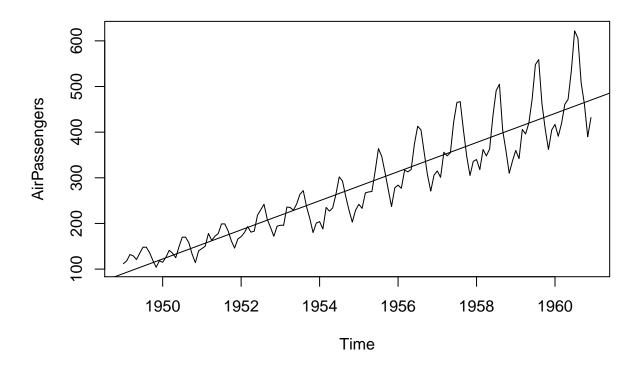
ARIMA

$pranit\ shinde$

10 December 2018

Time series ARIMA(Auto Regressive Integrated Moving Average)

```
data("AirPassengers")
plot(AirPassengers)
summary(AirPassengers)
                               Mean 3rd Qu.
##
      Min. 1st Qu.
                    Median
                                                Max.
##
     104.0
             180.0
                      265.5
                              280.3
                                      360.5
                                               622.0
abline(reg = lm(AirPassengers ~ time(AirPassengers)))
```



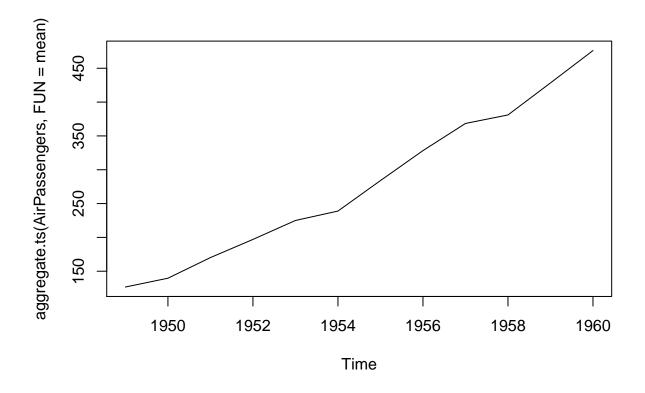
the mean for the above plot is not constant, the variance mapped using creast and troughs is also not same above and below the regression line

```
class(AirPassengers)
```

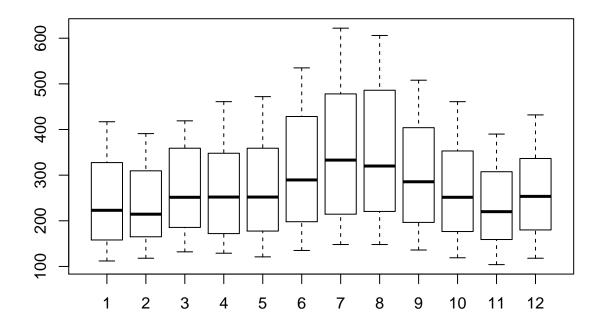
[1] "ts"

```
start(AirPassengers) # start of the time series
## [1] 1949
end(AirPassengers) # end of the time series
## [1] 1960
             12
frequency(AirPassengers) # cycle of the time series is 12 month a year
## [1] 12
summary(AirPassengers) # the no of passengers are distributed across the spectrum
     Min. 1st Qu. Median
                            Mean 3rd Qu.
##
                                            Max.
                   265.5
##
    104.0
           180.0
                           280.3
                                   360.5
                                           622.0
cycle(AirPassengers) ## this print the cycle across year
##
       Jan Feb Mar Apr May Jun Jul Aug Sep Oct Nov Dec
                            6
                                7
## 1949
        1
             2
                 3
                     4
                        5
                                    8
                                        9 10 11 12
             2
                        5
## 1950 1
                 3
                     4
                            6
                                7
                                    8
                                        9 10 11 12
```

```
## 1951
      1
          2
            3 4
                   5
                      6
                        7
                            8
                               9 10 11 12
## 1952
      1
          2
            3
               4
                   5
                      6
                        7
                            8
                               9 10 11 12
      1
          2
            3
               4
                   5
                        7
## 1953
                      6
                            8
                              9 10 11 12
## 1954
          2
            3 4
                   5
                        7
                              9 10 11 12
                            8
## 1955
          2
            3 4
                   5
                      6
                        7
                            8
                              9 10 11 12
      1
      1
          2
            3
               4
                   5
                        7
                              9 10 11 12
## 1956
                      6
                            8
## 1957
      1 2
            3 4
                  5
                     6 7
                            8 9 10 11 12
## 1958
      1 2
            3 4
                  5
                     6 7
                            8 9 10 11 12
## 1959
         2
            3 4
                   5
                     6 7
                            8 9 10 11 12
      1
## 1960
                   5
                            8 9 10 11 12
```

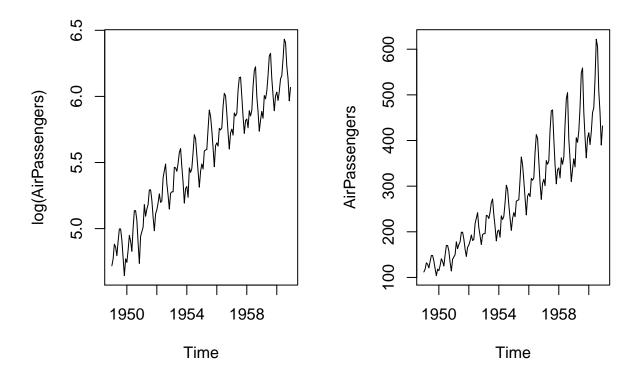


boxplot(AirPassengers ~ cycle(AirPassengers))



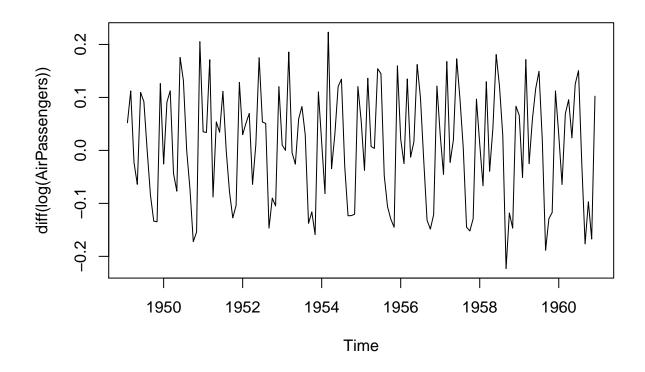
To make sure that the variance is constant through time series, we take log of the data

```
par(mfrow = c(1,2))
plot(log(AirPassengers))
plot(AirPassengers)
```

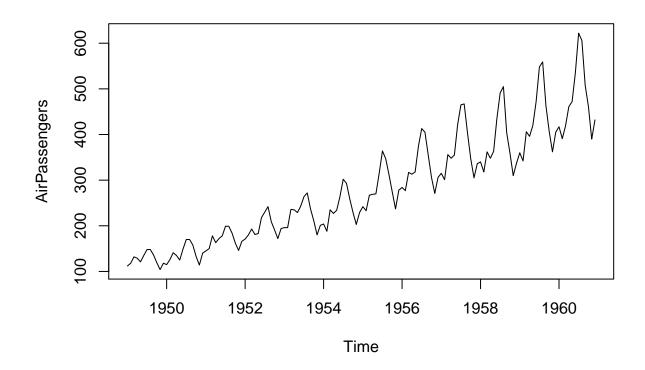


To make sure that the mean is constant through the time series , we take the derivative of the \log of data

```
plot(diff(log(AirPassengers))) # constant mean around zero
```



plot(AirPassengers)



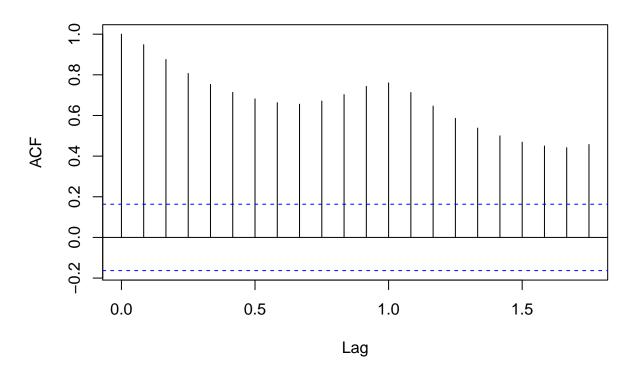
AR I MA

p d q

p, d and q are three parameters r that are used to build a time series model using $\ensuremath{\mathsf{ARIMA}}$

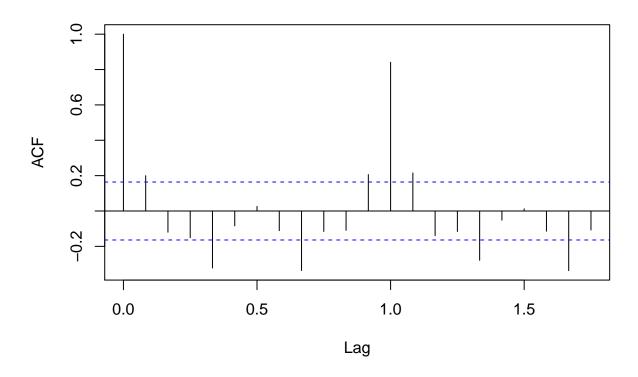
acf(AirPassengers) ## acf function to be directly applied if the time series is stationary

Series AirPassengers



acf(diff(log(AirPassengers))) ## acf function to be applied after transformation, if the series is

Series diff(log(AirPassengers))

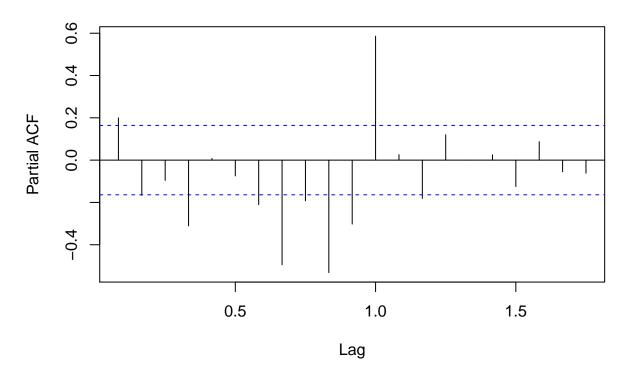


 $\mbox{\tt \#\#}$ not statinary , this determine the value of q.

Interpretaion : The line that get inverted , the index of the line just before that is ${\bf q}$:in our case line is 1 hence ${\bf q}$ is 1

pacf(diff(log(AirPassengers)))

Series diff(log(AirPassengers))



Interpretation: p is one line before the line that gets invented, here the # function that is used to generate this graph is called auto correlation # function'; in our case the value of p is 0 # value od d: d determines the number of times you do differentiation to # stationarize the time series, in our case we did differentiation just once # hence d will be 1.

lets fit the ARIMA model and predict the next 10 years

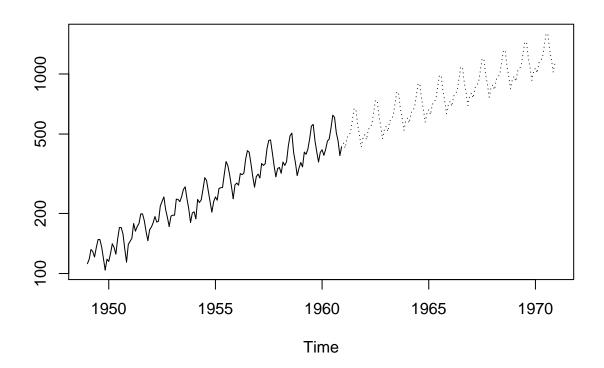
prediction are in the log form , hence to convert to them to decimal interpretable values

we use the shown formula, the value of e is 2.718

```
par(mfrow= c(1,1))
```

plotting the model

```
ts.plot(AirPassengers, 2.718 ^ pred$pred, log = "y", lty= c(1,3))
```



tesing the model

[1] 419 399 466 454 473 547 622 630 526 462 406 452

```
original_1960
```

[1] 417 391 419 461 472 535 622 606 508 461 390 432