

Answer to question number 4:

Conversion:-

$$1\text{sec}=10^6\mu\text{s}$$

$$1\text{min}=6\times 10^7\mu\text{s}$$

$$1\text{hour}=3.6\times 10^9\mu\text{s}$$

$$1\text{day}=8.64\times 10^{10}\mu\text{s}$$

$$1\text{month}=2.592\times 10^{12}\mu\text{s}$$

$$1\text{year}=3.1557\times 10^{13}\mu\text{s}$$

$$1\text{centuary}=3.1557\times 10^{15}\mu\text{s}$$

Calculations for a second (and rest of the calculations for different time are similar) :

| | |
|----------------|--|
| n! | $N! \leq 10^6$, so by hit and trial $n \approx 9$ |
| log(n) | $\log_2(n) \leq 10^6 \rightarrow 2^{(\log_2(n))} \leq 2^{(10^6)} \rightarrow n \leq 2^{(10^6)} \rightarrow n \approx 10^{(3 \times (10^5))} \approx 10^{(300000)}$ because $2^{10} \approx 10^3$ |
| nlog(n) | fsolve(n*log[2](n) - 1000000 = 0); solved for n in Maple |
| n | $N \leq 10^6$, hence $n \approx 10^6$ |
| n ² | $N^2 \leq 10^6$, hence $n \approx 10^3$ |
| n ³ | $N^3 \leq 10^6$, hence $n \approx 10^2$ |
| 2 ⁿ | $2^n \leq 10^6 \rightarrow n \log_2(2) \leq 6 \log_2(10) \rightarrow n \leq 6 \log_2(10) \approx 19$ |
| sqrt(n) | $\sqrt{n} \leq 10^6 \rightarrow n \leq 10^{12} \rightarrow n \approx 10^{12}$ |

Result:-

| f(n) | 1sec | 1min | 1hour | 1day | 1month | 1year | 1centuary |
|----------------|-----------------------|---------------------------|----------------------|------------------------|-------------------------------------|-------------------------|---------------------------------------|
| log(n) | $\approx 10^{300000}$ | $\approx 10^{1080000000}$ | 2.36×10 | $2^{8.64 \times 10^8}$ | $\approx 10^{7.7 \times 10^{(11)}}$ | $2^{3.19 \times 10^9}$ | $\approx 10^{9.332 \times 10^{(14)}}$ |
| sqrt(n) | 10^{12} | 3.6×10^{15} | 1.2×10^{19} | 7.46×10^{21} | 6.71×10^{24} | 9.94×10^{26} | 9.945×10^{30} |
| n | 10^6 | 6×10^7 | 3.6×10^9 | 8.64×10^{10} | 2.592×10^{12s} | 3.1557×10^{13} | 3.1557×10^{15} |
| n ² | 1000 | 7745 | 60000 | 293938 | 1609968 | 5615692 | 56175382 |
| n ³ | 100 | 391 | 1532 | 4420 | 13736 | 31593 | 146677 |
| 2 ⁿ | 19 | 25 | 31 | 36 | 41 | 44 | 51 |
| n! | 9 | 11 | 12 | 13 | 15 | 16 | 17 |
| nlogn | 62746 | 2801418 | 133378059 | 2755147513 | 71870656400 | 7.9×10^{11} | 9.9×10^{30} |