HW 1 Solution

- (a) At the beginning of the while loop, $K=2^{c}$.
- (b) Base Case: k=1, C=0 => 1=2°

Industrie Step: Let Kou t Cou be the Values of Kandl at the beginning of the While loop Meratron, and let Knew and Chew be these values after the Revolution.

Assume by inductive hypotheses that Row = 2. Note we have know = 2 * Kow and Grev = Cou +1.

Know = 2. Kow = 2(2^{cou}) = 2 = 2.

Artherend of the while loop, we have C=1, and therefore $K=J^2$. Therefore the algorithm is correct.

(c) The while loop runs from C=O to C=N, incrementing C by 1 each iteration. The algorithm runs in O(n) time.

Downing time = 27. leg 20 n = e(nlegn)

Drunning time = 27. leg 20 n = e(nlegn)

D Running time = > 1=1 =

< 103-(3n3) + log(3n3) + ... + log(

= 3 n + tota(3 n >)

Again primary fine

=
$$\frac{2}{2} \log_2^2$$

> $\frac{2}{2} \log_2^2$

= $\log_2(\frac{2n^2}{2}) + \log_2(\frac{2n^2}{2}) + \cdots + \log_2(\frac{2n^2}{2})$

> $\log_2(\frac{2n^2}{2}) + \log_2(\frac{2n^2}{2}) + \cdots + \log_2(\frac{2n^2}{2})$

= $2(n^2 \log n)$

Running fine = θ ($n^2 \log n$)

3. $0 + n^2 - 50 n^2 + 10 n \in \theta(n^5)$

Now $4n^2 - 50 n^2 + 10 n \in \theta(n^5)$

Now $4n^2 - 50 n^2 + 10 n \in \theta(n^5)$
 $1 + n^2 + 10 n \in \theta(n^5)$
 $1 + n^2 + 10 n \in \theta(n^5)$

Many 9 NS - 50 N2 + 10 M 2 4 NS - 50 M2 n5 + (3N5 - 50 N2) if 3m5-50 m2 => N > 3 2 (n5)

(b) 5 n 2/3 + 8 log n & 0(n) 0 + c. Min T. BAN + RION (o (v) (achier) () n + 4 n + 15 > n 5 + 4 n > No for (D. M.) (proved) Inted < DUTON SNS SNS SNO SN.

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