Input: Unsorted array of n distinct number

A [a1, a2, ... an]

output: Index i where of is the smallest in A [a1, a2, ... an] numbur

Divide and conquer algorithm

where each of them has size n/2. Now we have two smaller sub problem from the original one.

Conquer: Solve the sub problems recursively. The base couse will lose the subproblem with size ! and index of that element will be returned

the index of the smallest one. of the smallest element of both. We then compare ATS, I and ATS, I and ATS, I and return combine; from the two subproblem solved

Pseudo code

GREMMIN ENDER (A, i, i) if (133) return i, x = Gref Min Index A (((X) < (X])) GIES Min Index (A, i, i, i, i) return return

Re currence Relation

$$T(m) = \begin{cases} 1, & \text{if } m = 1 \\ 2T(m/2) + 1, & \text{ollowardije} \end{cases}$$

Proof by induction

At first to prove T(n) = O(n)

T(n) < c(n-1) for some constant 0 70

and n> no for some no >0 Givess algorithm takes O(v) time

Assume T(K) < Ck-y for

Now T(n) = 2 T (n/2) +1

< 2 · (() -1)+1

= CM - 2C + 1

1 - (M-1) - C+1

< c(n-1) + (1-c)

: 7(m) = 0(m)

NOW to prove T(n) = 12(n)

T(n) > cn for some constant c>0 70 >0

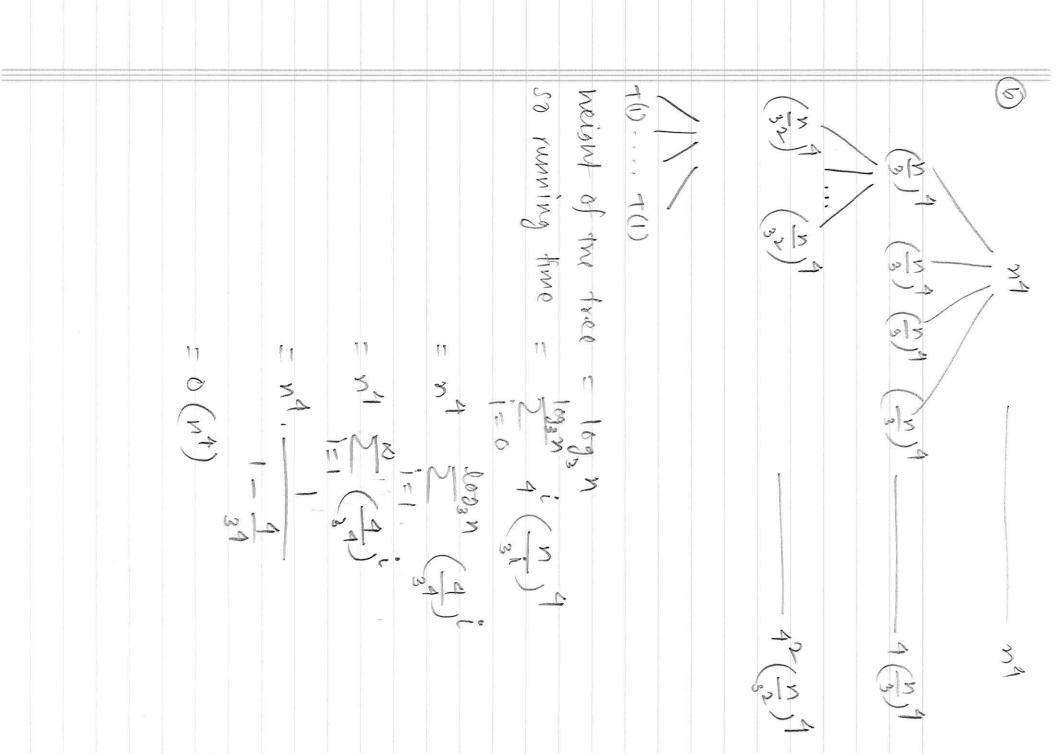
Now T(n) = 2 T (n/2) +1

7 2 C N + -

1 CN+1 +1

from () L (2) T(n) = B(n) : 7(m) = 2(m)

| (4569/24) (= (M) L : | = cm/1082 m mon cm-n->0 | = cn/10g2n - cn/+n/ = cn/(10g2n - 10g6)+n/ = cn/(10g2n - 10g6)+n/ | Proof by indudion: T(n) < cn20gsn Assume T(K) < ch20gsk for k <n< th=""><th>7(0).7(0)</th><th>(5) P (5) P</th><th>(3) (3) (4) (5) (5) (7) (7)</th></n<> | 7(0).7(0) | (5) P | (3) (3) (4) (5) (5) (7) |
|-----------------------|-------------------------|---|---|-----------|--|---|
| | | | | | in the second se | |



```
T(m) = en4 for some constanc

end nyn, 1 n, 70

Assume T(v) < cx4 for all k < n

- 4 cn4 + n4

- 4 cn4 + n4
1 7(n) = 0 (n4)
                                                                                                                                                             broad ph sugnetion
        = cm4 + (m4 + 4cm4) - cm4
                                                                 cmy + (my + 4cmy - 61 cm4
```

to dominate T(n)

to be determined

so m'esua = o(n') we want to find the number of the that the sun the time of Here As T(n) = 0 (n2), f(n) = 108 M is not going Mlod3x = 0(n2) . Its bound is soirg master method applied number 0 (m2) subproblem

> 103x 100x

can be taken. MAXIMUM smoddocams