0 0 0 0 0 0 0 0 0 0 0]; %Itself
1369
     B(22,12,:) = [3 6 0 0 0 0 0 0 0 0 0 0 0 0]; "Backward
1371
     1372
    Left
     B(22,14,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
    Right
     B(22,15,:) = [3 8 0 0 0 0 0 0 0 0 0 0 0 0]; %Left
1374
     B(22,17,:) = [3 5 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
1376
    Left
```

```
B(22,18,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
1377
     Right
     %Down
1378
     B(22,19,:) = [7 3 0 0 0 0 0 0 0 0 0 0 0 0]; %Itself
1379
     1380
     B(22,21,:) = [7 2 0 0 0 0 0 0 0 0 0 0 0 0]; "Backward
1381
     1382
     Left
     B(22,23,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
1383
     Right
     B(22,24,:) = [7 4 0 0 0 0 0 0 0 0 0 0 0 0 0]; "Left
1384
     1385
     B(22,26,:) = [7 1 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
1386
     B(22,27,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
1387
     Right
     %
1388
1389
     B(23,1,:) = [3 3 4 4 7 7 8 8 0 0 0 0 0 0 0]; %Itself
1390
     1391
     B(23,3,:) = [4 \ 1 \ 3 \ 2 \ 8 \ 5 \ 7 \ 6 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0]; Backward
1392
     B(23,4,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
1393
     Left
     1394
     Right
     B(23,6,:) = [3 4 7 8 0 0 0 0 0 0 0 0 0 0]; Left
1395
     1396
     B(23,8,:) = [3 1 7 5 0 0 0 0 0 0 0 0 0 0]; Backward +
     Left
     B(23,9,:) = [4 2 8 6 0 0 0 0 0 0 0 0 0 0]; Backward +
1398
     Right
     %Up
1399
     B(23,10,:) = [4 8 3 7 0 0 0 0 0 0 0 0 0 0]; %Itself
1400
     1401
     B(23,12,:) = [3 6 4 5 0 0 0 0 0 0 0 0 0 0]; "Backward
1402
     B(23,13,:) = [0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0]; Forward +
1403
     Left
     B(23,14,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
1404
     Right
     B(23,15,:) = [3 8 0 0 0 0 0 0 0 0 0 0 0 0]; %Left
1405
     B(23,16,:) = [4 7 0 0 0 0 0 0 0 0 0 0 0 0]; "Right
1406
     B(23,17,:) = [3 5 0 0 0 0 0 0 0 0 0 0 0 0];
*Backward +
1407
     Left
     B(23,18,:) = [4 6 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Backward +
1408
     Right
     %Down
1409
```

```
B(23,19,:) = [8 4 7 3 0 0 0 0 0 0 0 0 0 0]; %Itself
1410
     1411
     B(23,21,:) = [8 1 7 2 0 0 0 0 0 0 0 0 0 0 0]; "Backward
1412
1413
     B(23,22,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
    Left
     B(23,23,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
1414
    Right
     B(23,24,:) = [7 4 0 0 0 0 0 0 0 0 0 0 0 0]; %Left
1415
1416
     B(23,26,:) = [7 1 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
1417
    Left
     B(23,27,:) = [8 2 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
1418
    Right
1419
     %
     B(24,1,:) = [4 4 8 8 0 0 0 0 0 0 0 0 0 0]; %Itself
     1421
     1422
     B(24,4,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
1423
     1424
    Right
     1425
     1426
     B(24,8,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
1427
    Left
     B(24,9,:) = [4 2 8 6 0 0 0 0 0 0 0 0 0 0]; Backward +
1428
    Right
     %Up
1429
     B(24,10,:) = [4 8 0 0 0 0 0 0 0 0 0 0 0 0];%Itself
1430
     1431
     B(24,12,:) = [4 5 0 0 0 0 0 0 0 0 0 0 0 0 0]; "Backward
1432
     1433
    Left
     B(24,14,:) = [0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0]; Forward +
1434
    Right
     B(24,15,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Left
1435
     B(24,16,:) = [4 7 0 0 0 0 0 0 0 0 0 0 0 0]; %Right
1436
     B(24,17,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
1437
    Left
     B(24,18,:) = [4 6 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
1438
    Right
     %Down
1439
     B(24,19,:) = [8 4 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Itself
1440
     1441
     B(24,21,:) = [8 1 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Backward
```

```
B(24,22,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
1443
     B(24,23,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
1444
     Right
     B(24,24,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; Left
1445
     1446
     B(24,26,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Backward +
1447
     Left
     B(24,27,:) = [8 2 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
1448
     Right
     %
1449
     B(25,1,:) = [7 7 0 0 0 0 0 0 0 0 0 0 0 0]; %Itself
1450
     B(25,3,:) = [7 6 0 0 0 0 0 0 0 0 0 0 0 0]; Backward
1452
     B(25,4,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
1453
     Left
     B(25,5,:) = [0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0]; Forward +
1454
     Right
     B(25,6,:) = [7 8 0 0 0 0 0 0 0 0 0 0 0 0]; Left
1455
     1456
     B(25,8,:) = [7 5 0 0 0 0 0 0 0 0 0 0 0 0]; "Backward +
1457
     Left
     1458
     Right
     %Up
1459
     B(25,10,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Itself
1460
     B(25,11,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward
1461
     B(25,12,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0]; "Backward
1462
     B(25,13,:) = [0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0]; Forward +
1463
     Left
     1464
     Right
     1465
     B(25,16,:) = [0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0];Right
1466
     B(25,17,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
1467
     Left
     B(25,18,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Backward +
1468
     Right
     %Down
1469
     1470
     1471
     B(25,21,:) = [7 2 0 0 0 0 0 0 0 0 0 0 0 0]; "Backward
1472
     B(25,22,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
1473
     Left
     B(25,23,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
1474
     Right
```

```
B(25,24,:) = [7 4 0 0 0 0 0 0 0 0 0 0 0 0 0]; Left
1475
     B(25,25,:) = [0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0];Right
1476
     B(25,26,:) = [7 1 0 0 0 0 0 0 0 0 0 0 0 0]; "Backward +
1477
    Left
     1478
    Right
     %
1479
     . . . .
     B(26,1,:) = [7 7 8 8 0 0 0 0 0 0 0 0 0 0]; %Itself
1480
     1481
     B(26,3,:) = [8 5 7 6 0 0 0 0 0 0 0 0 0 0]; Backward
1482
     1483
    Left
     Right
     B(26,6,:) = [7 8 0 0 0 0 0 0 0 0 0 0 0 0]; Left
1485
     B(26,7,:) = [8 7 0 0 0 0 0 0 0 0 0 0 0 0]; %Right
1486
1487
     B(26,8,:) = [7 5 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
    Left
     B(26,9,:) = [8 6 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
1488
    Right
     %Up
1489
     B(26,10,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Itself
1490
     1491
     B(26,12,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0]; "Backward
1492
     1493
    Left
     B(26,14,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
1494
    Right
     B(26,15,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Left
1495
     B(26,16,:) = [0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0]; Right
     B(26,17,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
1497
    Left
     B(26,18,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
1498
    Right
     %Down
1499
     B(26,19,:) = [7 3 8 4 0 0 0 0 0 0 0 0 0 0]; %Itself
1500
     B(26,21,:) = [8 1 7 2 0 0 0 0 0 0 0 0 0 0]; "Backward
     1503
    Left
     B(26,23,:) = [0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0]; Forward +
1504
    Right
     B(26,24,:) = [7 4 0 0 0 0 0 0 0 0 0 0 0 0]; %Left
     1506
     B(26,26,:) = [7 1 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
1507
    Left
```

```
B(26,27,:) = [8 2 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
1508
     Right
1509
     %
     B(27,1,:) = [8 8 0 0 0 0 0 0 0 0 0 0 0 0]; %Itself
1510
     1511
     B(27,3,:) = [8 5 0 0 0 0 0 0 0 0 0 0 0 0];%Backward
1512
     1513
     Left
     B(27,5,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
1514
     Right
     B(27,6,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0]; "Left"
1515
     B(27,7,:) = [8 7 0 0 0 0 0 0 0 0 0 0 0 0];%Right
1516
     B(27,8,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
1517
     Left
     B(27,9,:) = [8 6 0 0 0 0 0 0 0 0 0 0 0 0 0]; "Backward +
1518
     Right
     %Up
1519
     B(27,10,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; "Itself
1520
     B(27,11,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward
     B(27,13,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
     Left
     B(27,14,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Forward +
1524
     Right
     B(27,16,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; "Right
1526
     B(27,17,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
     Left
     B(27,18,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
1528
     Right
     %Down
1529
     B(27,19,:) = [8 4 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Itself
1530
     1531
     B(27,21,:) = [8 1 0 0 0 0 0 0 0 0 0 0 0 0];%Backward
1532
     B(27,22,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]; Forward +
1533
     Left
     1534
     Right
     B(27,24,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Left
     1536
     B(27,26,:) = [0 0 0 0 0 0 0 0 0 0 0 0 0 0]; Backward +
     B(27,27,:) = [8 2 0 0 0 0 0 0 0 0 0 0 0 0 0]; %Backward +
     Right
1539 return
1540
```

```
1541 function [K11, K12, K13, K22, K23, K33, M] = SmallMatrix(Delta)
1542 % {
1543
   syms x
1544
   syms y
1545
1546 SYMS Z
   mwb.Update(2, 1, 0, ['Matrix Creation ' num2str(10) '%']);
   Q = zeros(64,1)*x;
1549 icount = 1;
   for i = 0:3
      for j = 0:3
         for k = 0:3
              Q(icount,1) = x^i*y^j*z^k;
              icount = icount + 1;
1554
          end
      end
1556
   end
1557
   mwb.Update(2, 1, 0, ['Matrix Creation 'num2str(20) '%']);
   K11 = zeros(size(Q,1))*x*y*z;
1559
1560 | K12 = zeros(size(Q,1))*x*y*z;
1561 K13 = zeros(size(Q,1))*x*y*z;
1562 K22 = zeros(size(Q,1))*x*y*z;
1563 K23 = zeros(size(Q,1))*x*y*z;
1564 K33 = zeros(size(Q,1))*x*y*z;
       = zeros(size(Q,1))*x*y*z;
1565
   mwb.Update(2, 1, 0, ['Matrix Creation ' num2str(25) '%']);
   for i = 1:size(Q,1)
1567
      for j = 1:size(Q,1)
         K11(j,i) = diff(Q(j),x)*diff(Q(i),x);
1569
         K12(j,i) = diff(Q(j),y)*diff(Q(i),x);
         K13(j,i) = diff(Q(j),z)*diff(Q(i),x);
1571
         K22(j,i) = diff(Q(j),y)*diff(Q(i),y);
1572
         K23(j,i) = diff(Q(j),z)*diff(Q(i),y);
1573
         K33(j,i) = diff(Q(j),z)*diff(Q(i),z);
1574
         M(j,i)
                 = Q(j)*Q(i);
1575
1576
   end
   mwb.Update(2, 1, 0, ['Matrix Creation 'num2str(30) '%']);
1578
1579 K11 = int(int(K11,x,[0,1]),y,[0,1]),z,[0,1]);
1580 K12 = int(int(int(K12,x,[0,1]),y,[0,1]),z,[0,1]);
   K13 = int(int(K13,x,[0,1]),y,[0,1]),z,[0,1]);
   K22 = int(int(K22,x,[0,1]),y,[0,1]),z,[0,1]);
1582
1583 K23 = int(int(int(K23,x,[0,1]),y,[0,1]),z,[0,1]);
1584 K33 = int(int(int(K33,x,[0,1]),y,[0,1]),z,[0,1]);
       = int(int(int(M,x,[0,1]),y,[0,1]),z,[0,1]);
nsse | mwb.Update(2, 1, 0, ['Matrix Creation ' num2str(35) '%']);
T = MATRIX_T(Q);
1588 Tinv = inv(T);
```

```
nwb.Update(2, 1, 0, ['Matrix Creation ' num2str(40) '%']);
   K11 = (Tinv)'*K11*Tinv;
   K12 = (Tinv)'*K12*Tinv;
1591
   K13 = (Tinv)'*K13*Tinv;
1592
1593 K22 = (Tinv)'*K22*Tinv;
1594 \text{ K23} = (\text{Tinv})'*\text{K23}*\text{Tinv};
1595 \text{ K33} = (Tinv)'*K33*Tinv;
        = (Tinv)'*M*Tinv;
1596 M
   mwb.Update(2, 1, 0, ['Matrix Creation ' num2str(45) '%']);
1598
   save('matrices.mat','K11','K12','K13','K22','K23','K33','M');
1599
1600 %}
1601 L = load('matrices.mat');
1602 \text{ K11} = \text{L.K11};
1603 | K12 = L.K12;
_{1604} K13 = L.K13;
1605 | K22 = L.K22;
1606 | K23 = L.K23;
1607
   K33 = L.K33;
_{1608} M = L.M;
1609
1610
K11 = double(K11*Delta(2)*Delta(3)/Delta(1));
1612 K12 = double(K12*Delta(3));
1613 K13 = double(K13*Delta(2));
   K22 = double(K22*Delta(1)*Delta(3)/Delta(2));
1615 K23 = double(K23*Delta(1));
1616 K33 = double(K33*Delta(1)*Delta(2)/Delta(3));
        = double(M*Delta(1)*Delta(2)*Delta(3));
1618 %mwb.Update(2, 1, 0, ['Matrix Creation 'num2str(50) '%']);
1619 return
1621 function T = MATRIX_T(Q)
1622 %{
   syms x;
1623
   syms y;
1624
   syms z;
1625
1626
   n = size(Q,1);
1627
   T = zeros(n);
1628
   for j = 1:n
1629
       T(j,1) = subs(Q(j),[x,y,z],[0,1,0]);
1630
       T(j,2) = subs(Q(j),[x,y,z],[0,0,0]);
1631
       T(j,3) = subs(Q(j),[x,y,z],[1,0,0]);
1632
       T(j,4) = subs(Q(j),[x,y,z],[1,1,0]);
1633
       T(j,5) = subs(Q(j),[x,y,z],[0,1,1]);
1634
       T(j,6) = subs(Q(j),[x,y,z],[0,0,1]);
       T(j,7) = subs(Q(j),[x,y,z],[1,0,1]);
1636
```

```
T(j,8) = subs(Q(j),[x,y,z],[1,1,1]);
1637
1638
1639
      T(j,9) = subs(diff(Q(j),x),[x,y,z],[0,1,0]);
      T(j,10) = subs(diff(Q(j),x),[x,y,z],[0,0,0]);
1640
      T(j,11) = subs(diff(Q(j),x),[x,y,z],[1,0,0]);
1641
      T(j,12) = subs(diff(Q(j),x),[x,y,z],[1,1,0]);
1642
      T(j,13) = subs(diff(Q(j),x),[x,y,z],[0,1,1]);
1643
      T(j,14) = subs(diff(Q(j),x),[x,y,z],[0,0,1]);
1644
      T(j,15) = subs(diff(Q(j),x),[x,y,z],[1,0,1]);
1645
      T(j,16) = subs(diff(Q(j),x),[x,y,z],[1,1,1]);
1646
1647
      T(j,17) = subs(diff(Q(j),y),[x,y,z],[0,1,0]);
1648
1649
      T(j,18) = subs(diff(Q(j),y),[x,y,z],[0,0,0]);
1650
      T(j,19) = subs(diff(Q(j),y),[x,y,z],[1,0,0]);
      T(j,20) = subs(diff(Q(j),y),[x,y,z],[1,1,0]);
      T(j,21) = subs(diff(Q(j),y),[x,y,z],[0,1,1]);
1652
      T(j,22) = subs(diff(Q(j),y),[x,y,z],[0,0,1]);
1653
      T(j,23) = subs(diff(Q(j),y),[x,y,z],[1,0,1]);
1654
1655
      T(j,24) = subs(diff(Q(j),y),[x,y,z],[1,1,1]);
1656
      T(j,25) = subs(diff(Q(j),z),[x,y,z],[0,1,0]);
1657
      T(j,26) = subs(diff(Q(j),z),[x,y,z],[0,0,0]);
1658
      T(j,27) = subs(diff(Q(j),z),[x,y,z],[1,0,0]);
1659
      T(j,28) = subs(diff(Q(j),z),[x,y,z],[1,1,0]);
1660
      T(j,29) = subs(diff(Q(j),z),[x,y,z],[0,1,1]);
1661
      T(j,30) = subs(diff(Q(j),z),[x,y,z],[0,0,1]);
1662
      T(j,31) = subs(diff(Q(j),z),[x,y,z],[1,0,1]);
1663
      T(j,32) = subs(diff(Q(j),z),[x,y,z],[1,1,1]);
1665
      T(j,33) = subs(diff(diff(Q(j),x),y),[x,y,z],[0,1,0]);
      T(j,34) = subs(diff(diff(Q(j),x),y),[x,y,z],[0,0,0]);
1667
      T(j,35) = subs(diff(diff(Q(j),x),y),[x,y,z],[1,0,0]);
1668
      T(j,36) = subs(diff(diff(Q(j),x),y),[x,y,z],[1,1,0]);
1669
      T(j,37) = subs(diff(diff(Q(j),x),y),[x,y,z],[0,1,1]);
1670
      T(j,38) = subs(diff(diff(Q(j),x),y),[x,y,z],[0,0,1]);
1671
      T(j,39) = subs(diff(diff(Q(j),x),y),[x,y,z],[1,0,1]);
1672
      T(j,40) = subs(diff(diff(Q(j),x),y),[x,y,z],[1,1,1]);
1673
1674
      T(j,41) = subs(diff(diff(Q(j),x),z),[x,y,z],[0,1,0]);
1675
      T(j,42) = subs(diff(diff(Q(j),x),z),[x,y,z],[0,0,0]);
1676
      T(j,43) = subs(diff(diff(Q(j),x),z),[x,y,z],[1,0,0]);
1677
      T(j,44) = subs(diff(diff(Q(j),x),z),[x,y,z],[1,1,0]);
1678
      T(j,45) = subs(diff(diff(Q(j),x),z),[x,y,z],[0,1,1]);
1679
      T(j,46) = subs(diff(diff(Q(j),x),z),[x,y,z],[0,0,1]);
1680
      T(j,47) = subs(diff(diff(Q(j),x),z),[x,y,z],[1,0,1]);
      T(j,48) = subs(diff(diff(Q(j),x),z),[x,y,z],[1,1,1]);
1682
1683
      T(j,49) = subs(diff(diff(Q(j),y),z),[x,y,z],[0,1,0]);
1684
```

```
T(j,50) = subs(diff(diff(Q(j),y),z),[x,y,z],[0,0,0]);
1685
   T(j,51) = subs(diff(diff(Q(j),y),z),[x,y,z],[1,0,0]);
1686
   T(j,52) = subs(diff(diff(Q(j),y),z),[x,y,z],[1,1,0]);
1687
   T(j,53) = subs(diff(diff(Q(j),y),z),[x,y,z],[0,1,1]);
1688
   T(j,54) = subs(diff(diff(Q(j),y),z),[x,y,z],[0,0,1]);
1689
   T(j,55) = subs(diff(diff(Q(j),y),z),[x,y,z],[1,0,1]);
1690
   T(j,56) = subs(diff(diff(Q(j),y),z),[x,y,z],[1,1,1]);
1691
1692
   T(j,57) = subs(diff(diff(Q(j),x),z),y),[x,y,z],[0,1,0])
1693
   T(j,58) = subs(diff(diff(Q(j),x),z),y),[x,y,z],[0,0,0])
   T(j,59) = subs(diff(diff(Q(j),x),z),y),[x,y,z],[1,0,0])
   T(j,60) = subs(diff(diff(Q(j),x),z),y),[x,y,z],[1,1,0])
   T(j,61) = subs(diff(diff(Q(j),x),z),y),[x,y,z],[0,1,1])
1697
1698
   T(j,62) = subs(diff(diff(Q(j),x),z),y),[x,y,z],[0,0,1])
   T(j,63) = subs(diff(diff(Q(j),x),z),y),[x,y,z],[1,0,1])
1699
   T(j,64) = subs(diff(diff(Q(j),x),z),y),[x,y,z],[1,1,1])
1700
 end
1701
 %}
1702
 1703
   0 0 0 0 0;
  0 0 0;
  1705
   0 0 0;
  1706
   0 0 0;
  1707
   0 0 0;
  1708
   0 0 0;
  0 0 0;
```

```
0 0 0:
      1 \;\; 0 \;\; 0 \;\; 1 \;\; 1 \;\; 0 \;\; 0 \;\; 1 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\; 0 \;\;
1711
          0 0 0;
      0 0 0;
      1713
          0 0 0;
      0 0 0:
      1 0 0 1 1 0 0 1 0 0 0 0 0 0 0 0 3 0 0 3 3 0 0 3 0 0 0 0 0 0
         0 0 0;
      1716
          1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 3 0 0 3 3 0 0 3 0 0 0 0
           0 0 0;
      1717
          0 0 0;
      1718
         0 0 0;
      0 0 0;
      1720
         0 0 0:
      0 0 0:
      3 0 0 0 0 0 0 0 0 0 0 0 0 3 3 3 3 0 0 0 0 0 0 0 0 0 0 0 0 0
           0 0 0;
      1723
          0 0 0:
      1 1 1;
      2 2 2:
```

```
1726
3 3 3:
0 0 0;
0 0 2;
1729
0 0 4;
0 0 6;
1731
0 0 0;
1732
1 0 0 0 0 3 0 0 3 1 0 0 1 1 0 0 1 0 0 0 3 0 0 0 3 3 0 0 3 3
0 0 3;
1733
0 0 6;
1734
0 0 9;
0 0 0;
1736
0 0 0:
0 0 0:
3 0 0 0 0 0 0 0 0 0 0 0 0 0 0 6 6 0 0 0 0 0 0 0 0 0 0 0 0
0 0 0;
1739
0 0 0:
1740
0 2 2;
0 4 4:
```

1742	0	0 0 0 3 0 0	0 0	0	1			0	0	0			2			0			0	1	1	0 3		0	0	0	0	0
1743	0	0 6 6 0 0 1 0 0 0	0 0																								0	
1744	0	0 0 0 0 0 0 1 0 0	0 0																									
1745	0	0 0 4 0 0 0 2 0 0	; 0 0	0	1	0	0	0	0	0	0	0	2	0	0	0	0	0	0	0	2	0	0	0	0	0	0	0
1746	0	0 0 8	; 0 0	0	1	0	0	0	0	0	0	0	2	0	0	0	0	0	0	0	2	0	0	0	0	0	0	0
1747	0	3 0 0 0 0 1 0 0 1	2;																								0	
		0 0 0	;																									
1748	0	0 0 0 1 0 0 0 6	0 0																									
1749	0	0 0 0 2 0 0	0 0																							0	0	-
1750	0	0 0 1 0 0 0 3 0 0	0 0																							0	0	
1751	0	0 0 1 0 1 1 0 0 0	0 0																								0	
1752	0	0 0 0	; 0 0	1	1	0	0	0	0	0	0	3	3	0	0	0	0	0	0	0	0	0	0	1	1		0	
1753	0	1 0 0 0 0 0 0 0	;														0									0	0	
	•	2 0 0	;																							_	0	
1754	O	0 0 0 3 0 0 0	0 0	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_
1755	0	0 0 1 0 0 0 0 0 0	3 3																									
1756	0	0 0 0 1 0 0	0 0																									
1757	0	0 3 3 0 0 0 2 0 0	0 0																									
		0 6 6																										

```
0 9 9:
 0 0 0;
 0 0 6;
 1761
  0 0 18;
 0 0 0;
 1 0 0 0 0 0 0 0 9 0 0 0 3 0 0 0 3 0 0 0 3 0 0 0 3 0 0 0 9 0
 0 0 18;
 3 0 0 0 0 0 0 0 9 0 0 0 0 0 0 0 9 0 0 0 0 0 0 0 9 0 0 0 0
   0 0 27];
_{1767} | T = T';
 return;
1768
 function [B11,B12,B13,B22,B23,B33,BM] = AddMatrix(K11,K12,K13,
  K22, K23, K33, M)
B = AdjacentType();
_{1772} B11 = zeros(216,216);
B12 = zeros(216,216);
_{1774} B13 = zeros(216,216);
B22 = zeros(216,216);
_{1776} B23 = _{zeros}(216,216);
| 1777 | B33 = zeros(216,216);
 BM = zeros(216, 216);
1778
 for g = 1:8
1779
   for f = 1:8
1780
    for i = 1:27
1781
      for j = 1:27
1782
       for k = 1:2:15
         if B(i,j,k) \sim 0
1784
          B11(i+(g-1)*27, j+(f-1)*27) = B11(i+(g-1)
  *27, j+(f-1)*27) + K11(B(i,j,k)+(g-1)*8,B(i,j,k+1)+(f-1)*8);
```

```
B12(i+(g-1)*27, j+(f-1)*27) = B12(i+(g-1)
1786
                                     *27, j+(f-1)*27 + K12(B(i,j,k)+(g-1)*8,B(i,j,k+1)+(f-1)*8);
                                                                                                                                     B13(i+(g-1)*27, j+(f-1)*27) = B13(i+(g-1)
                                     *27, j+(f-1)*27) + K13(B(i,j,k)+(g-1)*8,B(i,j,k+1)+(f-1)*8);
                                                                                                                                     B22(i+(g-1)*27, j+(f-1)*27) = B22(i+(g-1)
1788
                                     *27,j+(f-1)*27) + K22(B(i,j,k)+(g-1)*8,B(i,j,k+1)+(f-1)*8);
                                                                                                                                     B23(i+(g-1)*27, j+(f-1)*27) = B23(i+(g-1)
                                     *27, j+(f-1)*27) + K23(B(i,j,k)+(g-1)*8,B(i,j,k+1)+(f-1)*8);
                                                                                                                                     B33(i+(g-1)*27, j+(f-1)*27) = B33(i+(g-1)
                                     *27,j+(f-1)*27) + K33(B(i,j,k)+(g-1)*8,B(i,j,k+1)+(f-1)*8);
                                                                                                                                      BM(i+(g-1)*27,j+(f-1)*27) = BM(i+(g-1)*27,j
1791
                                     +(f-1)*27) + M(B(i,j,k)+(g-1)*8,B(i,j,k+1)+(f-1)*8);
                                                                                                                           else
                                                                                                                                                  break
1799
                                                                                                                           end
1794
                                                                                                   end
1795
                                                                                  end
1796
1797
                                                                end
                                          end
1798
1799
                  end
                  return;
1800
1801
                  function [K11,K12,K13,K22,K23,K33,M,D,E] = Matrices(Delta,N,
1802
                                     method)
                 %mwb.Update(2, 1, 0, ['Matrix Creation ' num2str(0) '%']);
1803
                   [K11q,K12q,K13q,K22q,K23q,K33q,Mq] = SmallMatrix(Delta);
                   [B11,B12,B13,B22,B23,B33,BM] = AddMatrix(K11q,K12q,K13q,K22q,
1805
                                     K23q, K33q, Mq);
                 % {
1806
                 K11 = spalloc((N(1)+1)*(N(2)+1)*(N(3)+1),(N(1)+1)*(N(2)+1)*(N(3)+1),(N(1)+1)*(N(2)+1)*(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)+1),(N(3)
                                     (3)+1),(N(1)+1)*(N(2)+1)*(N(3)+1)*27);
                 K12 = \text{spalloc}((N(1)+1)*(N(2)+1)*(N(3)+1),(N(1)+1)*(N(2)+1)*(N(3)+1))
                                      (3)+1),(N(1)+1)*(N(2)+1)*(N(3)+1)*27);
                 K13 = \text{spalloc}((N(1)+1)*(N(2)+1)*(N(3)+1),(N(1)+1)*(N(2)+1)*(N(3)+1))
1809
                                     (3)+1),(N(1)+1)*(N(2)+1)*(N(3)+1)*27);
1810 \times 22 = \text{spalloc}((N(1)+1)*(N(2)+1)*(N(3)+1),(N(1)+1)*(N(2)+1)*(N(2)+1)*(N(3)+1),(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)
                                     (3)+1),(N(1)+1)*(N(2)+1)*(N(3)+1)*27);
                 K23 = spalloc((N(1)+1)*(N(2)+1)*(N(3)+1),(N(1)+1)*(N(2)+1)*(N(2)+1)*(N(3)+1),(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)
1811
                                     (3)+1),(N(1)+1)*(N(2)+1)*(N(3)+1)*27);
                 K33 = spalloc((N(1)+1)*(N(2)+1)*(N(3)+1),(N(1)+1)*(N(2)+1)*(N(3)+1),(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)+1)*(N(3)
1812
                                     (3)+1),(N(1)+1)*(N(2)+1)*(N(3)+1)*27);
                 M = \text{spalloc}((N(1)+1)*(N(2)+1)*(N(3)+1),(N(1)+1)*(N(2)+1)*(N(3)+1)
1813
                                     +1),(N(1)+1)*(N(2)+1)*(N(3)+1)*27);
1814 %}
1815
                  [D,E] = Domain(N,Delta);
                 A = Adjacent(N,D);
1816
                T = Type(N,A);
1818 %
```

```
1819
   %mwb.Update(2, 1, 0, ['Matrix Creation 'num2str(55) '%']);
1820
1821
   %{
   for i = 1:(N(1)+1)*(N(2)+1)*(N(3)+1)
1822
        mwb.Update(2, 1, i/((N(1)+1)*(N(2)+1)*(N(3)+1)+1), ['Matrix]
1823
        Creation ' num2str(i/((N(1)+1)*(N(2)+1)*(N(3)+1)+1)*100)'
       %']);
        for j = 1:27
1824
           k = 1;
1825
           while (B(T(i),j,k) ~= 0 && ~isnan(A(i,j)))
1826
                  K11(i,A(i,j)) = K11(i,A(i,j)) + K11q(B(T(i),j,k),B(i,j))
1827
       T(i), j, k+1));
                 K12(i,A(i,j)) = K12(i,A(i,j)) + K12q(B(T(i),j,k),B(i,j))
       T(i), j, k+1));
                 K13(i,A(i,j)) = K13(i,A(i,j)) + K13q(B(T(i),j,k),B(i,j))
1829
       T(i),j,k+1));
                 K22(i,A(i,j)) = K22(i,A(i,j)) + K22q(B(T(i),j,k),B(i,j))
1830
       T(i), j, k+1));
1831
                 K23(i,A(i,j)) = K23(i,A(i,j)) + K23q(B(T(i),j,k),B(i,j))
       T(i), j, k+1));
                 K33(i,A(i,j)) = K33(i,A(i,j)) + K33q(B(T(i),j,k),B(i,j))
1832
       T(i), j, k+1));
1833
                 M(i,A(i,j)) = M(i,A(i,j)) + Mq(B(T(i),j,k),B(T(i),j)
1834
       ,k+1));
                 k = k + 2;
                  if(k >= 16)
1836
                     break;
1837
                  end
1838
1839
            end
        end
1840
1841
   end
   %}
1842
   n = 0;
1843
   for i = 1:(N(1)+1)*(N(2)+1)*(N(3)+1)
1844
        for j = 1:27
1845
          if ~isnan(A(i,j))
1846
              n = n + 1;
1847
          end
1848
        end
1849
   end
1850
1851
1852 % {
1853
   %}
1854
   %{
1855
1857 NAN_A = ^{\sim}isnan(A);
```

```
1858 A2 = repmat(A(:,1),1,size(A,2));
   A3 = repmat([1:27]',1,size(A,1))';
   iy = A(NAN_A);
   ix = A2(NAN_A);
1861
   iz = A3(NAN_A);
1862
1863 [ix iy iz];
   for i = 1:size(iy,1)
1865
        mwb.Update(2, 1, i/(size(iy,1)), ['Matrix Creation '
1866
       num2str(i/size(iy,1)*100) '%']);
       k = 1;
1867
        while (k < 16 \&\& B(T(ix(i)), iz(i), k) = 0)
1868
            K11s(i) = K11s(i) + K11q(B(T(ix(i)),iz(i),k),B(T(ix(i)))
1869
       ,iz(i),k+1));
            K12s(i) = K12s(i) + K12q(B(T(ix(i)),iz(i),k),B(T(ix(i)))
       ,iz(i),k+1));
            K13s(i) = K13s(i) + K13q(B(T(ix(i)),iz(i),k),B(T(ix(i)))
1871
       ,iz(i),k+1));
1872
            K22s(i) = K22s(i) + K22q(B(T(ix(i)),iz(i),k),B(T(ix(i)))
       ,iz(i),k+1));
            K23s(i) = K23s(i) + K23q(B(T(ix(i)),iz(i),k),B(T(ix(i)))
1873
       ,iz(i),k+1));
            K33s(i) = K33s(i) + K33q(B(T(ix(i)),iz(i),k),B(T(ix(i)))
1874
       ,iz(i),k+1));
            Ms(i) = Ms(i) + Mq(B(T(ix(i)),iz(i),k),B(T(ix(i)),iz(i))
1875
       ,k+1));
            k = k + 2;
1876
        end
1877
   end
1878
   %}
1879
   %%{
1880
1881
   if (method == 2)
1882
      % mwb.Update(2, 1, 0.1, ['Matrix Creation ' num2str(55)
1883
       '%']);
        InvA = A';
1884
        NAN_A = ~isnan(InvA);
1885
        A2 = repmat([1:27]',1,size(InvA,2))';
1886
        A3 = repmat(1:size(A,1),size(A,2),1);
1887
        InvA3 = A3';
1888
        InvA2 = A2';
1889
        iy1 = InvA(NAN_A);
1890
        ix1 = InvA3(NAN_A);
1891
        iz1 = InvA2(NAN_A);
1892
        Typex1 = T(ix1);
1893
1894
        iy = [];
1895
        ix = [];
1896
```

```
iz = [];
1897
        Typex = [];
1898
1899
1900
        for i = 1:8
1901
           for j = 1:8
1902
               iy = [iy; iy1+(j-1)*size(A,1)];
1903
               iz = [iz; iz1+(j-1)*27];
1904
               ix = [ix; ix1+(i-1)*size(A,1)];
1905
               Typex = [Typex; Typex1+(i-1)*27];
1906
           end
1907
        end
1908
1909
1910
1911
        %BAdd = B(Typex, Typey,:);
1912
       %mwb.Update(2, 1, 0.2, ['Matrix Creation 'num2str(60)
1913
       '%']);
1914
        K11s = B11(sub2ind(size(B11), Typex, iz));
        %mwb.Update(2, 1, 0.3, ['Matrix Creation 'num2str(65)
1915
       '%']);
       K12s = B12(sub2ind(size(B12), Typex, iz));
1916
       %mwb.Update(2, 1, 0.4, ['Matrix Creation 'num2str(70)
1917
       '%']);
        K13s = B13(sub2ind(size(B13), Typex, iz));
1918
        %mwb.Update(2, 1, 0.5, ['Matrix Creation 'num2str(75)
1919
       '%']);
       K22s = B22(sub2ind(size(B22), Typex, iz));
1920
       %mwb.Update(2, 1, 0.6, ['Matrix Creation 'num2str(80)
1921
       '%']);
       K23s = B23(sub2ind(size(B23), Typex, iz));
1922
       %mwb.Update(2, 1, 0.7, ['Matrix Creation 'num2str(85)
1923
       '%']);
        K33s = B33(sub2ind(size(B33), Typex, iz));
       %mwb.Update(2, 1, 0.8, ['Matrix Creation 'num2str(90)
1925
       '%']);
       Ms = BM(sub2ind(size(BM), Typex, iz));
1926
       %mwb.Update(2, 1, 0.9, ['Matrix Creation 'num2str(95)
1927
       '%']);
   elseif (method == 1)
1928
        B = AdjacentType();
1929
        K11s = zeros(n,1);
1930
        K12s = zeros(n,1);
1931
        K13s = zeros(n,1);
1932
        K22s = zeros(n,1);
1933
        K23s = zeros(n,1);
1934
        K33s = zeros(n,1);
1935
        Ms = zeros(n,1);
1936
```

```
ix = zeros(n,1);
1937
                    iy = zeros(n,1);
1938
                    ii = 1;
1939
                    for i = 1:(N(1)+1)*(N(2)+1)*(N(3)+1)
1940
                                mwb.Update(2, 1, i/((N(1)+1)*(N(2)+1)*(N(3)+1)+1), ['
1941
                  Matrix Creation ' num2str(i/((N(1)+1)*(N(2)+1)*(N(3)+1)+1)
                  *100) '%']);
                                for j = 1:27
1942
                                      if ~isnan(A(i,j))
1943
                                               ix(ii) = A(i,1);
1944
                                               iy(ii) = A(i,j);
1945
                                              k = 1;
1946
                                               while (B(T(i),j,k) = 0 \&\& sinan(A(i,j)))
1948
                                                       K11s(ii) = K11s(ii) + K11q(B(T(i),j,k),B(T(i),j)
1949
                   ,k+1));
                                                       K12s(ii) = K12s(ii) + K12q(B(T(i),j,k),B(T(i),j)
1950
                   ,k+1));
1951
                                                       K13s(ii) = K13s(ii) + K13q(B(T(i),j,k),B(T(i),j)
                   ,k+1));
                                                       K22s(ii) = K22s(ii) + K22q(B(T(i),j,k),B(T(i),j)
1952
                   ,k+1));
                                                       K23s(ii) = K23s(ii) + K23q(B(T(i),j,k),B(T(i),j)
1953
                   ,k+1));
                                                       K33s(ii) = K33s(ii) + K33q(B(T(i),j,k),B(T(i),j)
1954
                   ,k+1));
                                                       Ms(ii) = Ms(ii) + Mq(B(T(i),j,k),B(T(i),j,k+1))
1955
                                                       k = k + 2;
1956
                                                        if(k >= 16)
1957
                                                                 break;
1958
                                                        end
1959
1960
                                               Tempi(ii) = T(i);
1961
                                                          Tempj(ii) = j;
1962
                                               ii = ii +1;
1963
1964
                                      end
                                end
1965
                    end
1966
1967
         end
1968
1969
         K11 = sparse(ix, iy, K11s, 8*(N(1)+1)*(N(2)+1)*(N(3)+1), 8*(N(1)+1)
                  *(N(2)+1)*(N(3)+1));
        K12 = sparse(ix, iy, K12s, 8*(N(1)+1)*(N(2)+1)*(N(3)+1), 8*(N(1)+1)
                  *(N(2)+1)*(N(3)+1));
| 1972 | K13 = sparse(ix, iy, K13s, 8*(N(1)+1)*(N(2)+1)*(N(3)+1), 8*(N(1)+1) | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 | 1972 
                  *(N(2)+1)*(N(3)+1));
```

```
K22 = sparse(ix, iy, K22s, 8*(N(1)+1)*(N(2)+1)*(N(3)+1), 8*(N(1)+1)
       *(N(2)+1)*(N(3)+1));
   K23 = sparse(ix, iy, K23s, 8*(N(1)+1)*(N(2)+1)*(N(3)+1), 8*(N(1)+1)
1974
       *(N(2)+1)*(N(3)+1));
   K33 = sparse(ix, iy, K33s, 8*(N(1)+1)*(N(2)+1)*(N(3)+1), 8*(N(1)+1)
1975
       *(N(2)+1)*(N(3)+1));
   M = sparse(ix, iy, Ms, 8*(N(1)+1)*(N(2)+1)*(N(3)+1), 8*(N(1)+1)*(N(3)+1))
        (2)+1)*(N(3)+1));
   % {
1977
   B(T(1:(N(1)+1)*(N(2)+1)*(N(3)+1)),1:27,2:2:16)
1978
   K11q(B(T(1:(N(1)+1)*(N(2)+1)*(N(3)+1)),1:27,1:2:15),B(T(1:(N(1)+1)),1:27,1:2:15)
       +1)*(N(2)+1)*(N(3)+1)),1:27,2:2:16))
1980
   sum(K11q(B(T(1:(N(1)+1)*(N(2)+1)*(N(3)+1)),1:27,1:2:15)>0,B(T(1:(N(1)+1)*(N(2)+1)),1:27,1:2:15)>0,B(T(1:(N(1)+1)*(N(2)+1)),1:27,1:2:15)>0
1981
        (1:(N(1)+1)*(N(2)+1)*(N(3)+1)),1:27,2:2:16))>0)
   K11(1:(N(1)+1)*(N(2)+1)*(N(3)+1),1:(N(1)+1)*(N(2)+1)*(N(3)+1))
       = sum(B(T(1:(N(1)+1)*(N(2)+1)*(N(3)+1)),1:27,1:2:15))
1983 K11(1,:)
1984
   size(K11)
   K11(1:(N(1)+1)*(N(2)+1)*(N(3)+1),A(^{i}snan(A(1:(N(1)+1)*(N(2)+1)))
       *(N(3)+1),1:27))) = sum(K11q(B(T(1:(N(1)+1)*(N(2)+1)*(N(2)+1))))
        (3)+1)),1:27,1:2:15)>0,B(T(1:(N(1)+1)*(N(2)+1)*(N(3)+1))
        ,1:27,2:2:1))>0);
   %}
1986
1987
   %mwb.Update(2, 1, 1, ['Matrix Creation ' num2str(100) '%']);
1988
   return;
1989
1990
   function T = Type(N,A)
1991
   T = zeros((N(1)+1)*(N(2)+1)*(N(3)+1),1);
   TEST = [1]
                   10
                         nan
                                  11
                                        nan
                                                       nan
                                                              nan
                                                                     nan
1993
            13
                  nan
                           14
                                 nan
                                                nan
                                                       nan
                                                              nan
                                                                      nan
              nan
                      nan
                             nan
                                    nan
                                            nan
                                                   nan
                                                          nan;
       nan
             2
                                                  3
                   11
                         nan
                                  12
                                         10
                                                         1
                                                                               5
1994
                                                              nan
            14
                                  13
                           15
                                                  4
                                                       nan
                  nan
                                           6
                                                              nan
                                                                      nan
       nan
              nan
                      nan
                             nan
                                    nan
                                            nan
                                                   nan
                                                          nan:
             3
                                                         2
                   12
                                         11
                                                              nan
                                                                               6
1995
                         nan
                                 nan
                                               nan
                                                                     nan
            15
                                  14
                                                  5
                  nan
                          nan
                                        nan
                                                       nan
                                                                      nan
       nan
              nan
                      nan
                             nan
                                     nan
                                            nan
                                                   nan
                                                          nan;
                   13
                                  14
                                                                               7
1996
                         nan
                                        nan
                                                  5
                                                       nan
                                                              nan
                                                                     nan
            16
                           17
                                           8
                                                                        1
                  nan
                                 nan
                                                nan
                                                       nan
                                                              nan
       10
                                      2
             nan
                      11
                            nan
                                           nan
                                                  nan
                                                         nan;
             5
                                         13
                   14
                         nan
                                  15
                                                  6
                                                         4
                                                              nan
                                                                     nan
                                                                               8
1997
            17
                  nan
                           18
                                  16
                                           9
                                                  7
                                                                        2
                                                       nan
                                                              nan
                      12
                                      3
       11
             nan
                             10
                                             1
                                                  nan
                                                         nan;
1998
             6
                   15
                         nan
                                 nan
                                         14
                                               nan
                                                         5
                                                              nan
                                                                               9
                                                                     nan
            18
                  nan
                                  17
                                                  8
                          nan
                                        nan
                                                       nan
                                                              nan
                                                                        3
       12
                             11
                                   nan
                                             2
             nan
                     nan
                                                  nan
                                                         nan;
```

```
7 16 nan 17 nan 8 nan nan
1999
                                      nan
                                          nan
     nan nan nan nan nan nan
    13 nan 14 nan 5 nan nan nan;
                  18 16 9 7 nan
    8 17 nan 18 16 9 7
nan nan nan nan nan nan
2000
                                      nan
                                          nan
                                  nan
                                      5
    14 nan 15 13 6 4 nan nan;
     9 18 nan nan 17 nan 8 nan
nan nan nan nan nan nan nan
                                          nan
2001
                                      nan
                                       6
    15 nan nan 14 nan 5 nan nan;
      10
           19
               1 20 nan 11 nan
2002
    13
       22 4
              23 nan 14 nan 5
                                    nan
                nan nan nan nan;
    nan
       nan
           nan
           20
                2 21 19 12 10 3
       11
                                       1
2003
    14
       23
           5
                24 22 15 13 6
           nan
                nan nan nan nan;
    nan
       nan
       12
           21
                3 nan 20 nan
                              11 nan
2004
       24
           6
               nan 23 nan 14 nan 5
    15
                nan nan nan nan;
       nan
           nan
    nan
                4 23 nan 14 nan 5
       13
           22
2005
           7
20
                26 nan 17 nan 8 nan
    16
        25
                                        10
    19
        1
                nan 11 nan 2 nan;
       14
           23
                5 24
                       22 15 13
2006
                26
           8
21
                                    7
    17
    20
        2
       15 24
                       23 nan 14 nan
2007
                6 nan
                       nan 17 nan 8
11 nan 2;
       27
           9
               nan 26
                                        12
    18
       3 nan
                20
                   nan 11
       16 25
                7 26 nan 17 nan 8
2008
                nan nan nan nan nan 13
       nan nan
    nan
       4 23
                nan 14 nan 5 nan;
    22
       17 26
                8 27 25 18 16
2009
       nan nan
                nan nan nan nan nan 14
    23 5 24
                22 15 13 6 4;
       18 27
                9 nan 26 nan 17 nan
2010
                nan nan nan nan
       nan nan
                                    nan
    nan
       6 nan 23 nan 14 nan 5;
       19 nan
               10 nan nan 20 nan 11
2011
                                       nan
               nan nan 23 nan 14
       nan 13
    22
                                    nan
       nan
            nan
               nan nan nan nan;
    nan
               11 nan nan 21 19 12
       20 nan
                                        10
2012
                           22
                               15 13
    23
       nan 14
               nan nan 24
                                        nan
               nan nan nan nan
           nan
                               nan;
    nan
       nan
       21 nan
               12 nan nan nan
                               20 nan
                                        11
2013
               nan nan nan 23
    24
       nan 15
                               nan 14
                                        nan
       nan nan
               nan nan nan
                           nan nan;
    nan
       22 nan
               13 nan nan
                           23 nan 14
2014
                                       nan
    25
       nan 16
               nan nan 26
                           nan 17 nan
       10 nan nan 20 nan 11 nan;
    nan
```

```
23 nan 14 nan nan 24 22 15 13
2015
         nan 17
                   nan nan 27
                                   25
                                        18
                                             16
         11 nan
                          21 19 12
                                       10;
     nan
                   nan
                                        23 nan
2016
         24 nan
                   15 nan nan
                                  nan
                                                  14
     27
         nan 18
                   nan nan
                            nan
                                    26
                                        nan
                                              17
                                                   21
                   nan nan 20
     nan
         12
              nan
                                  nan 11;
         25 nan
                                  26 nan 17
                   16
                      nan nan
2017
                                                 nan
                   nan
          nan nan
                         nan nan
                                  nan nan nan
     nan
          13 nan nan
                                   14 nan;
                           23
                              nan
         26 nan
                   17 nan nan
                                   27
                                        25 18
2018
                                            nan
                                         nan
          nan nan
                    nan
                         nan
                               nan
                                    nan
         14
               nan
                           24
                                22
                                    15
                                         13;
      nan
                    nan
                                        26 nan
         27 nan
                   18 nan
                             nan
                                 nan
                                                  17
2019
     nan nan nan
                                         nan
                                              nan
                   nan
                         nan
                              nan
                                    nan
      nan 15 nan nan
                         nan
                                23
                                    nan
                                           14];
  for i = 1:(N(1)+1)*(N(2)+1)*(N(3)+1)
     for j = 1:27
       bflag = true;
2022
       for k = 1:27
2023
2024
          if(isnan(A(i,k))~= isnan(TEST(j,k)))
2025
            bflag = false;
          \verb"end"
2026
       end
2027
       if(bflag == true)
2028
         T(i) = j;
2029
          break;
2030
       end
2031
2032
     end
2033 end
2034 return
```