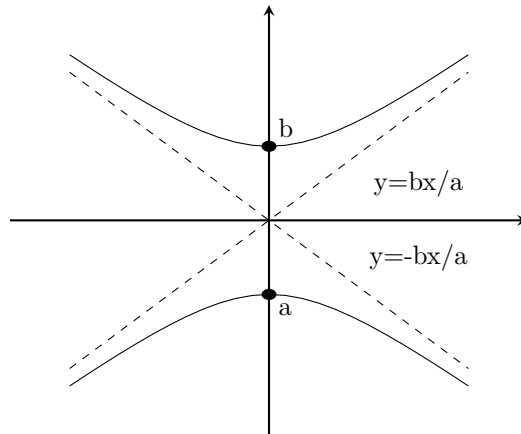


**EXAMPLE** Find the area between the branches of the hyperbola  $y^2 - x^2 = 4$  for  $0 \leq x \leq 1$ .

$$\Rightarrow y^2 = 4 + x^2 = \begin{cases} \sqrt{x^2 + 4} & \text{for } y < 0 \\ -\sqrt{x^2 + 4} & \text{for } y \geq 0 \end{cases} = \begin{cases} x = a \sinh t \\ y = a \cosh t \end{cases}$$

General hyperbola:  $y^2/b^2 - x^2/a^2 = 1$



And we could solve this by parameterizing the equation or using a substitution. Both hyperbolic.

We are definitely going to be expected to know hyperbolic properties, such as  $\sinh 2t = 2 \sinh t \cosh t$ . These are similar to their trigonometric counterparts.