

# Key Notes

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## Chapter-04

### Quadratic Equation

- **Quadratic Polynomial:** A polynomial of the form  $ax^2 + bx + c$  is called a quadratic expression in the variable  $x$ . This is a polynomial of the second degree. In quadratic expression  $ax^2 + bx + c$ ,  $a$  is the coefficient of  $x^2$ ,  $b$  is the coefficient of  $x$  and  $c$  is the constant term (or coefficient of  $x^0$ ).
- **Quadratic Equation:** An equation of the form  $ax^2 + bx + c = 0$ ,  $a \neq 0$ , is called a quadratic equation in one variable  $x$ , where  $a$ ,  $b$ ,  $c$  are constants.
- The equation  $x^2 + bx + c = 0$ ,  $a \neq 0$  is the standard form of a quadratic equation, where  $a$ ,  $b$  and  $c$  are real numbers.
- A real number  $\alpha$  is said to be a root of the quadratic equation  $x^2 + bx + c = 0$ ,  $a \neq 0$ . If  $a\alpha^2 + b\alpha + c = 0$ , the zeroes of quadratic polynomial  $x^2 + bx + c$  and the roots of the quadratic equation  $x^2 + bx + c = 0$  are the same.
- If we can factorise  $x^2 + bx + c = 0$ ,  $a \neq 0$  into product of two linear factors, then the roots of the quadratic equation can be found by equating each factors to zero.
- The roots of a quadratic equation  $x^2 + bx + c = 0$ ,  $a \neq 0$  are given by  $\frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$ , provided that  $b^2 - 4ac \geq 0$ .
- A quadratic equation  $x^2 + bx + c = 0$ ,  $a \neq 0$  has \_\_\_\_\_
  - (a) Two distinct and real roots, if  $b^2 - 4ac > 0$ .
  - (b) Two equal and real roots, if  $b^2 - 4ac = 0$ .
  - (c) Two roots are not real, if  $b^2 - 4ac < 0$ .
- A quadratic equation can also be solved by the method of completing the square.
  - (i)  $a^2 + 2ab + b^2 = (a + b)^2$
  - (ii)  $a^2 - 2ab + b^2 = (a - b)^2$
- Discriminant of the quadratic equation  $x^2 + bx + c = 0$ ,  $a \neq 0$  is given by  $D = b^2 - 4ac$ .