Stanford University ACM Team Notebook (2013-14)

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1

```
// Adjacency list implementation of Dinic's blocking flow algorithm. 
// This is very fast in practice, and only loses to push-relabel flow.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        - To obtain the actual flow values, look at all edges with
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      capacity > 0 (zero capacity edges are residual edges).
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             void AddEdge(int from, int to, int cap) {
    G[from].push.back(Edge(from, to, cap, 0, G[to].size()));
    if ([from == to) G[from].back().index++;
    G[to].push.back(Edge(to, from, 0, 0, G[from].size() - 1));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  struct Edge {
  int from, co, cap, flow, index;
  Edge(int from, int to, int cap, int flow, int index) :
  from(from), to(to), cap(cap), flow(flow), index(index) {}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               long long BlockingFlow(int s, int t) {
fill(dad.begin(), dad.end(), (Edge *) NULL);
dad[s] = &G[0][0] - 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               \label{eq:definition} \mbox{Dinic(int N) : N(N), G(N), dad(N), Q(N) } \big\{ \big\}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        graph, constructed using AddEdge()source
  Longest increasing subsequence (C++)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             - maximum flow value
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       const int INF = 2000000000;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        vector<vector<Edge> > G;
vector<Edge *> dad;
vector<int> Q;
                                                                                                                         Knuth-Morris-Pratt (C++)
                                                              Regular expressions (Java)
                                                                                                                                                                                                                                                            Dinic.cc 1/31
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   using namespace std;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       #include <iostream>
#include <queue>
                                                                                                                                                                                                                                                                                                                                                                                                                                                         O( |V |^2 |E|)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  #include <vector>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         #include <cmath>
                                                                                                                                                               Emacs settings
                                                                                                                                                                                                                                                                                                                                                                                                                                 // Running time:
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          struct Dinic {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 - sink
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    // OUTPUT:
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               INPUT:
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  int N;
26.
27.
28.
29.
30.
```

- To obtain the actual flow, look at positive values only.

MinCostMaxFlow.cc 2/31

```
// Implementation of min cost max flow algorithm using adjacency // matrix (Edmonds and Karp 1972). This implementation keeps track of forward and reverse edges separately (so you can set cap[i][i]] = // cap[i][i]). For a regular max flow, set all edge costs to 0. // Running time, O(|V|^{\lambda}2) cost per augmentation max flow: O(|V|^{\lambda}3) augmentations // min cost max flow: O(|V|^{\lambda}3) augmentations // min cost max flow: O(|V|^{\lambda}4* MAX\_EDGE\_COST) augmentations // rostructed using AddEdge() - source // - source // - sink // OUTPUT: - control flow value, minimum cost value)
```

```
int best = -1;
found[s] = true;
found[s] = true;
if (found[k]) continue;
Relax(s, k, cap[s][k] - flow[s][k], cost[s][k], 1);
if (best = -1 || dist[k] < dist[best]) best = k;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                N(N), \; \operatorname{cap}(N, \operatorname{VL}(N)), \; \operatorname{flow}(N, \operatorname{VL}(N)), \; \operatorname{cost}(N, \operatorname{VL}(N)), \; \operatorname{found}(N), \; \operatorname{dist}(N), \; \operatorname{pi}(N), \; \operatorname{width}(N), \; \operatorname{dad}(N) \; \big\{ \big\}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          void Relax(int s, int k, L cap, L cost, int dir) {
   L val = dist(s] + pi(s] - pi(k] + cost;
   L f (cap & val < dist(k)) {
        dist(k) = val;
        dist(k) = val;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   void AddEdge(int from, int to, L cap, L cost) {
    this->cap[from][to] = cap;
    this->cost[from][to] = cost;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               fill(found.begin(), found.end(), false);
fill(dist.begin(), dist.end(), INF);
fill(width.begin(), width.end(), 0);
                                                                                                                                                                                                                                                                                                                                                                                                                        const L INF = numeric_limits<L>::max() / 4;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     dad[k] = make_pair(s, dir);
width[k] = min(cap, width[s]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     for (int k = 0; k < N; k++)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     L Dijkstra(int s, int t) {
                                                                                                                                                                                                                                                                                                 typedef vector<VL> VVL;
typedef pair<int, int> PII;
typedef vector<PII> VPII;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   MinCostMaxFlow(int N) :
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     struct MinCostMaxFlow {
                                                                                                                                                                                                             typedef vector <VI> VVI;
                                                                                                                                                                             typedef vector<int> VI;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            VVL cap, flow, cost;
VI found;
                                                                                                                                                                                                                                          typedef long long L;
typedef vector<L> VL;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   while (s != -1) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            VL dist, pi, width;
                                                                                                                      using namespace std;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         width[s] = INF;
                                                             #include <iostream>
                                <vector>
#include <cmath>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               dist[s] = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 s = best;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            VPII dad;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        int N;
                                #include
```

3

```
pi[k] = min(pi[k] + dist[k], INF);

return width[t];

DaixeL, L> GetMaxFlow(int s, int t) {
   Lotflow = 0, totcost = 0;
   while (L amt = Dijkstra(s, t)) {
    tofflow += amt;
        for (int s = 1; x != s; x = dad[x].first) {
        if (ad[x].second == 1) {
            for (cost += amt * cost[dad[x].first][x];
            totcost += amt * cost[dad[x].first][x];
            flow[x][dad[x].first] -= amt;
            totcost -= amt * cost[x][dad[x].first];
        }
}

return make_pair(totflow, totcost);
};
```

PushRelabel.cc 3/31

```
// Adjacency list implementation of FIFO push relabel maximum flow
                             // with the gap relabeling heuristic. This implementation is // significantly faster than straight Ford-Fulkerson. It solves // random problems with 10000 vertices and 1000000 edges in a few
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        - To obtain the actual flow values, look at all edges with
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             capacity > 0 (zero capacity edges are residual edges).
                                                                                                                                     // seconds, though it is possible to construct test cases that
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          struct Edge {
  int from, to, cap, flow, index;
  Edge(int from, int to, int cap, int flow, int index) :
  from(from), to(to), cap(cap), flow(flow), index(index) {}
                                                                                                                                                                                                                                                                                                                                                                           - graph, constructed using AddEdge()
                                                                                                                                                            // achieve the worst-case. // Running time: // O(|V|^{\wedge 3})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          - maximum flow value
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              typedef long long LL;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         using namespace std;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    #include <vector>
#include <iostream>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            #include <cmath>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          #include <queue>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            OUTPUT:
                                                                                                                                                                                                                                                                                                                                      // INPUT:
```

```
\texttt{PushRelabel(int N) : N(N), G(N), excess(N), dist(N), active(N), count(2*N) } \left. \{ \right. \}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          for (int i = 0; excess[v] > 0 && i < G[v].size(); i++) Push(G[v][i]); if (excess[v] > 0) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                         void Enqueue(int v) {
   if (!active[v] && excess[v] > 0) { active[v] = true; Q.push(v); }
                                                                                                                                                                                                                                                                                void AddEdge(int from, int to, int cap) {
    Glfroml.yush.back(Edge(from. to, cap. 0, Glto].size()));
    if (from == to) Glfroml.back().index++;
    Glto].push_back(Edge(to, from, 0, 0, Glfrom].size() - 1));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    int amt = int(min(excess[e.from], LL(e.cap - e.flow)));
if (dist[e.from] <= dist[e.to] || amt == 0) return;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        for (int i = 0; i < G[v].size(); i++)
if (G[v][i].cap - G[v][i].flow > 0)
dist[v] = min(dist[v], dist[G[v][i].to] + 1);
count[dist[v]]++;
                                                                                       vector<LL> excess;
vector<int> dist, active, count;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       dist[v] = max(dist[v], N+1);
count[dist[v]]++;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         for (int v = 0; v < N; v++) {
  if (dist[v] < k) continue;
  count[dist[v]]--;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  G[e.to][e.index].flow -= amt;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           LL GetMaxFlow(int s, int t) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                if (count[dist[v]] == 1)
                                                            vector<vector<Edge> > G;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              excess[e.from] -= amt;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         void Discharge(int v) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       excess[e.to] += amt;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                void Relabel(int v) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     void Push(Edge &e) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               \label{eq:count_dist_v} \begin{split} \operatorname{count}[\operatorname{dist}[v]] --; \\ \operatorname{dist}[v] &= 2*N; \end{split}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     Gap(dist[v]);
struct PushRelabel {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         count[0] = N-1;
count[N] = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              void Gap(int k) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  Relabel(v);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                Enqueue (e.to);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       e.flow += amt;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           Enqueue (v);
                                                                                                                                                              queue<int> 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              Enqueue(v);
```

4

```
Lmate[i] = j;
                                                                                                                                                                                                                                                                                                 Rmate[j] = i;
                                                                                                                                        Lmate = VI(n, -1);
Rmate = VI(n, -1);
                                                                                                                                                                                                                                                                                                                      mated++;
                                                                                                                                                                                                                                                                        LL totflow = 0; for (int i = 0; i < G[s].size(); i++) totflow += G[s][i].flow;
dist[s] = N;
active[s] = active[t] = true;
for (int i = 0; i < G[s].size(); i++) {
    excess[s] += G[s][i].cap;
    Push(G[s][i]);</pre>
                                                                                                                                    while (!Q.empty()) {
   int v = Q.front();
                                                                                                                                                                                        active[v] = false;
Discharge(v);
                                                                                                                                                                                                                                                                                                                return totflow;
                                                                                                                                                                               Q.pop();
```

MinCostMatching.cc 4/31

```
// The values in cost[i][j] may be positive or negative. To perform // maximization, simply negate the cost[][] matrix.
                                                                                                             // algorithm for finding min cost perfect matchings in dense // graphs. In practice, it solves 1000x1000 problems in around 1 \,
                                                                             // This is an O(n^3) implementation of a shortest augmenting path
                                                                                                                                                                                                                                                                    cost[i][j] = cost for pairing left node i with right node j
Lmate[i] = index of right node that left node i pairs with
Rmate[j] = index of left node that right node j pairs with
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              double MinCostMatching(const VVD &cost, VI &Lmate, VI &Rmate) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  for (int j = 1; j < n; j++) u[i] = min(u[i], cost[i][j]);
// Min cost bipartite matching via shortest augmenting paths
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               // construct dual feasible solution \ensuremath{\mathsf{VD}}\xspace \ensuremath{\mathsf{u}}(n)\,;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    for (int i = 0; i < n; i++) {
  u[i] = cost[i][0];</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     int n = int(cost.size());
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 typedef vector<double> VD;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        typedef vector<int> VI;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    typedef vector<VD> VVD;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            #include <algorithm>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               using namespace std;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           #include <cstdio>
#include <cmath>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     #include <vector>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     VD v(n);
```

```
for (int j = 0; j < n; j++) {
    v[j] = cost[0][j] - u[0];
    for (int i = 1; i < n; i++) v[j] = min(v[j], cost[i][j] - u[i]);</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 const double new_dist = dist[j] + cost[i][k] - u[i] - v[k];
if (dist[k] > new_dist) {
    dist[k] = new_dist)
                                                                                                                                                    // construct primal solution satisfying complementary slackness
                                                                                                                                                                                                                         int mated = 0;
for (int i = 0; i < n; i++) {
    for (int j = 0; j < n; j++) {
    if (Rmate[3] i = -1) continue;
    if (fabs(cost[i][j] - u[i] - v[j]) < le-l0) {</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           if (seen[k]) continue;
if (j == -1 || dist[k] < dist[j]) j = k;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         // repeat until primal solution is feasible while (mated < n) \{
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  // initialize Dijkstra
fill(dad.begin(), dad.end(), -1);
fill(seen.begin(), seen.end(), 0);
for (int k = 0; k < n; k++)
dist(k] = cost[s][k] - u[s] - v[k];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              j = -1;
for (int k = 0; k < n; k++) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          const int i = Rmate[j];
for (int k = 0; k < n; k++) {</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      // find an unmatched left node
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               if (Rmate[j] == -1) break;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                int s = 0;
while (Lmate[s] != -1) s++;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               if (seen[k]) continue;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          // termination condition
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    // relax neighbors
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      // find closest
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           dad[k] = j;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 while (true) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        seen[j] = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            int j = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 VI dad(n);
VI seen(n);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         VD dist(n);
```

MaxBipartiteMatching.cc 5/31

```
// This code performs maximum bipartite matching.

// Running time: O(|E| |V|) -- often much faster in practice

// INPUT: w[i][] = dege between row node i and column node j

// OUTPUT: w[i]] = assignment for row node i, -1 if unassigned

// mc[i] = assignment for column node j, -1 if unassigned

#include <vector>
using namespace std;

typedef vector<int> VI;

typedef vector<int> VI;

typedef vector<int> VI;

typedef vector<int> VI;

typedef vector<int i, const VVI &w, VI &mr, VI &mc, VI &seen) {
    for (int j = 0; j < w[i].size(); j++) {
        if (w[i]) && !seen[j]) {
            mr[i] = j;
            mr[i] = j;
```

```
return false;
}
int BipartiteMatching(const VVI &w, VI &mc, VI &mc) {
    mr = VI(w.size(), -1);
    int ct = 0;
    for (int i = 0; i < w.size(); i++) {
        VI &sen w(0).size();
        if (FindMatch(i, w, mr, mc, seen)) ct++;
}
return ct;
}</pre>
```

MinCut.cc 6/31

```
for (int j = 0; j < N; j++) weights[prev][j] += weights[last][j];
for (int j = 0; j < N; j++) weights[j][prev] = weights[prev][j];
used[last] = true;</pre>
// Adjacency matrix implementation of Stoer-Wagner min cut algorithm.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               for (int j = 1; j < N; j++)
if (!added[j] && (last == -1 || w[j] > w[last])) last = j;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             cut.push_back(last);
if (best_weight == -1 || w[last] < best_weight) {
   best_cut = cut;</pre>
                                                                                                                                                                                                                                                                     - (min cut value, nodes in half of min cut)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     for (int phase = N-1; phase >= 0; phase--) {
   VI w = weights[0];
   VI added = used;
   int prev, last = 0;
   for (int i = 0; i < phase; i++) {
     prev = last;</pre>
                                                                                                                                                                               - graph, constructed using AddEdge()
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     pair<int, VI> GetMinCut(VVI &weights) {
  int N = weights.aize();
  VI used(N), cut, best_cut;
  int best_weight = -1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  const int INF = 100000000;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           if (i == phase-1) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               typedef vector<int> VI;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            typedef vector<VI> VVI;
                                                                                                                                                                                                                                                                                                                                                                                                                                            using namespace std;
                                                                                                                                                                                                                                                                                                                                                         #include <vector>
#include <iostream>
                                                           // Running time:
                                                                                                                                                                                                                                                                                                                                 #include <cmath>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       last = -1;
                                                                                         0(10/23)
                                                                                                                                                                                                                                           // OUTPUT:
                                                                                                                                                 INPUT:
```

```
best_weight = w(last);
} else {
    for (int j = 0; j < N; j++)
        w(j) += weights:last][j];
    added[last] = true;
}
}return make_pair(best_weight, best_out);
}</pre>
```

ConvexHull.cc 7/31

```
bool between(const PT &a, const PT &b, const PT &c) {  return \ (fabs(area2(a,b,c)) < EPS & & (a.x-b.x)*(c.x-b.x) <= 0 & & (a.y-b.y)*(c.y-b.y) <= 0); 
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              PT(T x, T y) : x(x), y(y) {} bool operator<(const PT &rhs) const { return make_pair(y,x) < make_pair(rhs.y,rhs.x); } bool operator==(const PT &rhs) const { return make_pair(y,x) == make_pair(rhs.y,rhs.x); }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           while (up.size() > 1 && area2(up[up.size()-2], up.back(), pts[i]) >= 0) up.pop_back();
                                                                                                                                                                                                                                                  INPUT: a vector of input points, unordered.
OUTPUT: a vector of points in the convex hull, counterclockwise, starting
with bottommost/leftmost point
// Compute the 2D convex hull of a set of points using the monotone chain // algorithm. Eliminate redundant points from the hull if REMOVE_REDUNDANT is
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  T cross(PT p, PT q) { return p.x*q.y-p.y*q.x; } T area2(PT a, PT b, PT c) { return cross(a,b) + cross(b,c) + cross(c,a); }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   void ConvexHull(vector<PT> &pts) {
    sort(pts.begin(), pts.end());
    pts.erase(unique(pts.begin(), pts.end());
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              vector<PT> up, dn;
for (int i = 0; i < pts.size(); i++) {</pre>
                                                                                                                                                                     // Running time: O(n log n)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  #define REMOVE_REDUNDANT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   #include <algorithm>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          using namespace std;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               typedef double T;
const T EPS = 1e-7;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                  #include <cassert>
#include <vector>
                                                                                                                                                                                                                                                                                                                                                                                                                                #include <cstdio>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         #include <cmath>
                                                                                     #defined.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    struct PT {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 PT()
```

Geometry.cc 8/31

```
#include ciostream>
#include costream>
#include cos
```

6

```
b = b-a;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  // determine if lines from a to b and c to d are parallel or collinear bool LinesParallel(PT a, PT b, PT c, PT d) \{
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         if (LinesCollinear(a, b, c, d)) {
   if (dist2(a, c) < EPS | | dist2(a, d) < EPS | |
    dist2(b, c) < EPS | | dist2(b, d) < EPS) return true;
   if (dot(c-a, c-b) > 0 && dot(d-a, d-b) > 0 && dot(c-b, d-b) > 0)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             double DistancePointFlane(double x, double y, double z, double c, double c, double d)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        compute distance between point (x,y,z) and plane ax+by+cz=d
PT RotateCCW(PT p, double t) {
    return PT(p.x*cos(t)-p.y*sin(t), p.x*sin(t)+p.y*cos(t));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        if (cross(d-a, b-a) * cross(c-a, b-a) > 0) return false;
if (cross(a-c, d-c) * cross(b-c, d-c) > 0) return false;
return true;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                with line passing through c and d, assuming that unique
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              intersection exists; for segment intersection, check if
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         // determine if line segment from a to b intersects with
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       compute intersection of line passing through a and b
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            // compute distance from c to segment between a and b
double DistancePointSegment(PT a, PT b, PT c) {
   return sqrt(dist2(c, ProjectPointSegment(a, b, c)));
                                                                                                                                                                                                                                                                                                                                                                                                  // project point c onto line segment through a and
PT ProjectPointSegment(PT a, PT b, PT c) {
   double r = dot(b-a,b-a);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        bool SegmentsIntersect(PT a, PT b, PT c, PT d) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 return fabs(a*x+b*y+c*z-d)/sqrt(a*a+b*b+c*c);
                                                                                                                                                                                                                                                                              return a + (b-a)*dot(c-a, b-a)/dot(b-a, b-a);
                                                                                                                                                             // project point c onto line through a and .// assuming a l=b
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 bool LinesCollinear(PT a, PT b, PT c, PT return LinesParallel(a, b, c, d)
                                                                                                                                                                                                       // assuming a != b
PT ProjectPointLine(PT a, PT b, PT c) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                return fabs(cross(b-a, c-d)) < EPS;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           && fabs(cross(a-b, a-c)) < EPS && fabs(cross(c-d, c-a)) < EPS;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          if (fabs(r) < EPS) return a;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               line segment from c to d
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               // segments intersect first
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       r = dot(c-a, b-a)/r;
if (r < 0) return a;
if (r > 1) return b;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            return a + (b-a)*r;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            return false;
```

```
return ComputeLineIntersection(b, b+RotateCW90(a-b), c, c+RotateCW90(a-c));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           if ((p[i].y <= q.y && q.y < p[i].y ||
p[i].y <= q.y && q.y < p[i].y) &&
q.x < p[i].x + (p[i].x + (p[i].x - p[i].x) * (q.y - p[i].y) / (p[i].y - p[i].y))
c = !o;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      // determine if point is on the boundary of a polygon
book pointonpolygon(const vectorPr &p, PT q) {
    for (int i = 0 i i < p.size(); i++)
    if (dist2(ProjectPointSegment(p[i], p[(i+1)%p.size()], q), q) < BPS)
    if (dist2(ProjectPointSegment(p[i], p[(i+1)%p.size()], q), q) < BPS)</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             // Note that it is possible to convert this into an *exact* test using
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    (making sure to deal with signs properly) and then by writing exact
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            // with circle centered at b with radius R vector<PT> CircleCircleIntersection(PT a, PT b, double r, double R) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               // determine if point is in a possibly non-convex polygon (by William
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          Randolph Franklin); returns 1 for strictly interior points, 0 for strictly exterior points, and 0 or 1 for the remaining points.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 // integer arithmetic by taking care of the division appropriately
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        // circle centered at c with radius r > 0 vector<PT> CircleLineIntersection(PT a, PT b, PT c, double r)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             // compute intersection of circle centered at a with radius r
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             // compute intersection of line through points a and b with
ComputeLineIntersection(PT a, PT b, PT c, PT d) {
b=b-a; d=c-d; c=c-a;
assert(dot(b, b) > EPS && dot(d, d) > EPS);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       bool PointInPolygon(const vector<PT> &p, PT q) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    tests for checking point on polygon boundary
                                                                                                                                                                                                                                                            // compute center of circle given three points
                                                                                                                                                                                                                                                                                               PT ComputeCircleCenter(PT a, PT b, PT c) { b=(a+b)/2;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         ret.push_back(c+a+b*(-B+sqrt(D+EPS))/A);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        ret.push_back(c+a+b*(-B-sqrt(D))/A);
                                                                                                                                  return a + b*cross(c, d)/cross(b, d);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     for (int i = 0; i < p.size(); i++){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          double d = sqrt(dist2(a, b));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          a = a-c;
double A = dot(b, b);
double B = dot(a, b);
double C = dot(a, a) - r*r;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 int j = (i+1)%p.size();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              if (D < -EPS) return ret;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      double D = B*B - A*C;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           vector<PT> ret;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           vector<PT> ret;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       return false,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     if (D > EPS)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       bool c = 0;
                                                                                                                                                                                                                                                                                                                                                                                  c=(a+c)/2;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     return c;
```

```
<< SegmentsIntersect(PT(0,0), PT(2,4), PT(3,1), PT(-1,3)) << " "
<< SegmentsIntersect(PT(0,0), PT(2,4), PT(4,3), PT(0,5)) << " "
<< SegmentsIntersect(PT(0,0), PT(2,4), PT(2,-1), PT(-2,1)) < " " "
<< SegmentsIntersect(PT(0,0), PT(2,4), PT(5,5), PT(1,7)) << endl;
<< SegmentsIntersect(PT(0,0), PT(2,4), PT(5,5), PT(1,7)) << endl;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                    cerr << ProjectPointLine(PT(-5,-2), PT(10,4), PT(3,7)) << endl;
                                                                                                                                                                                                                                      cerr << DistancePointFlane(4,-4,3,2,-2,5,-8) << endl;
                                                               // expected: (5,2) (7.5,3) (2.5,1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     // expected: 1 1 1 0 0 cerr << PointInPolygon(v,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        (5,4) (4,5)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           (4,5) (5,4)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          blank line
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    blank line
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    v.push_back(PT(0,0));
v.push_back(PT(5,0));
v.push_back(PT(5,5));
v.push_back(PT(0,5));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             // expected: 1 1 1 0
                                                                                                                                                                                                        expected: 6.78903
                                                                                                                                                                                                                                                                                                   // expected: 1 0 1
                                                                                                                                                                                                                                                                                                                                                                                                                                               // expected: 0 0 1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    // expected: (1,2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         // expected: (1,1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              vector<PT> v;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                expected:
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            cerr
                                                                                                                                                                                                                                                                                          // This code computes the area or centroid of a (possibly nonconvex) // polygon, assuming that the coordinates are listed in a clockwise or // counterclockwise fashion. Note that the centroid is often known as
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 or CCW order) is simple
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         for (int i = 0; i < p.size(); i++){
  int j = (i+1) % p.size();
  c = c + (p[i]+p[j])*(p[i].x*p[j].y - p[j].x*p[i].y);</pre>
if (d > r+R | | d+min(r, R) < max(r, R)) return ret;
double x = (d*d-R*R+r*r)/(2*d);
double y = sqrt(r*r-r*x);</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        for (int i = 0; i < p.size(); i++) {
  for (int k = i+1; k < p.size(); k++) {
   int j = (i+1) % p.size();
  int l = (k+1) % p.size();
  if (i = 1 | | | j == k) continue;
  if (SegmentsIntersect(p[i], p[i], p[i])))</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                double ComputeSignedArea(const vector<PT> &p) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 // tests whether or not a given polygon (in CW bool IsSimple(const vector<PT> &p) \{
                                                                                                                                                                                                                                                                                                                                                                                        // the "center of gravity" or "center of mass"
                                                                                                                                                                          ret.push_back(a+v*x - RotateCCW90(v)*y);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                double scale = 6.0 * ComputeSignedArea(p);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           cerr << RotateCCW(PT(2,5),M_PI/2) << endl;</pre>
                                                                                                                   ret.push_back(a+v*x + RotateCCW90(v)*y);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 area += p[i].x*p[j].y - p[j].x*p[i].y;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          ComputeCentroid(const vector<PT> &p) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               double ComputeArea (const vector<PT> &p)
                                                                                                                                                                                                                                                                                                                                                                                                                                            double area = 0;
for(int i = 0; i < p.size(); i++) {</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     return fabs(ComputeSignedArea(p));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              cerr << RotateCCW90(PT(2,5)) <<
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     int j = (i+1) % p.size();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      cerr << RotateCW90(PT(2,5))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  return false;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       expected: (5,-2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               // expected: (-5,2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       return area / 2.0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    // expected: (5,2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            return c / scale;
                                                                                     PT v = (b-a)/d;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       return true;
                                                                                                                                              if (y > 0)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         int main() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     PT c(0,0);
```

```
cerr << ComputeLineIntersection(PT(0,0), PT(2,4), PT(3,1), PT(-1,3)) << endl;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   vectorvectorvectorvertorvertorvertorvertorvertorvertorvertorvertorvertorvertorvertorvertorvertorvertorvertorvertorvertorvertorvertorvertorvertorvertorvertorvertorvertorvertorvertorvertorvertorvertorvertorvertorvertor
                                                                                             cerr << ComputeCircleCenter(PT(-3,4), PT(6,1), PT(4,5)) << endl;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          endl;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    << pointInPolygon(v, PT(2,2)) << " "
<< pointInPolygon(v, PT(2,0)) << " "
<< pointInPolygon(v, PT(0,2)) << " "
<< pointInPolygon(v, PT(0,2)) << " "
<< pointInPolygon(v, PT(5,2)) << " "
<< pointInPolygon(v, PT(5,2)) << " "</pre>
```

9

```
u = CircleCircleIntersection(PT(1,1), PT(10,10), 5, 5);
for (int i = 0; i = u.size(); i++) cerr < u[i] << " "; cerr << endl;
u = CircleCircleIntersection(PT(1,1), PT(8,8), 5, 5);
for (int i = 0; i < u.size(); i++) cerr << u[i] << " "; cerr << endl;
u = CircleCircleIntersection(PT(1,1), PT(4,5,4,5), 10, sgrt(2.0),2.0);
for (int i = 0; i < u.size(); i++) cerr << u[i] << " "; cerr << endl;
u = CircleCircleIntersection(PT(1,1), PT(4,5,4,5), 10, sgrt(2.0),2.0);
for (int i = 0; i < u.size(); i++) cerr << u[i] << " "; cerr << endl;
// area should be 5.0

// centroid should be (1.1666666, 1.166666)
PT pall = {PT(0,0), PT(5,0), PT(1,1), PT(0,5)};
vcctor_PT> p[pa, pa+4);
PT c = ComputeCentroid(p);
cerr << "Area: " << ComputeArea(p) << endl;
return 0;
}</pre>
```

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```
String[] arr = s.trim().split("\\s+");
double[] ret = new double[arr.length];
for (int i = 0; i < arr.length; i++) ret[i] = Double.parseDouble(arr[i]);</pre>
                                                                                                                                                                                                                                                            (1) whether B - A is a single closed shape (as opposed to multiple shapes) (2) the area of B - A
                             containing an even number of doubles, separated by commas. The first two lines represent the coordinates of two polygons, given in counterclockwise (or clockwise) order, which we will call "A" and "B". The last line
// In this example, we read an input file containing three lines, each
                                                                                                                                                                                                                                                                                                                                   (3) whether each p[i] is in the interior of B - A
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         // make an array of doubles from a string
                                                                                                                                             contains a list of points, p[1], p[2], ...
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  static double[] readPoints(String s) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      Point does not belong to the area.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     Point belongs to the area.
                                                                                                                                                                                                                       Our goal is to determine:
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   public class JavaGeometry {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       The area is singular.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              import java.awt.geom.*;
import java.io.*;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               The area is 25.0
                                                                                                                                                                                                                                                                                                                                                                                                                                       0 0 10 0 0 10
0 0 10 10 10 0
8 6
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             import java.util.*;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    return ret;
```

```
static double computePolygonArea(ArrayList*Point2D.Double> points) {
   Point2D.Double[] pts = points.toArray(new Point2D.Double[points.size()]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                // compute the area of an Area object containing several disjoint polygons static double computeArea(Area area) \{
                                                                                                                                          for (int i = 2; i < pts.length; i += 2) p.lineTo(pts[i], pts[i+1]);
p.closePath();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      ArrayList<Point2D.Double> points = new ArrayList<Point2D.Double>();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       points.add(new Point2D.Double(buffer[0], buffer[1]));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              // notice that the main() throws an Exception -- necessary to // avoid wrapping the Scanner object for file reading in a
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     area += pts[i].x * pts[j].y - pts[j].x * pts[i].y;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             Scanner scanner = new Scanner(new File("input.txt"));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    public static void main(String args[]) throws Exception {
// make an Area object from the coordinates of a polygon static Area makeArea(double[] pts) \{
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        double[] pointsA = readPoints(scanner.nextLine());
double[] pointsB = readPoints(scanner.nextLine());
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      PathIterator iter = area.getPathIterator(null);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               Scanner scanner = new Scanner (System.in);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 totArea += computePolygonArea(points);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        double[] buffer = new double[6];
switch (iter.currentSegment(buffer)) {
                                                                             Path2D.Double p = new Path2D.Double();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    for (int i = 0; i < pts.length; i++){
  int j = (i+1) % pts.length;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      case PathIterator.SEG_MOVETO:
case PathIterator.SEG_LINETO:
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        case PathIterator.SEG_CLOSE:
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     Area areaA = makeArea(pointsA);
Area areaB = makeArea(pointsB);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             areaB.intersect (areaA);
                                                                                                                          p.moveTo(pts[0], pts[1]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    while (!iter.isDone()) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              return Math.abs(area)/2;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     points.clear();
                                                                                                                                                                                                                                                                                                                                                     // compute area of polygon
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            catch block.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   areaB.subtract(areaA);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         double totArea = 0;
                                                                                                                                                                                                                                       return new Area(p);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                       double area = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       iter.next();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                return totArea;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  break;
```

```
Rectangle2D.Double rect = new Rectangle2D.Double (double x, double y, double w, double h);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            Each of these can be embedded in an Area object (e.g., new Area (rect)).
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         Ellipse2D.Double ellipse = new Ellipse2D.Double (double x, double y),
double w, double h);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   creates an ellipse inscribed in box with bottom-left corner (x,y)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         System.out.println ("Point does not belong to the area.");
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              creates a box with bottom-left corner (x,y) and upper-right corner (x+y,w+h)
                                                                                                                                                                                                                                                                                                                                                                                                                                  // (2) compute the area of B - A System.out.println("The area is " + computeArea(areaB) + ".");
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    // (3) determine whether each p[i] is in the interior of B - A
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                // Finally, some useful things we didn't use in this example:
// (1) determine whether B - A is a single closed shape (as ^{\prime\prime} opposed to multiple shapes)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       if (areaB.contains(x,y)) \{ System.out.println ("Point belongs to the area.");
                                                                                                                                                                                                                                                                                                                                                             System.out.println("The area is not singular.");
                                                                                                                                                                                                                                                                                System.out.println("The area is singular.");
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           and upper-right corner (x+y,w+h)
                                                                                 boolean isSingle = areaB.isSingular();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        while (scanner.hasNextDouble()) {
  double x = scanner.nextDouble();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          assert(scanner.hasNextDouble());
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  double y = scanner.nextDouble();
                                                                                                                                                              areaB.isEmpty();
                                                                                                                                                                                                                                           if (isSingle)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 } else {
                                                                                                                                                                                                                                                                                                                        else
```

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```
double u = ((px-x1)*(x2-x1) + (py-y1)*(y2-y1) + (pz-z1)*(z2-z1)) / pd2;  
x = x1 + u * (x2 - x1);  
x = y1 + u * (y2 - y1);  
y = y1 + u * (y2 - y1);  
z = z1 + u * (z2 - z1);  
if (type != LINE && u < 0) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                return Math.sgrt(ptLineDistSq(x1, y1, z1, x2, y2, z2, px, py, pz, type));
                                                                                                   // distance from point (px, py, pz) to line (x1, y1, z1)-(x2, y2, z2) // (or ray, or segment; in the case of the ray, the endpoint is the
                                                                                                                                                                                                                                                                                                                                                         double x2, double y2, double z2, double px, double py, double pz,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              double x2, double y2, double z2, double px, double py, double pz,
                                                                                                                                                                                                                                                                                                                                                                                   int type) { double pd2 = (x1-x2)*(x1-x2) + (y1-y2)*(y1-y2) + (z1-z2)*(z1-z2);
                                                                                                                                                                                                          public static final int LINE = 0;
public static final int SROMENT = 1;
public static final int RAY = 2;
public static double ptLineDistSq(double x1, double y1, double z1,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             public static double ptLineDist(double x1, double y1, double z1,
return Math.abs(d1 - d2) / Math.sqrt(a*a + b*b + c*c);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      return (x-px)*(x-px) + (y-py)*(y-py) + (z-pz)*(z-pz);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          if (type == SEGMENT && u > 1.0)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              double x, y, z;
if (pd2 == 0) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               int type) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       x = x2;
y = y2;
z = z2;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     x = x1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       y = y1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    z = z1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     y = y1;z = z1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    x = x1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    } else {
```

Delaunay.cc 11/31

```
// Slow but simple Delaunay triangulation. Does not handle
// degenerate cases (from O'Rourke, Computational Geometry in C)
// Running time: O(n^4)
// INPUT: x[] = x-coordinates
// INPUT: x[] = y-coordinates
// OUTPUT: triples = a vector containing m triples of indices
// corresponding to triangle vertices
```

```
while(b){a%=b; tmp=a; a=b; b=tmp;}
                                                                                                                                                                                                                    // return a % b (positive value)
                                                                                                                                                              typedef pair<int,int> PII;
                                                                                                                                                                                                                                      int mod(int a, int b) {
   return ((a%b)+b)%b;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     int lcm(int a, int b) {
   return a/gcd(a,b)*b;
                                                                                                                                                                                                                                                                                                                                                                 int gcd(int a, int b) {
                                                                                                                                          typedef vector<int> VI;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 // computes lcm(a,b)
                                              #include <algorithm>
                                                                                              using namespace std;
                                                                                                                                                                                                                                                                                                                                          computes gcd(a,b)
#include <iostream>
#include <vector>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       return solutions;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  VI solutions;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        return a;
                                                                                                                                                                                                                                                                                                                                                                                              int tmp;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       double xn = (y[i]-y[i])*(z[k]-z[i]) - (y[k]-y[i])*(z[j]-z[i]);
double yn = (x[k]-x[i])*(z[j]-z[i]) - (x[j]-x[i])*(z[k]-z[i]);
double zn = (x[j]-x[i])*(y[k]-y[i]) - (x[k]-x[i])*(y[j]-y[i]);
                                                                                                                                                                                                                                                                vector<triple> delaunayTriangulation(vector<T>& x, vector<T>& y) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       (y[m]-y[i])*yn +
(z[m]-z[i])*zn <= 0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        if (flag) ret.push_back(triple(i, j, k));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               for(i = 0; i < txi.size(); i++)
    printf("%d %d %d\n", tri[i].i, tri[i].j, tri[i].k);
return 0;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             bool flag = zn < 0;

for (int m = 0; flag && m < n; m++)

flag = flag && ((x[m]-x[i])*xn +
                                                                                                                struct triple {
   int i, j, k;
   triple() {}
   triple(int i, int j, int k) : i(i), j(j), k(k) {}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       for (int i = 0; i < n-2; i++) {
  for (int j = i+1; j < n; j++) {
      for (int k = i+1; k < n; k++) {
      if (j == k) continue;
      if (j == k) continue;</pre>
                                                                                                                                                                                                                                                                                                                                                                                   for (int i = 0; i < n; i++)
z[i] = x[i] * x[i] + y[i] * y[i];</pre>
                                                                                                                                                                                                                                                                                                                                        vector<triple> ret;
                                                                                                                                                                                                                                                                                          int n = x.size();
vector<T> z(n);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                //expected: 0 1 3 // 0 3 2
#include<vector>
using namespace std;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       return ret;
                                                                     typedef double T;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            int main()
{
```

Euclid.cc 12/31

```
// This is a collection of useful code for solving problems that
// involve modular linear equations. Note that all of the
// algorithms described here work on nonnegative integers.
```

```
int extended_euclid(int a, int b, int &x, int &y) {
    int x = y = 0;
    int xy = x = 1;
    whise (b) {
        int q = a/b;
        int t = b; b = a&b; a = t;
        t = xx; xx = x-q*xx; x = t;
        t = xx; xx = x-q*xx; x = t;
        t = xy; yy = y-q*yy; y = t;
    }

    return a;
}

// finds all solutions to ax = b (mod n)

VI modular_linear_equation_solver(int a, int b, int n) {
        int x, y;
        v = extended_euclid(a, n, x, y);
        int d = extended_euclid(a, n, x, y);
        if ((b&d)) {
            x = mod (x*'b)d, n);
        if ((b&d)) {
            x = mod (x*'b)d, n);
        for (int i = 0; i < d; i++)
            solutions.push_back(mod(x + i*(n/d), n));
        feturn solutions;
}

// computes b such that ab = 1 (mod n), returns -1 on failure
    int d = extended_euclid(a, n, x, y);
    int d = extended_euc
```

```
// to be relatively prime.
PII chinese_remainder_theorem(const VI &x, const VI &a) {
    PII chinese_remainder_theorem(const VI &x, const VI &a) {
    PII ret = make_pair(a[0], x[0]),
    PII i < x.size(); i++) {
        ret = chinese_remainder_theorem(ret.second, ret.first, x[i], a[i]);
    ret = chinese_remainder_theorem(ret.second, ret.first, x[i], a[i]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        VI sols = modular_linear_equation_solver(14, 30, 100);

for (int i = 0; i < (int) sols.size(); i++) cout << sols[i] << " ";
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          int xs[] = {3, 5, 7, 4, 6};
int as[] = {2, 3, 2, 3, 5};
PII ret = chinese_remainder_theorem(VI (xs, xs+3), VI(as, as+3));
cout << ret.first << " " < ret.second << end1;
cout << ret.first << " " < ret.second (VI(xs+3, xs+5), VI(as+3, as+5));
cout << ret.first << " " < ret.second <</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  // computes x and y such that ax + by = c; on failure, x = y =-1 void linear_diophantine(int a, int b, int c, int &x, int &y) {
chinese_remainder_theorem(int x, int a, int y, int b) \{
                                                                                                                                                                                                                                                                                                                                                                           // failure, M = -1. Note that we do not require the a[i]'s
                                                                                                                                                                                                                                                   // Chinese remainder theorem: find z such that // z % x[i] = a[i] for all i. Note that the solution is // unique modulo M = lcm_i (x[i]). Return (z,M). On
                                                                                                        if (a%d != b%d) return make_pair(0, -1);
return make_pair(mod(s*b*x+t*a*y,x*y)/d, x*y/d);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      int x, y;
int d = extended_euclid(14, 30, x, y);
cout << d << " " << x << " " << y << endl;</pre>
                                      int s, t;
int d = extended_euclid(x, y, s, t);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       x = c/d * mod_inverse(a/d, b/d);

y = (c-a*x)/b;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              cout << mod_inverse(8, 9) << endl;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            linear_diophantine(7, 2, 5, x, y);
cout << x << " " << y << endl;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                if (ret.second == -1) break;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   // expected: 2 cout << gcd(14, 30) << endl;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   // expected: 2 -2 1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     // expected: 95 45
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        // expected: 23 56
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                int d = gcd(a,b);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               // expected: 8
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      x = y = -1; } else {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          return ret;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             int main() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               if (c%d)
```

GaussJordan.cc 13/31

```
int pi = 0; i < n; i++) {
  int pi = -1, pk = -1; i ++) if (lipiv[j])
  for (int j = 0; j < n; j++) if (lipiv[j])
  for (int k = 0; k < n; k++) if (lipiv[k])
  if (pj == -1 || fabs(a[j][k]) > fabs(a[pj][pk])) { pj = j; pk = k; }
  if (fabs(a[pj][pk]) < EPS) { cerr < "Watrix is singular." << endl; exit(0); }
  ipiv[pk]++;</pre>
                                                                                                                                                                                                                                                                                                                                                                  X = \text{an nxm matrix (stored in b[][])} A^{\wedge}\{-1\} = \text{an nxn matrix (stored in a[][])} returns determinant of a[][]
                                                                                      (1) solving systems of linear equations (AX=B)
                                                                                                                 (2) inverting matrices (AX=I)
(3) computing determinants of square matrices
// Gauss-Jordan elimination with full pivoting.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   for (int p = 0; p < n; p++) a[pk][p] *= c; for (int p = 0; p < m; p++) b[pk][p] *= c; for (int p = 0; p < n; p++) if (p != pk) {
                                                                                                                                                                                                                                                                           a[][] = an nxn matrix
b[][] = an nxm matrix
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              \label{eq:viscosity} \begin{split} \text{VI irow(n), icol(n), ipiv(n);} \\ \text{T det} &= 1; \end{split}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                swap(a[pj], a[pk]);
swap(b[pj], b[pk]);
if (pj] = pk) det *= -1;
irow(i] = pj;
icol[i] = pk;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        T GaussJordan(VVT &a, VVT &b)
const int n = a.size();
const int m = b[0].size();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   T c = 1.0 / a[pk][pk];
det *= a[pk][pk];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   const double EPS = 1e-10;
                                                                                                                                                                                                                 Running time: O(n^3)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             typedef vector<int> VI;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               typedef vector<T> VT;
typedef vector<VT> VVT;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               using namespace std;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             a[pk][pk] = 1.0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             #include <iostream>
#include <vector>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            typedef double T;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       #include <cmath>
                                                                                                                                                                                                                                                                                                                                                                        OUTPUT:
                                                                                                                                                                                                                                                                           INPUT:
```

```
for (int p = n-1; p >= 0; p--) if (irow[p] != icol[p]) {
    for (int k = 0; k < n; k++) swap(a[k][irow[p]], a[k][icol[p]]);</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                 const int n = 4;
const int m = 2;
double Aln|[n] = { {1,2,3,4}, {1,0,1,0}, {5,3,2,4}, {6,1,4,6} };
double Aln|[n] = { {1,2},{4,3},{5,6},{8,7} };

VUT a(n), b(n);
for (int i = 0); i < n; i++) {
    a(i) = VT(A(i), A(i) + n);
    b(i) = VT(B(i), B(i) + n);
    b(i) = VT(B(i), B(i) + m);
    construction</pre>
c = a[p][pk];
a[p][pk] = 0;
for (int q = 0; q < n; q++) a[p][q] -= a[pk][q] * c;
for (int q = 0; q < n; q++) b[p][q] -= b[pk][q] * c;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     0.166667 0.166667 0.333333 -0.333333 0.233333 0.833333 -0.133333 -0.0666667
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  // expected: -0.233333 0.166667 0.133333 0.066667 // 0.166667 0.166667 0.333333 -0.333333
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         cout << "Determinant: " << det << endl;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    // 0.05 -0.3333 0.83333 -0.3.

cout << "Inverse: " < endl;

for (int i = 0; i < n; i++) {

for (int j = 0; j < n; i++) {

cout << a[i][j] << ' ';

}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 double det = GaussJordan(a, b);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           //
cout << "Solution: " << endl;
for (int i = 0; i < m; i+) {
    for (int j = 0; i < m; i+) {
      cout << b[i][i] << '';
}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      -0.166667 0.5
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      // expected: 1.63333 1.3 // -0.166667 0.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      2.36667 1.7
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         // expected: 60
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       << endl;</pre>
                                                                                                                                                                                                                                                                                                          return det;
                                                                                                                                                                                                                                                                                                                                                                                         int main() {
```

ReducedRowEchelonForm.cc 14/31

```
// Reduced row echelon form via Gauss-Jordan elimination
// with partial pivoting. This can be used for computing
// the rank of a matrix.
```

```
const int n = 5;
const int m = 4;
double A[n][m] = { \{16,2,3,13\},\{5,11,10,8\},\{9,7,6,12\},\{4,14,15,1\},\{13,21,21,13\} \};
VVT a(n);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    for (int j = 0; j < m; j++) a[i][j] -= t * a[r][j];
                                                                                   rref[][] = an nxm matrix (stored in a[][])
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          T s = 1.0 / a[r][c];

for (int j = 0; j < m; j++) a[r][j] *= s;

for (int i = 0; i < n; i++) if (i i= r) {

T t = a[i][c];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            int n = a.size();
int m = a[0].size();
int r = 0;
for (int c = 0; c < m && r < n; c++) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  cout << "Rank: " << rank << endl;
                                         a[l][l] = an nxm matrix
                                                                                                           returns rank of a[][]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          0 0 0 3.22398e-15

cout << "xref: " << endl;

for (int i = 0; i < 5; i++) {

for (int j = 0; j < 4; j++)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       0 0 0 2.78206e-15
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  for (int i = 0; i < n; i++)
a[i] = VT(A[i], A[i] + n);</pre>
                                                                                                                                                                                                                                                                            const double EPSILON = 1e-10;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       // expected: 1 0 0 1 // 0 1 // 0 1 0 3 // 0 0 1 -3 //
// Running time: O(n^{3})
                                                                                                                                                                                                                                                                                                               typedef double T;
typedef vector<T> VI;
typedef vector<VT> VVT;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    int rank = rref (a);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           swap(a[j], a[r]);
                                                                                                                                                                                                                                    using namespace std;
                                                                                                                                                     #include <iostream>
                                                                                                                                                                                                                                                                                                                                                                                                     int rref(VVT &a) {
                                                                                                                                                                           #include <vector>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              // expected: 4
                                                                                                                                                                                             #include <cmath>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               int main(){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      return r;
                                                                                     OUTPUT:
                                         INPUT:
```

```
cout << ali)[ij << ' ';
cout << endl;
}
</pre>
```

```
return cpx(a.a * b.a - a.b * b.b, a.a * b.b + a.b * b.a);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 return cpx(r.a / b.modsq(), r.b / b.modsq());
                                                                                                                                                                            cpx(double aa):a(aa){{}}
cpx(double aa, double bb):a(aa),b(bb){{}}
double a;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       return cpx(cos(theta),sin(theta));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                    return cpx(a.a + b.a, a.b + b.b);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          const double two_pi = 4 * acos(0);
FFT new.cpp 15/31
                                                                                                                                                                                                                                                                                                                                                                                                                                  cpx operator +(cpx a, cpx b)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        cpx operator *(cpx a, cpx b)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             dpx operator /(cpx a, cpx b)
                                                                                                                                                                                                                                                      double modsq(void) const
                                                                                                                                                                                                                                                                                      return a * a + b * b;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            output array
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              cpx r = a * b.bar();
                                                                                                                                                                                                                                                                                                                                                           return cpx(a, -b);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             input array
                                                                                                                                                                                                                                                                                                                          cpx bar(void) const
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     cpx EXP(double theta)
                                                         #include <cassert>
                                                                            #include <cstdio>
                                                                                             #include <cmath>
                                                                                                                                                                                                                                      double b;
                                                                                                                                 struct cpx
                                                                                                                                                             cpx(){}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             // in:
```

```
cpx even = out[i];
cpx odd = out[i];
cpx odd = out[i] + size / 2];
out[i] = even + ExP(dir * two_pi * i / size) * odd;
out[i] = even + ExP(dir * two_pi * (i + size / 2) / size) * odd;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       h(n) = \operatorname{sum} \ of \ E(k)g(n-k) \ (k=0,\ldots,N-1), where, the index is cyclic, \Gamma(n-1) = \Gamma(N-1), \Gamma(n-2) = \Gamma(N-2), etc. Let \Gamma(0,\ldots,N-1) be \Gamma\Gamma\Gamma(1) = \Gamma(n-1), \Gamma(1) = \Gamma(n-1), define G and H. The convolution theorem says \Pi(n) = \Gamma(n)G(n) (element-wise product).

    Compute F and G (pass dir = 1 as the argument).
    Get H by element-wise multiplying F and G.
    Get h by taking the inverse FFT (use dir = -1 as the argument) and *dividing by N*. DO NOT FORGET THIS SCALING FACTOR.

                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             printf("If rows come in identical pairs, then everything works.\n");
                                                                                                                                                                                                                       FFT(in, out, step * 2, size / 2, dir);
FFT(in + step, out + size / 2, step * 2, size / 2, dir);
for(int i = 0 ; i < size / 2 ; i++)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 \begin{aligned} \exp & \ a[8] \ = \ \{0,\ 1,\ \exp(1,3),\ \exp(0,5),\ 1,\ 0,\ 2,\ 0\}; \\ \exp & \ b[8] \ = \ \{1,\ \exp(0,-2),\ \exp(0,1),\ 3,\ -1,\ -3,\ 1,\ -2\}; \end{aligned} 
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    To compute h[\ ] in O(N \log N) time, do the following:
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    Want to compute the convolution h, defined by
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  Ai = Ai + a[j] * EXP(j * i * two_pi / 8);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     printf("%7.21f%7.21f", A[i].a, A[i].b);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             f[0...N-1] and g[0..N-1] are numbers
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             printf("%7.21f%7.21f", Ai.a, Ai.b);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            for(int j = 0 ; j < 8 ; j++)</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  for(int i = 0 ; i < 8 ; i++)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           printf("\n");
for(int i = 0 ; i < 8 ; i++)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 for(int i = 0 ; i < 8 ; i++)
AB[i] = A[i] * B[i];</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       cpx aconvb[8];
FFT(AB, aconvb, 1, 8, -1);
if(size < 1) return;
if(size == 1)</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 FFT(a, A, 1, 8, 1);
FFT(b, B, 1, 8, 1);
                                                                                                             out[0] = in[0];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             cpx Ai(0,0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       printf("\n");
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   int main(void)
{
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             cpx AB[8];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          cpx A[8];
cpx B[8];
```

Simplex.cc 16/31

```
// Two-phase simplex algorithm for solving linear programs of the form
                                                                                                                                                                                                                                                                                                                                                                                                   To use this code, create an LPSolver object with A, b, and c as
                                                                                                                                                                  INPUT: A -- an m x n matrix b -- an \ m-dimensional \ vector \\ c -- an \ n-dimensional \ vector \\ x -- a \ vector \ where the optimal solution will be stored <math display="block">
                                                                                                                                                                                                                                                                                                             OUTPUT: value of the optimal solution (infinity if unbounded
                                                                                                                                                                                                                                                                                                                                          above, nan if infeasible)
                                                                                                                                                                                                                                                                                                                                                                                                                                  call Solve(x).
                                                   C^{\wedge}T \quad X
AX \quad c = \quad D
X \quad > = \quad 0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     typedef long double DOUBLE;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               typedef vector<DOUBLE> VD;
typedef vector<VD> VVD;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           const DOUBLE EPS = 1e-9;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  typedef vector<int> VI;
                                                                                                                                                                                                                                                                                                                                                                                                                               // arguments. Then,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     using namespace std;
                                                                                     subject to
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               #include <iomanip>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           struct LPSolver {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              #include <vector>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         #include inits>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     #include <cmath>
                                                      maximize
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        int m, n;
VI B, N;
```

```
-numeric_limits<DOUBLE>::infinity();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  int s = -1;
for (int j = 0; j <= n; j++) {
   if (phase == 2 && N[j] == -1) continus;
   if (s == -1 || D[x][j] < D[x][s] || D[x][j] == D[x][s] && N[j] < N[s]) s = j;
   if (s == -2 || D[x][s] || D[x][s] || D[x][s] && D[x][s] && D[x][s] || D[x][x] || D[x][s] || D[x][x] 
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                for (int j = 0; j <= n; j++) if (s == -1 || D[i][j] < D[i][s] || D[i][j] == D[i][s] && N[j] < N[s]) s
                                          m(b.size()), n(c.size()), N(n+1), B(m), D(m-2, VD(n+2)) {
  for (int i = 0; i < m; i++) for (int j = 0; j < n; j++) D[i][j] = A[i][j];
  for (int i = 0; i < m; i++) { B[i] = n+i; D[i][n] = -1; D[i][n+1] = D[i]; }
  for (int j = 0; j < n; j++) { N[j] = j; D[i][n] = -2[j]; }
  N[n] = -1; D[m+1][n] = 1;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             int r = -1;
for (int i = 0; i < m; i++) {
   if (D[i][s] <= 0) continue;
   if (D[i][s] <= 0) continue;
   if (x == -1 | | D[i][s] | | D[i][s] < D[x][n+1] / D[x][s] ||
        D[i][n+1] / D[i][s] == D[x][n+1] / D[x][s] && B[i] < B[x]) x = i;
</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  int x = 0;
for (int | 1 = 1; i < m; i++) if (D[i][n+1] < D[x][n+1]) x = i;
if (D[x][n+1] <= -EDS) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                x = VD(n);
for (int i = 0; i < m; i++) if (B[i] < n) x[B[i]] = D[i][n+1];
return D[m][n+1];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       if (!Simplex(2)) return numeric_limits<DOUBLE>::infinity();
LPSolver(const VVD &A, const VD &b, const VD &c) :
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               if (!Simplex(1) | D[m+1][n+1] < -EPS) return
for (int i = 0; i < m; i++) if (B[i] == -1) {</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  if (D[x][s] >= -EPS) return true;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            bool Simplex(int phase) {
  int x = phase == 1 ? m+1 : m;
  while (true) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             if (r == -1) return false;
Pivot(r, s);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             DOUBLE Solve(VD &x) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              Pivot(i, s);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     int s = -1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                const int m = 4;
```

FastDijkstra.cc 17/31

```
scanf ("%d%d", &vertex, &dist);
edges[i].push_back (make_pair (dist, vertex)); // note order of arguments here
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 // use priority queue in which top element has the "smallest" priority priority_queue.pII, vector.pII>, greater.pII> > Q; vector.int> dist(N, INF), dad(N, -1);
// Implementation of Dijkstra's algorithm using adjacency lists
                                    // and priority queue for efficiency.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    vector<vector<PII> > edges(N);
for (int i = 0; i < N; i++){</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          scanf ("%d", &M);
for (int j = 0; j < M; j++){</pre>
                                                                                                    // Running time: O(|E| \log |V|)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      scanf ("%d%d%d", &N, &s, &t);
                                                                                                                                                                                                                                                             using namespace std;
const int INF = 200000000;
                                                                                                                                                                                                                                                                                                                            typedef pair<int,int> PII;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             int vertex, dist;
                                                                                                                                                                                                    #include <stdio.h>
                                                                                                                                                                      #include <queue>
                                                                                                                                                                                                                                                                                                                                                                                                                                                    int N, s, t;
                                                                                                                                                                                                                                                                                                                                                                                        int main() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   int M;
```

```
Q.push (make_pair (0, s));
date[s] = 0;
while (i0.empt/) {
    PII p = 0.top();
    if (p.eecond == t) break;
Q.pop();
    int here = p.second;
    if (dist[here] + it->first < dist[it->second]) {
        dist[it->second] = dist here] + it->first;
        dist[it->second]);
    }
}
printf ("%d\n", dist[l]);
if (dist[r] < INF)
for(int i=t;i]=-1;i=dad[i])

return 0;
}
return 0;</pre>
```

SCC.cc 18/31

```
for(i=spr[x];i;i=er[i].nxt) if(v[er[i].e]) fill_backward(er[i].e);
                                                                                                                                                                                                                                                                                 for(i=sp[x];i;i=e[i].nxt) if(!v[e[i].e]) fill_forward(e[i].e);
stk(++stk(0]]=x;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           void add_edge(int v1, int v2) //add edge v1->v2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             memset(v, false, sizeof(v));
for(i=1;i<=V;i++) if(!v[i]) fill_forward(i);</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           e [++E].e=v2; e [E].mxt=sp [v1]; sp [v1]=E; er[ E].e=v1; er[E].mxt=spr[v2]; spr[v2]=E;
                                                                                                                        int group_cnt, group_num[MAXV];
bool v[MAXV];
                        struct edge{int e, nxt;};
                                                                                                                                                                                                                                                                                                                                                                               void fill_backward(int x)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                group_num[x]=group_cnt;
                                                                                                      int sp[MAXV], spr[MAXV];
                                                                                                                                                                                                   void fill_forward(int x)
                                                                           edge e[MAXE], er[MAXE];
#include<memory.h>
                                                                                                                                                                              int stk[MAXV];
                                                                                                                                                                                                                                                                                                                                                                                                                                                           v[x]=false;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  stk[0]=0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            void SCC()
                                                                                                                                                                                                                                                         int i;
                                                                                                                                                                                                                                                                                                                                                                                                                                     int i;
```

```
group_cnt=0;
for(i=stk[0];i>=1;i--) if(v[stk[i]]){group_cnt++; fill_backward(stk[i]);}
}
```

EulerianPath.cc 19/31

```
adj[vn].erase(adj[v].front().reverse_edge);
                                                                                                                                                                                                                                                                                                                                                         // adjacency list
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     int vn = adj[v].front().next_vertex;
                                                                                                                                                                                                                :next_vertex(next_vertex)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   adj[v].pop_front();
find_path(vn);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               adj[a].push_front(Edge(b));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             adj[b].push_front(Edge(a));
iter itb = adj[b].begin();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        iter ita = adj[a].begin();
                    typedef list<Edge>::iterator iter;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             ita->reverse_edge = itb;
itb->reverse_edge = ita;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       while(adj[v].size() > 0)
                                                                                                                                                                                                                                                                                                                                                            list<Edge> adj[max_vertices];
                                                                                                                                                                                      Edge(int next_vertex)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    void add_edge(int a, int b)
                                                                                                                                                                                                                                                                                                              const int max_vertices = ;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       path.push_back(v);
                                                                                                                                           iter reverse_edge;
                                                                                                                    int next_vertex;
                                                                                                                                                                                                                                                                                                                                                                                                                                                    void find_path(int v)
                                                                                                                                                                                                                                                                                                                                  int num_vertices;
                                                                                                                                                                                                                                                                                                                                                                                                         vector<int> path;
struct Edge;
                                                                    struct Edge
```

SuffixArray.cc 20/31

```
// Suffix array construction in O(L log'2 L) time. Routine for
// computing the length of the longest common prefix of any two
// suffixes in O(log L) time.
// INPUT: string s
// OUTPUT: array suffix[] such that suffix[i] = index (from 0 to L-1)
```

```
for (int i = 0; i < L; i++)
M[i] = make_pair(make_pair(P[level-1][i], i + skip < L ? P[level-1][i + skip] : -1000)</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          sort(M.begin(), M.end());
for (int i = 0; i < L; i++)
P[level][M[i].second] = (i > 0 && M[i].first == M[i-1].first) ? P[level][M[i-1].second
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             SuffixArray(const string &s) : L(s.length()), s(s), P(1, vector<int>(L, 0)), M(L) {
  for (int i = 0; i < L; i++) P(0][i] = int(s[i]);
  for (int skip = 1, level = 1; skip < L; skip *= 2, level++) {
  P.push_Dack(vector<int>(L, 0));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    // returns the length of the longest common prefix of s[i...L-1] and s[j...L-1] int LongestCommonPrefix(int i, int j) {
of substring s[i...L-1] in the list of sorted suffixes. That is, if we take the inverse of the permutation suffix[],
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              if (i == j) return L - i;
for (int k = P.sise() - l; k >= 0 && i < L && j < L; k--) {
   if (P(k|[i] == P(k][i]) {
     i += 1 << k;
     j += 1 << k;
     j += 1 << k;
}</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       for (int i = 0; i < v.size(); i++) cout << v[i] << " ";</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    vector<int> GetSuffixArray() { return P.back(); }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        cout << endl;
cout << suffix.LongestCommonPrefix(0, 2) << endl;</pre>
                                                                    we get the actual suffix array.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  vector<int> v = suffix.GetSuffixArray();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       vector<pair<pair<int,int>,int> M;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      // Expected output: 0 5 1 6 2 3 4
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              SuffixArray suffix("bobocel");
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      cel is the 2'nd suffix el is the 3'rd suffix
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      // bobocel is the 0'th suffix
// obocel is the 5'th suffix
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 bocel is the 1'st suffix
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              ocel is the 6'th suffix
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          I is the 4'th suffix
                                                                                                                                                                                                                                                                                                                                                                                                                                                       vector<vector<int> > P;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               len += 1 << k;
                                                                                                                                                                                                                                                                                                                                                  struct SuffixArray {
                                                                                                                                                                                                                                                                                 using namespace std;
                                                                                                                                                   <vector>
                                                                                                                                                                                                             #include <string>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            int len = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            return len;
                                                                                                                                                                                                                                                                                                                                                                                      const int L;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 int main() {
                                                                                                                                            #include
```

BIT.cc 21/31

```
// get largest value with cumulative sum less than or equal to x; // for smallest, pass x-1 and add 1 to result
                                                                                                                                                                                                                                                                                                                                   // get cumulative sum up to and including x
int get(int x) {
  int res = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          int getind(int x) {
  int idx = 0, mask = N;
  while(mask &E idx < N) {
    int t = idx + mask;
    if(x >= tree[t]) {
                                                                                                                                                                                      void set(int x, int v) {
  while(x <= N) {</pre>
                                                                                                     int tree[(1<<LOGSZ)+1];
int N = (1<<LOGSZ);</pre>
                                                                                                                                                                     // add v to value at x
#include <iostream>
using namespace std;
                                                                                                                                                                                                                                                                                                                                                                                                   while(x) {
  res += tree[x];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     x -= tree[t];
                                                                                                                                                                                                                                tree[x] += v;
x += (x & -x);
                                                                                                                                                                                                                                                                                                                                                                                                                                             x -= (x & -x);
                                                             #define LOGSZ 17
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           mask >>= 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  idx = t;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       return res;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       return idx;
```

UnionFind.cc 22/31

```
//union-find set: the vector/array contains the parent of each node int find(vector <int> (x_1)^2 + (x_2)^2 + (x_3)^2 + (x_3
```

KDTree.cc 23/31

```
- handles nearest-neighbor query in \mathcal{O}(1g~n) if points are well distributed - worst case for nearest-neighbor may be linear in pathological case
// A straightforward, but probably sub-optimal KD-tree implmentation that's // probably good enough for most thinna (annual in
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         bbox() \; : \; x0(sentry), \; x1(-sentry), \; y0(sentry), \; y1(-sentry) \; \big\{ \big\}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        void compute(const vector<point> &v) {
    for (int i = 0; i < v.size(); ++i) {
        x0 = min(x0, v[i].x); x1 = max(x1, v[i].x);
}</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              ntype x, y; point(ntype xx = 0, ntype yy = 0) : x(xx), y(yy) {}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         // point structure for 2D-tree, can be extended to 3D
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        // number type for coordinates, and its maximum value
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 // computes bounding box from a bunch of points
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                const ntype sentry = numeric_limits<ntype>::max();
                                                                                                                                                    - constructs from n points in O(n lg^2 n) time
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               bool operator == (const point &a, const point &b)
                                                                                                                                                                                                                                                                                                         Sonny Chan, Stanford University, April 2009
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            ntype pdist2(const point &a, const point &b)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                &b)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      bool on_y(const point &a, const point &b)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              // sorts points on x-coordinate
bool on_x(const point &a, const point
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            ntype dx = a.x-b.x, dy = a.y-b.y; return dx*dx + dy*dy;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   return a.x == b.x && a.y == b.y;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             // bounding box for a set of points
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              // squared distance between points
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                // sorts points on y-coordinate
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    ntype x0, x1, y0, y1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          typedef long long ntype;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         return a.x < b.x;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           return a.y < b.y;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       using namespace std;
                                                                                                                                                                                                                                                                                                                                                                                                                        #include <iostream>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               #include <cstdlib>
                                                                                                                                                                                                                                                                                                                                                                                                                                                      #include <vector>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                #include inits>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   struct point {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   struct bbox
```

```
// simple kd-tree class to hold the tree and handle queries
int half = vp.size()/2;
vectorspoint> vl(vp.begin(), vp.begin()+half);
vectorspoint> vr(vp.begin()+half, vp.end());
first = new Kdnode(); first->construct(vl);
second = new Kdnode(); second->construct(vl);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            // squared distance to the nearest
ntype nearest(const point &p) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                         kdtree(const vector<point> &vp)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           if (bfirst < bsecond) {</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          return search(root, p);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      ~kdtree() { delete root; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              root = new kdnode();
root->construct(v);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          // some basic test code here
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         if (node->leaf) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  return best;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              return best;
                                                                                                                                                                                                                                                                                                                                                                 kdnode *root;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       else {
                                                                                                                                                                                                                                                                                                   struct kdtree
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      int main()
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       split on x if the bbox is wider than high (not best heuristic...)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                ~kdnode() { if (first) delete first; if (second) delete second;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           // true if this is a leaf node (has one point)
// the single point of this is a leaf
// bounding box for set of points in children
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           // intersect a point with this node (returns squared distance)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  return pdist2(point(p.x, y0), p);
return pdist2(point(p.x, y1), p);
return 0;
                                                                                                                                                                                                              return pdist2(point(x0, y0), p);
return pdist2(point(x0, y1), p);
return pdist2(point(x0, p.y), p);
                                                                                                                                                                                                                                                                                                                                                           return pdist2(point(x1, y0), p);
return pdist2(point(x1, y1), p);
return pdist2(point(x1, p.y), p);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        // recursively builds a kd-tree from a given cloud of points void construct(vector<br/>cpoint> &vp)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       // stores a single node of the kd-tree, either internal or leaf
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        kdnode *first, *second; // two children of this kd-node
      y1 = max(y1, v[i].y);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        // if we're down to one point, then we're a leaf :
if (vp.size() == 1) {
  leaf = true;
                                                                                                                      // squared distance between a point and this bbox, 0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         if (bound.x1-bound.x0 >= bound.y1-bound.y0)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   // compute bounding box for points at this node
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    kdnode() : leaf(false), first(0), second(0) {}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   sort(vp.begin(), vp.end(), on_x);
// otherwise split on y-coordinate
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             sort(vp.begin(), vp.end(), on_y);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           ntype intersect(const point &p) {
                                                                                                                                                      ntype distance(const point &p) {
      y0 = min(y0, v[i].y);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       return bound.distance(p);
                                                                                                                                                                                                              if (p,y < y0)
else if (p,y > y1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           if (p.y < y0)
else if (p.y > y1)
                                                                                                                                                                                                                                                                                                                                                                                          else if (p.y > y1)
                                                                                                                                                                                                                                                                                                                               else if (p.x > x1) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  bound.compute(vp);
                                                                                                                                                                                                                                                                                                                                                                 if (p.y < y0)
                                                                                                                                                                                     if (p.x < x0) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   pt = vp[0];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                'punoq xoqq
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              bool leaf;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           else {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  else {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 point pt;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      struct kdnode
```

```
// constructs a kd-tree from a points (copied here, as it sorts them)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 // choose the side with the closest bounding box to search first // (note that the other side is also searched if needed)
                                                                                                                                                                                                                                                                                                                                                         // recursive search method returns squared distance to nearest point
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   // commented special case tells a point not to find itself
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           best = min(best, search(node->first, p));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  best = min(best, search(node->second,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  ntype bsecond = node->second->intersect(p);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        ntype best = search(node->second, p);
if (bfirst < best)</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    ntype bfirst = node->first->intersect(p);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      ntype best = search(node->first, p);
if (bsecond < best)</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 if (p == node->pt) return sentry;
                                                                                       vector<point> v(vp.begin(), vp.end());
                                                                                                                                                                                                                                                                                                                                                                                             ntype search(kdnode *node, const point &p)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        return pdist2(p, node->pt);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 // divide by taking half the array for each child
// (not best performance if many duplicates in the middle)
```

p));

SegmentTreeLazy.java 24/31

```
leaf[curr] += (Math.min(end,tEnd)-Math.max(begin,tBegin)+1) * val;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    public void update(int curr, int tBegin, int tEnd, int begin, int end, int val)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  if(tEnd >= begin && mid+1 <= end)
update(2*curr+1, mid+1, tEnd, begin, end, val);</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        end)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      update(2*curr, tBegin, mid, begin, end, val);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        public long query(int curr, int tBegin, int tEnd, int begin, int
                                                                                                                                                                                                                                                                                                                                                                            public void build(int curr, int begin, int end, int[] list)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           build(2 * curr, begin, mid, list);
build(2 * curr + 1, mid+1, end, list);
leaf[curr] = leaf[2*curr] + leaf[2*curr+1];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     public void update(int begin, int end, int val) {
    update(1,0,origSize-1,begin,end,val);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           int mid = (tBegin+tEnd)/2;
if(mid >= begin && tBegin <= end)</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            return query(1,0,origSize-1,begin,end);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            if(tBegin >= begin && tEnd <= end)
                                                                                                           public int origSize;
public SegmentTreeRangeUpdate(int[] list)
                                                                                                                                                                                                                                                         update = new long[4*list.length];
build(1,0,list.length-1,list);
                                                                                                                                                                                                                                                                                                                                                                                                                                                leaf[curr] = list[begin];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               int mid = (begin+end)/2;
                                                                                                                                                                                      origSize = list.length;
leaf = new long[4*list.length];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        public long query(int begin, int end)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                update[curr] += val;
public class SegmentTreeRangeUpdate {
                                                                                                                                                                                                                                                                                                                                                                                                                    if(begin == end)
                                   public long[] leaf;
public long[] update;
```


LCA.cc 25/31

int LCA(int p, int q)

```
node p situated on the same level as q
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    // read p, the parent of node i or -1 if node i is the root
// ensure node p is at least as deep as node q if(L[p] < L[q])
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    // read num_nodes, the total number of nodes
                                                                                                                                                                                                                                                                                        for(int i = log_num_nodes; i >= 0; i--)
if(A[p][i] != -1 && A[p][i] != A[q][i])
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 // precompute A using dynamic programming
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   A[i][j] = A[A[i][j-1]][j-1];
                                                                                        // "binary search" for the ancestor of n
for(int i = log_num_nodes; i >= 0; i.-)
if(L[p] - (1<4i) >= L[q])
p = A[p][i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   for(int i = 0; i < num_nodes; i++)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        children[p].push_back(i);
                                                                                                                                                                                                                                                                   // "binary search" for the LCA
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         log_num_nodes=lb(num_nodes);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         int main(int argc,char* argv[])
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          A[i][j] = -1;
                                                                                                                                                                                                                                                                                                                                                     p = A[p][i];
q = A[q][i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 root = i;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           A[i][0] = p;
                                                                                                                                                                                                                                                                                                                                                                                                                                       return A[p][0];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          // precompute L
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    if(p != -1)
                                                                                                                                                                                                                          return p;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              DFS(root, 0);
                                                                                                                                                                                                      if(p == q)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               else
```

LongestIncreasingSubsequence.cc 26/31

```
// Given a list of numbers of length n, this routine extracts a
// longest increasing subsequence.
```

```
PII item = make_pair(v[i], 0);
VPII::iterator it = lower_bound(best.begin(), best.end(), item);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 PII item = make_pair(v[i], i);
VPII::iterator it = upper_bound(best.begin(), best.end(), item);
                                                                                                                    OUTPUT: a vector containing the longest increasing subsequence
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                if (it == best.end()) {
  dad[i] = (best.size() == 0 ? -1 : best.back().second);
  best.push_back(iten);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    VI ret;
for (int i = best.back().second; i >= 0; i = dad[i])
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      VI LongestIncreasingSubsequence(VI v) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    for (int i = 0; i < v.size(); i++) {</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      reverse(ret.begin(), ret.end());
                                                                                       INPUT: a vector of integers
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 } else {
  dad[i] = dad[it->second];
  *it = item;
//
// Running time: O(n log n)
                                                                                                                                                                                                                                                                                                                                     typedef vector<int> VI;
typedef pair<int,int> PII;
typedef vector<PII> VPII;
                                                                                                                                                                                                                                                                                                                                                                                                                                                    #define STRICTLY_INCREASNG
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            ret.push_back(v[i]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             VI dad(v.size(), -1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                item.second = i;
                                                                                                                                                                                                                                #include <algorithm>
                                                                                                                                                                                                                                                                                       using namespace std;
                                                                                                                                                                           #include <iostream>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          #else
```

Dates.cc 27/31

```
// Routines for performing computations on dates. In these routines,
// months are expressed as integers from 1 to 12, days are expressed
// as integers from 1 to 31, and years are expressed as 4-digit
// integers.
#include clostream>
#include cstring>
using namespace std;
string dayOfWeek[] = {"Mon", "Tue", "Wed", "Thu", "Pri", "Sat", "Sun"};
```

```
// converts integer (Julian day number) to Gregorian date: month/day/year
void introDate (int jd, int &m, int &d, int &y){
int x, n, i, j;
converts Gregorian date to integer (Julian day number)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               // converts integer (Julian day number) to day of week
                                                                                                 367 * (m - 2 - (m - 14) / 12 * 12) / 12 - 3 * ((\rm Y + 4900 + (m - 14) / 12) / 100) / 4
                                                                           1461 * (y + 4800 + (m - 14) / 12) / 4 +
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      int dateToInt (int m, int d, int y) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                int jd = dateToInt (3, 24, 2004);
                                                                                                                                                                                                                                                                                                                              x = jd + 68569;

n = 4 * x / 146097;

x = (146097 * n + 3) / 4;

i = (4000 * (x + 1)) / 1461001;

x = 1461 * i / 4 - 31;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        int main (int argc, char **argv){
                                                                                                                                                                                                                                                                                                                                                                                                                                                       j = 80 * x / 2447;
d = x - 2447 * j / 80;
x = j / 11;
m = j + 2 - 1 * x;
y = 100 * (n - 49) + i + x;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            string day = intToDay (jd);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    string intToDay (int jd){
    return dayOfWeek[jd % 7];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         int m, d, y;
intToDate (jd, m, d, y);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               // expected output:
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  3/24/2004
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       2453089
```

LogLan.java 28/31

```
// Code which demonstrates the use of Java's regular expression libraries.
// This is a solution for
// Loglan: a logical language
// http://acm.uva.es/p/v1/134.html
// In this problem, we are given a regular language, whose rules can be
// inferred directly from the code. For each sentence in the input, we must
// determine whether the sentence matches the regular expression or not. The
// code consists of [1] building the regular expression (which is fairly
// complex) and (2) using the regex to match sentences.
```

```
String predclaim = "(" + predname + space + BA + space + preds + "|" + DA + space +
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 s.length() to get length of string s.charAt() to extract characters from a Java string s.trim() to remove whitespace from the beginning and end of Java string
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  s.lastIndexOf("apple") returns index of last occurrence of "apple" in s
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             s.toLowerCase() / s.toUpperCase() returns a new lower/uppercased string
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        String predname = "(" + LA + space + predstring + "|" + NAM + ")"; String preds = "(" + predstring + "(" + space + A + space + predstring + ")*)";
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             s.indexOf("apple") returns index of first occurrence of "apple" in s
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    String verbpred = "(" + MOD + space + predstring + ")";
String statement = "(" + predname + space + verbpred + space + predname + "|"
predname + space + verbpred + ")";
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           // In this problem, each sentence consists of multiple lines, where the // line is terminated by a period. The code below reads lines until
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           // encountering a line whose final character is a '.'. Note the use of
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      String PREDA = "(" + C + C + A + C + A + " | " + C + A + C + C + A + ")";
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  s.replace(c,d) replaces occurrences of character c with d
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             Integer.parseInt(s) converts s to an integer (32-bit)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 String predstring = "(" + PREDA + "(" + space + PREDA + ")*)";
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                String sentence = "(" + statement + "|" + predclaim + ")";
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             s.startsWith("apple) returns (s.indexOf("apple")
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   Long.parseLong(s) converts s to a long (64-bit)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  s.compareTo(t) < 0 if s < t, lexicographically
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 // Other useful String manipulation methods include
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        Double.parseDouble(s) converts s to a double
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              Pattern pattern = Pattern.compile (regex);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             public static void main (String args[]) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     Scanner s = new Scanner(System.in);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           String NAM = "([a-z]*" + C + ")";
                                                                                                                                                                                                                                                                                                                                                         String C = "([a-z&&[^aeiou]])";
String MOD = "(g" + A + ")";
                                                                                                                                                                                 public static String BuildRegex (){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              String regex = BuildRegex();
                                                                                                                                                                                                                                                                                                                                                                                                                                      String BA = "(b" + A + ")";

String DA = "(d" + A + ")";

String IA = "(1" + A + ")";
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      return "^" + sentence + "$";
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   String sentence = "";
                                                                                                                                                                                                                                                                                                                        String A = "([aeiou])";
import java.util.regex.*;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   preds + ")";
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     while (true) {
                                                                                      public class LogLan {
```

Primes.cc 29/31

```
largest prime smaller than 10000000 is 9999991.
                                                                                                                                                                                                 smaller than 1000000 is 999991.
smaller than 1000000 is 999983.
                                                                                       smaller than 10000 is 9973.
                                                                                                                                                                           The largest prime smaller than 10 is 7.

The largest prime smaller than 1000 is 97.

The largest prime smaller than 10000 is 997.

The largest prime smaller than 100000 is 999

The largest prime smaller than 1000000 is 99

The largest prime smaller than 1000000 is 99
                                                                                                                                                                                       smaller than 1000 is 997.
                                                                                       677
127
127
1257
2257
3331
4467
467
767
797
877
877
                                                             if (!(x%i) || !(x%(i+2))) return false;
                                                                                       13
61
1113
1181
1251
2251
3397
3463
3463
701
787
787
// O(sqrt(x)) Exhaustive Primality Test
                                   if(x<=3) return true;
if (!(x$2) || !(x$3)) return false;
LL s=(LL)(sqrt((double)(x))+EPS);</pre>
                                                                                       }
// Primes less than 1000:
                               if(x<=1) return false;
                    bool IsPrimeSlow (LL x)
                                                   for (LL i=5;i<=s;i+=6)
                                                                                       typedef long long LL;
     #include <cmath>
#define EPS le-7
                                                                       return true;
```

KMP.cpp 30/31

```
Searches for the string w in the string s (of length k). Returns the 0-based index of the first match (k if no match is found). Algorithm
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           if(w(i-1) == w(j)) \ \{ \ t(i) = \ j+1; \ i++; \ j++; \ \} else if(j > 0) j = t(j); else { t(i) = 0; i++; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                if(i == w.length()) return m;
                                                                                                                                                                                                                                                                                                                                               void buildTable(string& w, VI& t)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            int KMP(string& s, string& w)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       buildTable(w, t);
while(m+i < s.length())</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               m += i-t[i];
if(i > 0) i = t[i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     while(i < w.length())</pre>
                                                                                                                                                                                                                                                                                              typedef vector<int> VI;
                                                                                                                                                                                                                                                                                                                                                                                                                         int i = 2, j = 0;

t[0] = -1; t[1] = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   if(w[i] == s[m+i])
                                                                                                                                                                                                                                                                                                                                                                                                t = VI(w.length());
                                                                                                                                                                                                                                          using namespace std;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           int m = 0, i = 0;
                                                                                                                                     #include <iostream>
                                                         runs in O(k) time.
                                                                                                                                                                   #include <string>
                                                                                                                                                                                         #include <vector>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   else
```

```
int main()

string a = (string) "The example above illustrates the general technique for assembling "+
    "the table with a minimum of fuss. The principle is that of the overall search: "+
    "most of the work was already done in getting to the current position, so very "+
    "little needs to be done in leaving it. The only minor complication is that the "+
    "logic which is correct late in the string erroneously gives non-proper "+
    "substrings at the beginning. This necessitates some initialization code.";

string b = "table";

int p = KMP(a, b);

cout << p << ": " << a.substr(p, b.length()) << " " << b << endl;
}</pre>
```

EmacsSettings.txt 31/31

```
(global-set-key "\C-x(-p" (lambda() (interactive) (other-window -1)) ) (global-set-key "\C-x(-p" (lambda() (interactive) (other-window) (global-set-key "\C-x(-p" other-window) (global-set-key "\C-x(-p" other-window) (global-set-key "\M-y" end-of-buffer) (global-set-key "\M-y" 'peginning-of-buffer) (global-set-key "\M-y" 'goto-line) (global-set-key "\M-y" 'compare-windows) (tool-bar-mode 0) (scoll-bar-mode 1) (slobal-font-lock-mode 1) (slobal-font-lock-mode 1) (slobal-font-lock-mode 1) (slobal-font-winde 1) (custom-set-wariables '(compare-ignore-whitespace t) )
```

Generated by GNU enscript 1.6.1.