

ELEC 341 – Graded Assignments

# Assignment A2

## 2<sup>nd</sup> Order Approximations

### 10 Marks

#### Learning Objectives

Modeling Black Box Systems

2<sup>nd</sup> Order Performance Metrics

Natural Frequency

Damping Co-efficient

2<sup>nd</sup> Order Approximations

Matlab

zpk()

a2DSPlot()

When you use off-the-shelf (OTS) sub-components, you only have the information available in the data-sheet about what's inside. This is called a "Black Box" system.

Data sheets often contain experimental curves, but rarely provide a linear model. To use the device in a control system, you must develop one of your own. The best you can do is a linear approximation which will never be perfect, but it's better than nothing. And if you do a good job, it's **a lot** better than nothing.

**Q1      2 mark(s)   Experimental Data from a Data-Sheet**

Use **a2DSPlot.p** to plot an experimental curve from a data-sheet.

Estimate Rise Time (Tr), Modified Rise Time (Tr1), Time Constant (Tau), Peak Time (Tp), Settle Time (Ts), and Percent Overshoot (Pos).

- Q1.Tr      (ms)      Scalar
- Q1.Tr1    (ms)      Scalar
- Q1.Tau    (ms)      Scalar
- Q1.Tp    (ms)      Scalar
- Q1.Ts    (ms)      Scalar
- Q1.Pos    (%)      Scalar

The data has noise, which doesn't make your task particularly easy, but it's experimental data and that's what experimental data looks like.

Answer this question carefully. The whole assignment depends on these values.

**Q2      1 mark(s)   Damping Co-efficient**

Compute the damping co-efficient  $\zeta$ .

- Q2.zeta    (pure)      Scalar

**Q3      1 mark(s)   Approximate #1**

Use **Rise Time** to compute natural frequency  $\omega_n$ .

Use  $\zeta$  and  $\omega_n$  to compute a 2<sup>nd</sup> Order Approximation transfer function G.

- Q3. $\omega_n$     (rad/s)      Scalar
- Q3.G      (V/V)      LTI

**Q4      1 mark(s)   Approximate #2**

Use **Peak Time** to re-compute natural frequency  $\omega_n$ .

Use  $\zeta$  and  $\omega_n$  to compute a 2<sup>nd</sup> Order Approximation transfer function G.

- Q4. $\omega_n$     (rad/s)      Scalar
- Q4.G      (V/V)      LTI

**Q5      1 mark(s)   Approximate #3**

Use **Settle Time** to re-compute natural frequency  $\omega_n$ .

Use  $\zeta$  and  $\omega_n$  to compute a 2<sup>nd</sup> Order Approximation transfer function G.

- Q5. $\omega_n$     (rad/s)      Scalar
- Q5.G      (V/V)      LTI

**Q6 1 mark(s) Approximate #4**

Use both **Rise Time** and **Peak Time** to compute natural frequency  $\omega_n$ .

Use the mean of the two natural frequencies you already calculated.

Use  $\zeta$  and  $\omega_n$  to compute a 2<sup>nd</sup> Order Approximation transfer function G.

- Q6. $\omega_n$  (rad/s) Scalar
- Q6.G (V/V) LTI

**Q7 1 mark(s) Approximate #5**

Use both **Rise Time** and **Settle Time** to compute natural frequency  $\omega_n$ .

Use the mean of the two natural frequencies you already calculated.

Use  $\zeta$  and  $\omega_n$  to compute a 2<sup>nd</sup> Order Approximation transfer function G.

- Q7. $\omega_n$  (rad/s) Scalar
- Q7.G (V/V) LTI

**COW:** Plot the step response of each transfer function.

Are the target metrics of each approximation **identical** to the source function ???

Do any of them reach 98% of FV at  $4\tau$  ???

Plot all approximations on the same figure. If you were developing an approximation of a real system, you would choose the most appropriate one, based on your particular RCGs.

**Q8 1 mark(s) Approximate #6**

Compute the damping co-efficient  $\zeta$  and natural frequency  $\omega_n$  of a 2<sup>nd</sup> Order Approximation that has the same **Peak Time** and **DC Gain** as Q3, but **1/2 the Overshoot**.

- Q8. $\zeta$  (pure) Scalar
- Q8. $\omega_n$  (rad/s) Scalar
- Q8.G (V/V) LTI

**Q9 1 mark(s) Approximate #7**

Use the time constant **Tau  $\tau$**  to compute a 2<sup>nd</sup> Order Approximation transfer function that is **Critically Damped**.

- Q9. $\omega_n$  (rad/s) Scalar
- Q9.G (V/V)

**COW:** Plot the step response of each transfer function.

Do your approximations satisfy all requirements ???