1. Input: Unsorted array of n distinct number A [a1, a2, an]

output: Index i where a; is the smallest number in A [91, 92, ... an]

Divide and conquer algorithm Divide: Divide the n-element array into two array A [a1, a2...anz] and A [a1, 12+1], ...an] where each of them has size n/2. Now we have two smaller sub problem from the original one.

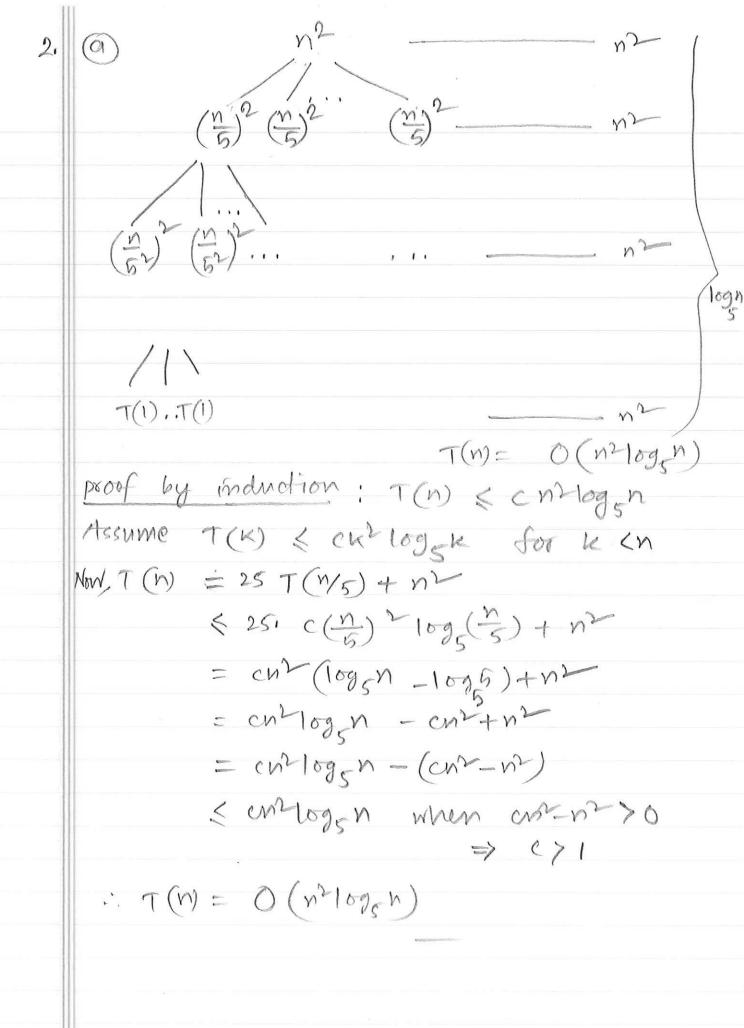
Conquer: solve the subproblems recursively. The base case will be the subproblem with size ! and index of that element will be returned

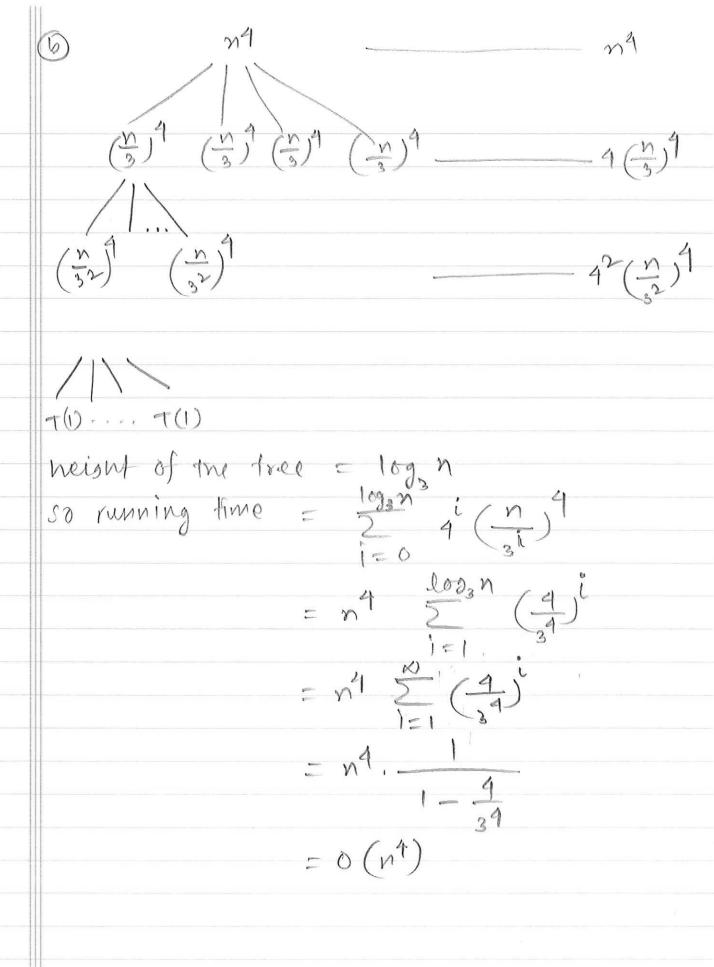
combine; From the two subproblem solved individually, we get the index 5, 2 52 of the smallest element of both. We then compare A[si] and A[si] and return the index of the smallest one.

Pseudo code

GetMin Index (A, i, i) if (1>,3) return i; else x = GetMinIndex (A, i, i+) y = Get Min Index (A, it +1, j) if (A[x] < A[y]) return x; return y; else

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Recurrence Relation
     T(n) = \begin{cases} 1, & \text{if } n = 1 \\ 2T(n/2) + 1, & \text{olverwise} \end{cases}
Proof by induction
Givess algorithm takes O() time
At first to prove T(n) = O(n)
T(n) < c(n-1) for some constant c 70
              and ny no for some no 70
Assume T(K) & C(K-1) for K<n
Now T(n) = 2 T (n/2) +1
        < 2 · (1/2-1)+1
      = cn - 2C + 1
       = e (n-1) - c+1
         = c(n-1)+(1-C)
         < c(n-1) for 1-C <0 → C>1
T(n) = O(n)
NOW to prove T(n) = 12(n)
T(n) you for some constant c>0
            and nyno for some no 70
Assume T(V) >, ex for Ken
NOW T(n) = 2 T (n/2) +1
        > 2. c. 1 +1
          = cn+1
          > cn
T(n) = Q(n) - (2)
from 1 L 2 T(n) = 0 (n)
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proof by induction T(n) = en4 for some constanc and ny no , no 70 Assume $T(k) \leq Ck^4$ for all k < nso $T(n) \leq 4c(\frac{N}{3})^4 + n^4$ = 4 cn9 + n9 = en4 + (n4 + 101 - cn4) = cn4+ (n4+ 4cn4-81 cn4) = en4 + (n9 = 77 cn9) = cn4 + n4 (1- 77 c) < cm if n1 (1- 37 () <0 => 1-770 <0 => 1 < 27 c => C> 81

1. T(n) = 0 (n4)