

# Artificial Intelligence Lecture 6: Introduction to Reinforcement Learning

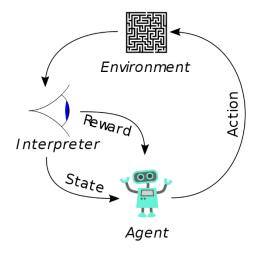
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## What is Reinforcement Learning?

 Reinforcement Learning (RL) is focused on goal-directed learning from interaction



- RL is learning what to do how to map situations to actions – so as to maximize a numerical reward signal
  - The learner is not told which actions to take: it must discover which actions yield the most reward by trying them
  - Typically, actions may affect not only immediate reward but also the next situation and subsequent rewards
- The exploration-exploitation tradeoff
  - Agent must prefer actions that it knows to be effective exploit
  - But to discover such actions, it has to try actions not selected before explore

## RL vs (Un)Supervised Learning

- Different from supervised learning
  - In interactive problems it is impractical to obtain examples of desired behavior
  - In uncharted territory, an agent must learn from its own experience
- Different from unsupervised learning
  - RL is trying to maximize a reward signal, not trying to find hidden structure in collections of unlabeled data
- RL explicitly considers the whole problem of a goal-directed agent interacting with an uncertain environment
  - Creating a behavior model while applying it in the environment
- RL is the closest form of ML to the kind of learning humans do

## **Learning to Play Tic-Tac-Toe**

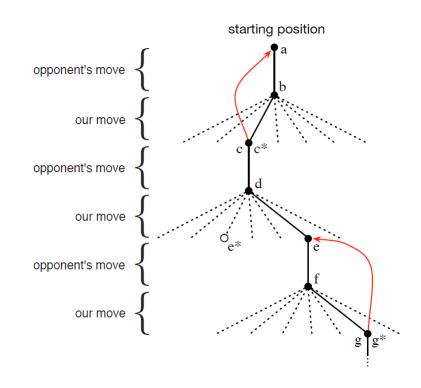
- Rule-based approach
  - Need to hardcode rules for each possible situations that might arise in a game

X	0	0
0	X	X
		Х

- Minimax
  - Assumes a particular way of playing by the opponent
- Dynamic programming can compute an optimal solution for any opponent
  - But requires as input a complete specification of that opponent (state/action probabilities)
- Can we obtain such information from experience?
  - Play many games against the opponent!

## **Learning to Play Tic-Tac-Toe**

- States
  - Possible configurations of the board
- Actions
  - Possible moves to make
- Policy
  - Which action should I play in each state?
- Reward
  - How good was the chosen action?



## **Elements of RL**

#### • Policy $\pi$

- How should the agent behave over time?
- A policy is a (possibly stochastic) mapping from perceived states to actions

#### Reward signal r

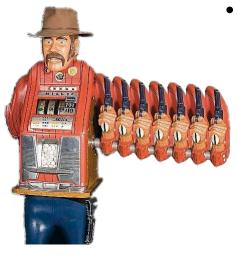
- Defines the goal of the RL problem
- On each time step, the environment sends a reward to the RL agent the agent's goal is to maximize the total reward received over the long run

#### • Value function v

- Specifies what is good in the long run
- The value of a state is the total amount of reward an agent can expect to accumulate from that state onwards (it takes into account future rewards)
- →We seek actions that bring about states of highest value, not highest reward, because these actions obtain the greatest amount of reward over the long run

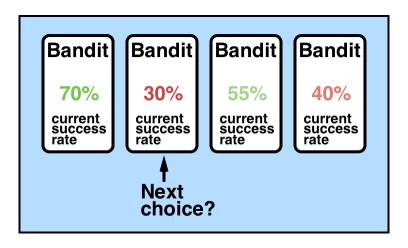
#### **Bandit Problems**

A simple setting with a single state



- K-armed bandit problem
  - There are k different actions
  - After each action a numerical reward is received from a stationary probability distribution
  - Each action has a *value* its expected or mean reward, not known by the agent:  $q_*(a) \doteq \mathbb{E}[R_t | A_t = a]$
  - The agent *estimates*, at time step t, the value of an action a:  $Q_t(a)$

#### **Bandit Problems**



- Selecting greedy actions (whose estimated value is greatest): exploiting
- Selecting non-greedy actions: exploring
  - Improve estimates of non-greedy actions' value
- Lower reward in the short run (during exploration), but higher in the long run after discovering the best actions, we can exploit them many times

## **Estimating Action Values**

Sample average:

$$Q_t(a) \doteq \frac{\sum_{i=1}^{t-1} R_i \cdot 1_{A_i = a}}{\sum_{i=1}^{t-1} 1_{A_i = a}}$$

Update rule:

$$Q_{n+1} = Q_n + \frac{1}{n} [R_n - Q_n]$$

 $NewEstimate \leftarrow OldEstimate + StepSize[Target - OldEstimate]$ 

- The target indicates a desirable direction in which to move
- The step-size parameter changes from time step to time step
- Giving more weight to recent rewards constant step-size parameter:

$$Q_{n+1} \doteq Q_n + \alpha [R_n - Q_n]$$

where  $\alpha \in (0,1]$ 

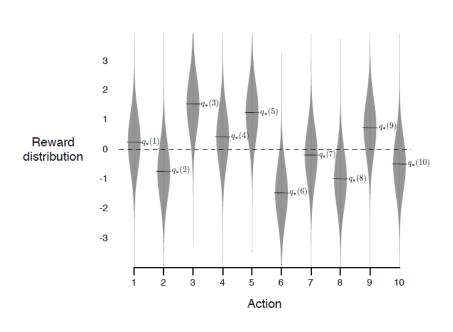
#### **Action Selection**

- Greedy action selection (always exploits):  $A_t \doteq \underset{a}{\operatorname{argmax}} Q_t(a)$
- $\varepsilon$ -greedy action selection: behave greedily most of the time, but with small probability  $\varepsilon$  select randomly from among all the actions
  - $Q_t(a)$  will converge to  $q_*(a)$  if a is selected sufficiently often
- Soft-max action selection (Boltzmann distribution):

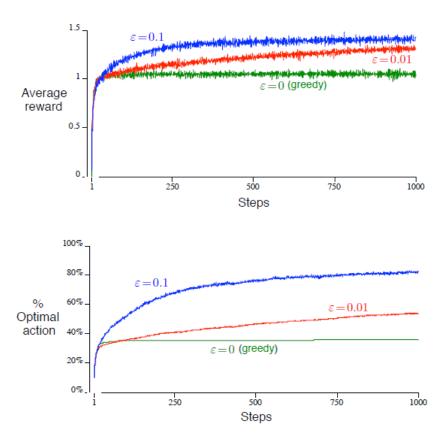
$$\Pr\{A_t = a\} \doteq \frac{e^{Q_t(a)/\tau}}{\sum_{b=1}^k e^{Q_t(b)/\tau}}$$

where  $\tau$  is a temperature parameter: if high, actions will tend to be equiprobable; if low, action values matter more; if  $\tau \to 0$ , then we have greedy action selection

## The 10-armed Testbed



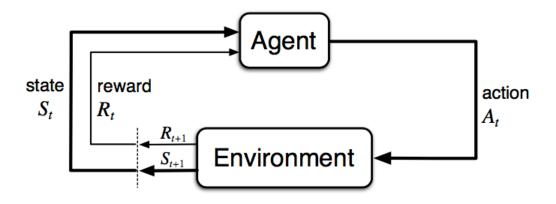
#### averages over 2000 runs



#### **Markov Decision Processes**

- In the general setting we have many states
- Markov Decision Processes (MDP) are a classical formalization of sequential decision making
  - Actions influence not just immediate rewards, but also subsequent situations (states) and thus future rewards
- In a finite MDP, there is a finite number of states, actions and rewards
- In MDPs we estimate the value  $q_*(s, a)$

## **Agent-Environment Interface**



• Dynamics of the MDP:

$$p(s', r|s, a) \doteq \Pr\{S_t = s', R_t = r \mid S_{t-1} = s, A_{t-1} = a\}$$

- The probability of each possible value for s' and r depends only in the immediately preceding state s and action a
- The state must include all relevant information about the past agent-environment interaction Markov property

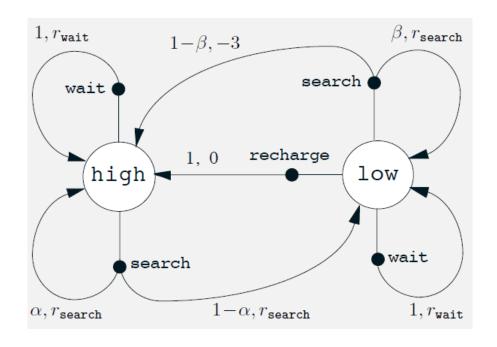
## **Example: Recycling Robot**

- A robot has to decide whether it should (1) actively search for a soda can, (2) wait for someone to bring it a can, or (3) go to home base and recharge
- Searching is better (higher probability of getting a can) but runs down battery; if out of battery, the robot has to be rescued
- Decisions made on the basis of current energy level: high, low
- Reward is zero except when getting a can, and negative if out of battery

$$\mathcal{S} = \{high, low\}$$
 $\mathcal{A}(high) = \{search, wait\}$ 
 $\mathcal{A}(low) = \{search, wait, recharge\}$ 
 $r_{search} > r_{wait}$ 

s	a	s'	p(s' s,a)	r(s, a, s')
high	search	high	$\alpha$	$r_{ t search}$
high	search	low	$1-\alpha$	$r_{ t search}$
low	search	high	$1-\beta$	-3
low	search	low	$\beta$	$r_{ t search}$
high	wait	high	1	$r_{\mathtt{Wait}}$
high	wait	low	0	-
low	wait	high	0	-
low	wait	low	1	rwait
low	recharge	high	1	0
low	recharge	low	0	-

## **Example: Recycling Robot**



#### **Goals and Rewards**

- A reward signal is used to define the goal of the agent
  - Learning to walk: reward proportional to the robot's forward motion
  - Learning to Escape from a maze: reward -1 for any state prior to escape (encourage escaping as quickly as possible)
  - Learning to find empty cans for recycling: reward of 0 most of the time, +1 for each can collected
  - Learning to play checkers or chess: reward +1 for winning, -1 for losing, and 0 for drawing and nonterminal positions
- Provide rewards in such a way that by maximizing them the agent will also achieve our goal
  - The agent's goal is to maximize the cumulative reward it receives in the long run
- →The reward signal is a way of communicating to the robot what you want it to achieve, not how

## **Returns and Episodes**

Agent wants to maximize expected return

$$G_t \doteq R_{t+1} + R_{t+2} + R_{t+3} + \dots + R_T$$

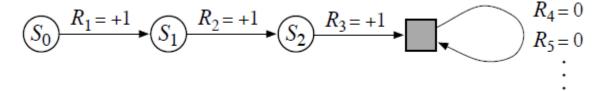
- Episodic tasks: when the agent-environment interaction breaks naturally into subsequences – episodes
  - From a starting state to a terminal state
  - Followed by a reset to another starting state, chosen independently of how the previous episode ended
- Continuing tasks do not break naturally into identifiable episodes (e.g., on-going process-control)
  - Problem with calculating G<sub>t</sub>:
    - $T=\infty$
    - $G_t$  could also be infinite (if rewards are positive at each time step)

## **Returns and Episodes**

Adding discounting: agent wants to maximize expected discounted return

$$G_t \doteq R_{t+1} + \gamma R_{t+2} + \gamma^2 R_{t+3} + \dots = \sum_{k=0}^{\infty} \gamma^k R_{t+k+1}$$
 
$$G_t \doteq R_{t+1} + \gamma G_{t+1}$$

- $0 \le \gamma \le 1$  is the discount rate
  - If  $\gamma = 0$  the agent is "myopic" (only immediate reward matters)
  - As  $\gamma$  approaches 1, the agent becomes more farsighted (strongly considers future rewards)
- $G_t$  is now finite, even if summing an infinite number of terms
- Applicable also to episodic tasks, if we consider a final absorbing state:



## **Example: Pole Balancing**

- Move a cart so as to keep a pole from falling over
  - Failure if the pole falls past a given angle or if the cart runs off the track
  - The pole is reset to vertical after each failure



- Episodic task: reward +1 except when failure
  - return is the number of steps until failure
- Continuing task, using discounting: reward –1 on each failure and 0 otherwise
  - return is  $-\gamma^K$ , where K is the number of steps before failure

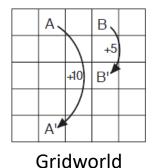
## **Policies and Value Functions**

- RL algorithms involve estimating value functions
  - How good (in terms of expected return) is it to be in a given state?
  - How good is it to perform a given action in a given state?
- Future rewards depend on the choice of actions
  - Value functions are defined with respect to policies (ways of acting)
- Policy: a mapping from states to probabilities of selecting each possible action
  - $\pi(a|s) = \Pr(A_t = a|S_t = s)$

 $\rightarrow$ RL methods specify how the policy (*i.e.*, the probability distribution over  $a \in \mathcal{A}(s)$  for each  $s \in \mathcal{S}$ ) is changed with experience

#### **Policies and Value Functions**

- State-value function  $v_{\pi}(s)$ 
  - Expected return when starting in s and following  $\pi$  thereafter
  - $v_{\pi}(s) \doteq \mathbb{E}_{\pi}[G_t|S_t = s]$  (Bellman equation)
- Action-value function  $q_{\pi}(s, a)$ 
  - Expected return when taking action  $\alpha$  in state s, and following  $\pi$  thereafter
  - $q_{\pi}(s,a) \doteq \mathbb{E}_{\pi}[G_t|S_t = s, A_t = a]$
- The value functions  $v_{\pi}$  and  $q_{\pi}$  can be estimated from experience
- Example: using a random policy, with  $\gamma = 0.9$ :





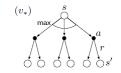
- Off-grid actions have no effect, with r=-1
- Any action from A gets to A', with r = +10
- Any action from B gets to B', with r = +5

3.3	8.8	4.4	5.3	1.5
1.5	3.0	2.3	1.9	0.5
0.1	0.7	0.7	0.4	-0.4
-1.0	-0.4	-0.4	-0.6	-1.2
-1.9	-1.3	-1.2	-1.4	-2.0

 $v_{\pi}$ 

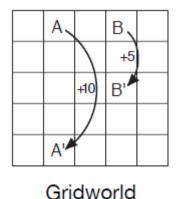
## **Optimal Policy and Value Function**

- Optimal policy  $\pi_*$ : expected return is greater than any other policy
  - Optimal state-value function:  $v_*(s) \doteq \max_{\pi} v_{\pi}(s)$
  - Optimal action-value function:  $q_*(s, a) \doteq \max_{\pi} q_{\pi}(s, a)$



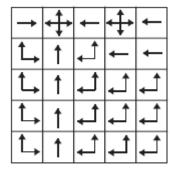


- Once we know  $v_*$  or  $q_*$ , the optimal policy is greedy
- Example:





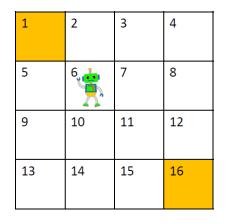
22.0	24.4	22.0	19.4	17.5
19.8	22.0	19.8	17.8	16.0
17.8	19.8	17.8	16.0	14.4
16.0	17.8	16.0	14.4	13.0
14.4	16.0	14.4	13.0	11.7



 $v_*$ 

 $\pi_*$ 

## **Example Grid World**





- A bot is required to traverse a grid of 4×4 dimensions to reach its goal (1 or 16)
- There are 2 terminal states (1 and 16) and 14 non-terminal states (2 to 15)
- Each step is associated with a reward of -1
- Consider a random policy: at every state, the probability of every action {up, down, left, right} is 0.25
- Initialize  $v_1$  for the random policy with all 0s

# **Example Grid World: Policy Evaluation**

Turning Bellman equation into an update:

$$v_{k+1}(s) \doteq \mathbb{E}_{\pi}[R_{t+1} + \gamma v_k(S_{t+1}) | S_t = s]$$

1	2	3	4
5	6	7	8
9	10	11	12
13	14	15	16

$$v_{1}(6) = \sum_{a \in \{u,d,l,r\}} \pi(a|6) \sum_{s',r} p(s',r|6,a)[r + \gamma v_{0}(s')]$$

$$= \sum_{a \in \{u,d,l,r\}} \pi(a|6) \sum_{s'} p(s'|6,a)[r + \gamma v_{0}(s')]$$

$$= 0.25 * \{-p(2|6,u) - p(10|6,d) - p(5|6,l) - p(7|6,r)\}$$

$$= 0.25 * \{-1 - 1 - 1 - 1\}$$

$$= -1$$

$$\Rightarrow v_{1}(6) = -1$$

- For non-terminal states,  $v_1(s) = -1$
- For terminal states, p(s'|s,a) = 0

• 
$$v_k(1) = v_k(16) = 0$$
, for all  $k$ 

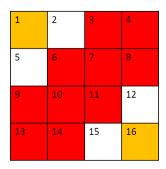
$$\nu_1 = \begin{bmatrix}
0.0 & -1.0 & -1.0 & -1.0 \\
-1.0 & -1.0 & -1.0 & -1.0
\end{bmatrix}$$
 $-1.0 & -1.0 & -1.0 & -1.0$ 
 $-1.0 & -1.0 & -1.0 & 0.0$ 

# **Example Grid World: Policy Evaluation**

• Step 2, with discount factor  $\gamma = 1$ 

$$\begin{split} v_2(6) &= \sum_{a \in \{u,d,l,r\}} \pi(a|6) \sum_{s'} p(s'|6,a) \underbrace{[r + \gamma v_1(s')]}_{=-1} &= \begin{cases} -1, s' \in S \\ 0, s' \in S^+ \setminus S \end{cases} \\ &= 0.25 * \{p(2|6,u)[-1 - \gamma] + p(10|6,d)[-1 - \gamma] \\ &+ p(5|6,l)[-1 - \gamma] + p(7|6,r)[-1 - \gamma] \} \\ &= 0.25 * \{-2 - 2 - 2 - 2\} \\ &= -2 \end{split}$$

• For all red states,  $v_2(s) = -2$ 



• For the other states (2, 5, 12, 15):

$$v_{2}(2) = \sum_{a \in \{u,d,l,r\}} \pi(a|2) \sum_{s'} p(s'|2,a) \underbrace{[r + \gamma v_{1}(s')]}_{= -1} = \begin{cases} -1, s' \in S \\ 0, s' \in S^{+} \setminus S \end{cases}$$

$$= 0.25 * \{p(2|2,u)[-1-\gamma] + p(6|2,d)[-1-\gamma] + p(1|2,l)[-1-\gamma*0] + p(3|2,r)[-1-\gamma]\}$$

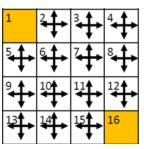
$$= 0.25 * \{-2-2-1-2\}$$

$$= -1.75$$

$$\Rightarrow v_{2}(2) = -1.75$$

$$v_2 = \begin{bmatrix} 0.0 & -1.7 & -2.0 & -2.0 \\ -1.7 & -2.0 & -2.0 & -2.0 \\ -2.0 & -2.0 & -2.0 & -1.7 \\ -2.0 & -2.0 & -1.7 & 0.0 \end{bmatrix}$$

## **Example Grid World: Policy Evaluation**



Random policy

k = 0				
0.0	0.0	0.0	0.0	
0.0	0.0	0.0	0.0	
0.0	0.0	0.0	0.0	
0.0	0.0	0.0	0.0	

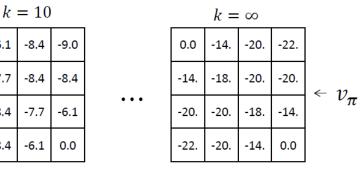
$$k = 1$$

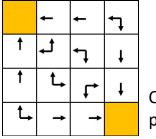
$$\begin{array}{c|ccccc}
0.0 & -1.0 & -1.0 & -1.0 \\
-1.0 & -1.0 & -1.0 & -1.0 \\
-1.0 & -1.0 & -1.0 & -1.0 \\
-1.0 & -1.0 & -1.0 & 0.0
\end{array}$$

$$k = 1$$
  $k = 2$ 

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$$k = 3$$
0.0 -2.4 -2.9 -3.0
-2.4 -2.9 -3.0 -2.9
-2.9 -3.0 -2.9 -2.4
-3.0 -2.9 -2.4 0.0





Optimal policy

## **Approximation**

- Optimal policies are computationally costly to find we can only approximate
  - In tasks with small, finite state sets: tabular methods
  - Otherwise: function approximation using a more compact parameterized function representation (e.g. using neural networks)

→The online nature of RL allows us to put more effort into learning to make decisions for frequently encountered states

## **Temporal-Difference Learning**

- TD methods update estimates based on immediately observed reward and state
- Update rule:

$$V(S_t) \leftarrow V(S_t) + \alpha [R_{t+1} + \gamma V(S_{t+1}) - V(S_t)]$$

Because TD bases its update in part on an existing estimate, it is a bootstrapping

method

```
Input: the policy \pi to be evaluated Algorithm parameter: step size \alpha \in (0,1] Initialize V(s), for all s \in \mathbb{S}^+, arbitrarily except that V(terminal) = 0 Loop for each episode:

Initialize S
Loop for each step of episode:

A \leftarrow \text{action given by } \pi \text{ for } S
Take action A, observe R, S'
V(S) \leftarrow V(S) + \alpha [R + \gamma V(S') - V(S)]
S \leftarrow S'
until S is terminal
```

## **Temporal-Difference Learning**

- TD vs Dynamic Programming methods
  - TD methods do not require a model of the environment's dynamics (rewards and next-state probability distributions)
- TD vs Monte Carlo methods
  - TD methods are naturally implemented in an online, fully incremental fashion, while MC methods must wait until the end of an episode
    - Useful if episodes are very long, or in continuing tasks (that have no episodes at all)
- Usually, TD methods converge faster than MC methods on stochastic tasks

## Sarsa: On-policy TD Control



Update rule:

$$Q(S_t, A_t) \leftarrow Q(S_t, A_t) + \alpha [R_{t+1} + \gamma Q(S_{t+1}, A_{t+1}) - Q(S_t, A_t)]$$

• This rule uses every element of the quintuple of events  $(S_t, A_t, R_{t+1}, S_{t+1}, A_{t+1})$ 

```
Sarsa (on-policy TD control) for estimating Q \approx q_*

Algorithm parameters: step size \alpha \in (0,1], small \varepsilon > 0
Initialize Q(s,a), for all s \in \mathbb{S}^+, a \in \mathcal{A}(s), arbitrarily except that Q(terminal,\cdot) = 0
Loop for each episode:
Initialize S
Choose A from S using policy derived from Q (e.g., \varepsilon-greedy)
Loop for each step of episode:
Take action A, observe R, S'
Choose A' from S' using policy derived from Q (e.g., \varepsilon-greedy)
Q(S,A) \leftarrow Q(S,A) + \alpha \left[R + \gamma Q(S',A') - Q(S,A)\right]
S \leftarrow S'; A \leftarrow A';
until S is terminal
```



• Converges to optimal policy and action-value function if all state-action pairs are visited infinitely and policy converges to greedy (e.g. using  $\varepsilon$ -greedy with  $\varepsilon = 1/t$ )

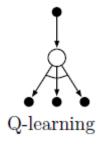
## **Q-learning: Off-policy TD Control**

Update rule:

$$Q(S_t, A_t) \leftarrow Q(S_t, A_t) + \alpha \left[ R_{t+1} + \gamma \max_{a} Q(S_{t+1}, a) - Q(S_t, A_t) \right]$$

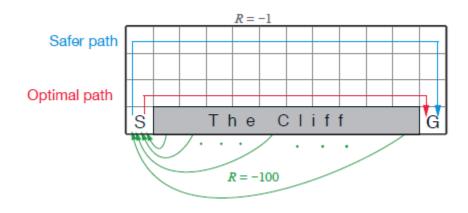
```
Q-learning (off-policy TD control) for estimating \pi \approx \pi_*

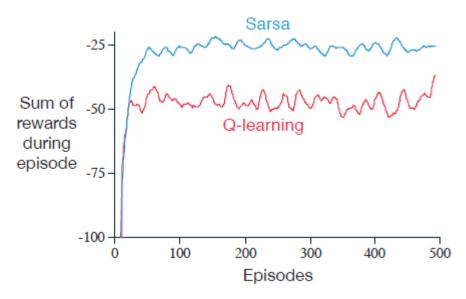
Algorithm parameters: step size \alpha \in (0,1], small \varepsilon > 0
Initialize Q(s,a), for all s \in \mathbb{S}^+, a \in \mathcal{A}(s), arbitrarily except that Q(terminal, \cdot) = 0
Loop for each episode:
Initialize S
Loop for each step of episode:
Choose A from S using policy derived from Q (e.g., \varepsilon-greedy)
Take action A, observe R, S'
Q(S,A) \leftarrow Q(S,A) + \alpha [R + \gamma \max_a Q(S',a) - Q(S,A)]
S \leftarrow S'
until S is terminal
```



• The learned action-value function Q directly approximates  $q_{st}$ , independently of the policy being followed

## **Example: Cliff Walking**





- Sarsa and Q-learning with  $\varepsilon$ -greedy action selection ( $\varepsilon=0.1$ )
  - Q-learning learns values for the optimal policy
  - Sarsa takes action selection into account and learns the longer but safer path
  - Given exploration, Q-learning occasionally falls off the cliff, hence the lower online performance
- If  $\varepsilon$  is gradually reduced, both methods converge to the optimal policy

# **Quiz: The Toothpick Game**

- 10 toothpicks
- 2 players take 1, 2 or 3 in turn
- Avoid last toothpick

• 
$$r(0) = +1$$

$$r(1) = -1$$

• 
$$r(0) = +1$$
  $r(1) = -1$   $r(n) = 0, n > 1$ 



- Using Q-learning with  $\alpha = 0.5$  and  $\gamma = 0.9$ , which values of Q(s, a) change in each of the following episodes? (Consider only self-actions, shown in **bold**.)
  - Actions: **2**-1-**2**-3-**1**-1 (States: **10**-8-**7**-5-**2**-1-**0**)



- Actions: 2-2-1-3-1-1 (States: 10-8-6-5-2-1-0)
- Actions: **1**-3-**1**-3-**1**-1 (States: **10**-9-**6**-5-**2**-1-**0**)
- After such updates, does the agent win when starting in state 10 and following a greedy policy, assuming the opponent always takes as much toothpicks as it can?

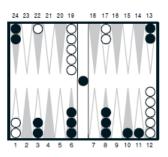
# **RL Algorithms**

Algorithm	Description	Policy	Action Space	State Space
Monte Carlo	Every visit to Monte Carlo	Either	Discrete	Discrete
Q-learning	State-action-reward-state O		Discrete	Discrete
SARSA	State-action-reward-state-action	On-policy	Discrete	Discrete
Q-learning - Lambda	Q-learning with eligibility traces	Off-policy	Discrete	Discrete
SARSA - Lambda	SARSA with eligibility traces	On-policy	Discrete	Discrete
<u>DQN</u> [Mnih et al., 2013]	Deep Q Network	Off-policy	Discrete	Continuous
DDPG [Lillicrap et al., 2016]	Deep Deterministic Policy Gradient	Off-policy	Continuous	Continuous
A3C [Mnih et al., 2016]	Asynchronous Advantage Actor-Critic	On-policy	Continuous	Continuous
NAF [Gu et al., 2016]	Q-Learning with Normalized Advantage Functions	Off-policy	Continuous	Continuous
TRPO [Schulman et al., 2015]	Trust Region Policy Optimization	On-policy	Continuous	Continuous
PPO [Schulman et al., 2017]	Proximal Policy Optimization	On-policy	Continuous	Continuous
TD3 [Fujimoto et al., 2018]	Twin Delayed Deep Deterministic Policy Gradient	Off-policy	Continuous	Continuous
SAC [Haarnoja et al., 2018]	Soft Actor-Critic	Off-policy	Continuous	Continuous

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#### **RL in Games**

- TD-Gammon [Tesauro, 1995]
  - Neural Network trained with self-play reinforcement learning

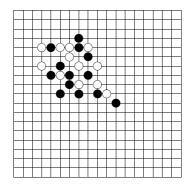


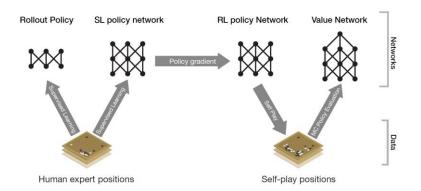
- Atari 2600 Games [DeepMind, 2013]
  - Learn control policies directly from high-dimensional sensory input using reinforcement learning
  - Input is raw pixels and output is a value function estimating future rewards



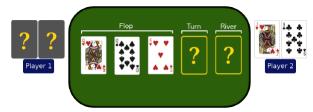
#### **RL in Games**

- AlphaGo [Google DeepMind, 2016]
  - Convolutional Neural Networks trained with human expert data
  - Deep Reinforcement Learning with fictitious self-play



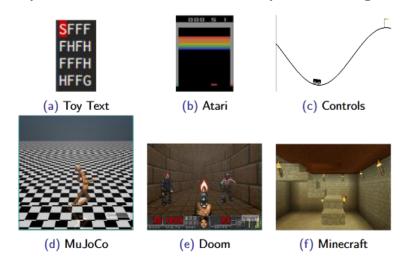


- Poker: Heads-Up Limit Texas Hold'em NFSP [UCL, 2016]
  - Deep Reinforcement Learning with fictitious self-play
  - No prior knowledge



## **OpenAl Gym**

- Gym is a toolkit for developing and comparing reinforcement learning algorithms
- The <u>gym library</u> is a collection of test problems with a shared interface <u>environments</u> — that you can use to work out your RL algorithms

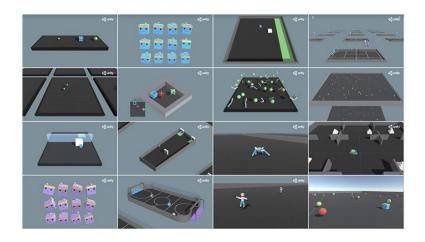


- OpenAl Baselines is a set of high-quality implementations of RL algorithms
  - See also <u>Stable Baselines</u>

## **Unity ML-Agents**

• With Unity Machine Learning Agents (<u>ML-Agents</u>), you teach intelligent agents through a combination of deep reinforcement learning and imitation learning





## **Further Reading**

• Sutton, R. S. and Barto, A. G. (2018). *Reinforcement Learning – An Introduction*, 2<sup>nd</sup> ed., The MIT Press: Chap. 1-3, 6

Simple Tutorial Videos for Deep RL:

Introduction on Reinforcement Learning and Deep RL:

https://www.youtube.com/watch?v=JgvyzlkgxF0

PPO – Proximal Policy Optimization (PPO):

https://www.youtube.com/watch?v=5P7I-xPq8u8

## **Conclusions**

- RL enables to learn intelligent behavior in complex environments
- Large number of algorithms and approaches
- Amazing results in vintage Atari Games
- Stunning results of AlphaGo and AlphaZero
- Very promising results in Robotics
- Very fast evolution in the last few years