

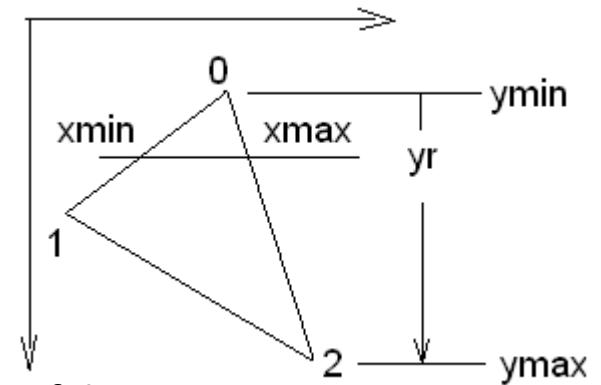
Rasterizarea suprafetelor triunghiulare

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Rasterizarea suprafetelor triunghiulare- algoritmul

Bool SupTri(int x0, int y0, int x1, int y1, int x2, int y2)

- { 1. Se sorteaza varfurile triunghiului crescator dupa coordonata y, a.i. $y_0 = y_{min}$;
- 2. Daca triunghiul este degenerat (varfurile sunt coliniare), return false;
- 3. Se orienteaza conturul in sens trigonometric (0-1-2: sens trigonometric);
- 4. Se calculeaza extremitatile segmentelor interioare suprafeței triunghiului, pentru toate liniile raster de la y_{min} -triunghi la y_{max} -triunghi si se memoreaza in 2 tablouri, XMIN, XMAX;
- 5. Se afiseaza pixelii interiori triunghiului (intre xmin si xmax pe fiecare linie raster);
return true;
- }



Algoritmul: pași 1 și 2

1. Se sortează varfurile triunghiului crescător după coordonata y, a.i. $y_0 = y_{\min}$

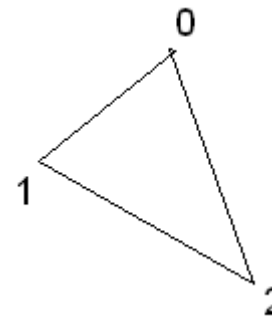
if($y_1 < y_0$) { $t = y_1$; $y_1 = y_0$; $y_0 = t$; }

if($y_2 < y_0$) { $t = y_2$; $y_2 = y_0$; $y_0 = t$; }

2. Dacă triunghiul este degenerat (varfurile sunt coliniare), return false

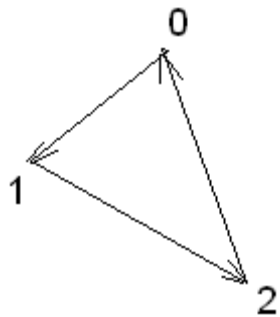
$$\begin{aligned} \det &= \begin{vmatrix} x_1 - x_0 & y_1 - y_0 \\ x_2 - x_0 & y_2 - y_0 \end{vmatrix} \\ &= (x_1 - x_0)(y_2 - y_0) - (x_2 - x_0)(y_1 - y_0) \end{aligned}$$

if($\det == 0$) return false



Pasul 3: orientarea conturului

3. Se orienteaza conturul in sens trigonometric (0-1-2: sens trigonometric)



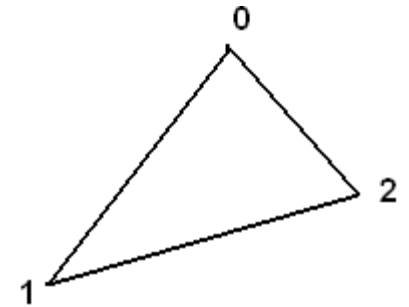
sens trigonometric

$$dx0 = x1 - x0; \quad dx1 = x2 - x0; \quad dy0 = y1 - y0; \quad dy1 = y2 - y0;$$

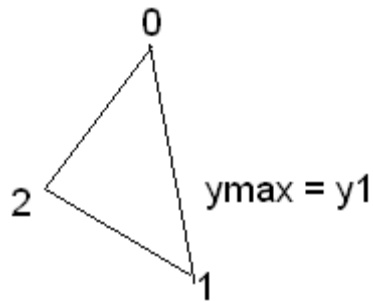
$$x1 < x0, \quad x2 > x0$$

$$dx0 < 0, \quad dx1 > 0, \quad dy0 > 0, \quad dy1 > 0$$

$$\mathbf{det} = dx0 * dy1 - dx1 * dy0 < 0$$



sens trigonometric



sens anti-trigonometric

$$x1 > x0, \quad x2 < x0$$

$$dx0 > 0, \quad dx1 < 0, \quad dy0 > 0, \quad dy1 > 0$$

$$\mathbf{det} = dx0 * dy1 - dx1 * dy0 > 0$$

Se inverseaza varful 1 cu 2

Pasul 4: calculul extremitatilor segmentelor interioare

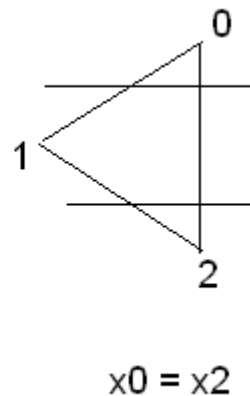
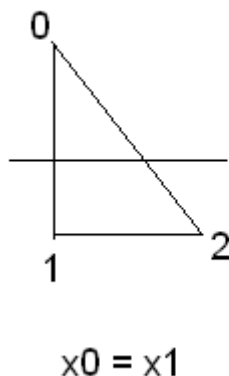
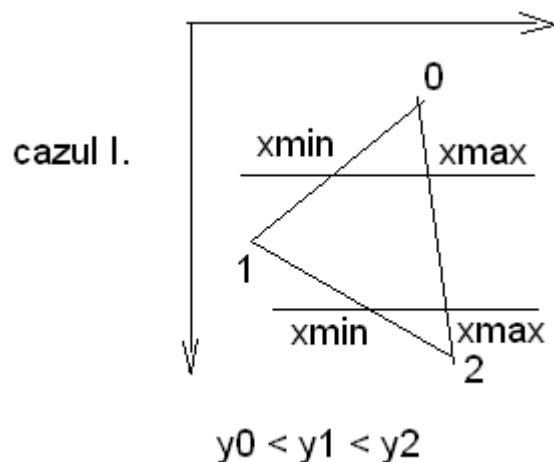
4. Se calculeaza extremitatile segmentelor interioare suprafetei triunghiului

- Coordonatele xmin, xmax ale extremitatilor segmentelor interioare suprafetei triunghiului se memoreaza in 2 tablouri:

`int XMIN[H], XMAX[H]; // H este numarul de linii imagine`

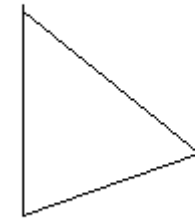
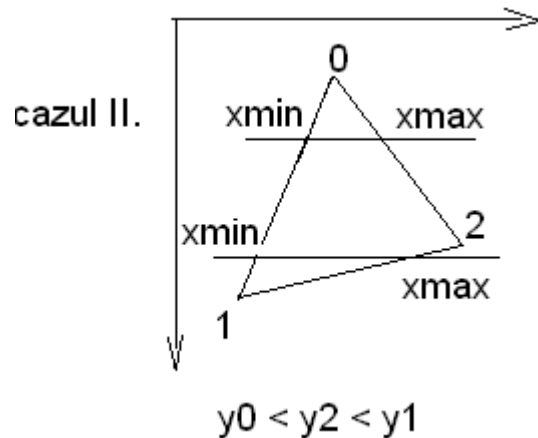
- Calculul extremitatilor este efectuat in functiile **CalculXmin()** si **CalculXmax()**;

Cazuri:

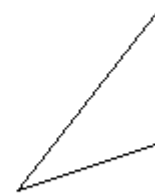


`CalculXmin(x0, y0, x1, y1);`
`CalculXmin(x1, y1, x2, y2);`
`CalculXmax(x0, y0, x2, y2);`

Pasul 4: calculul extremitatilor segmentelor interioare (2)



$x_0 = x_1$

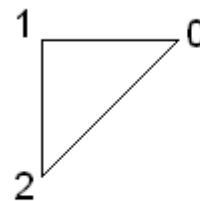
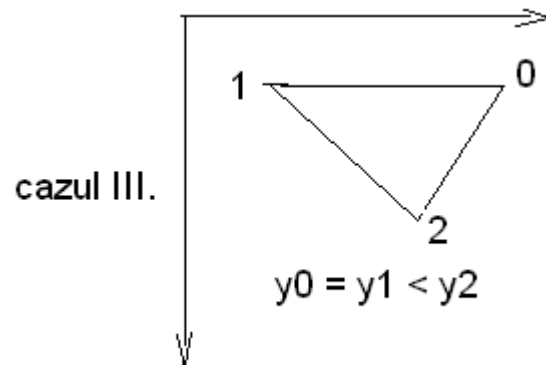


$x_0 = x_2$

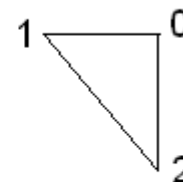
CalculXmin(x_0, y_0, x_1, y_1);

CalculXmax(x_0, y_0, x_2, y_2);

CalculXmax(x_2, y_2, x_1, y_1);



$x_1 = x_2$

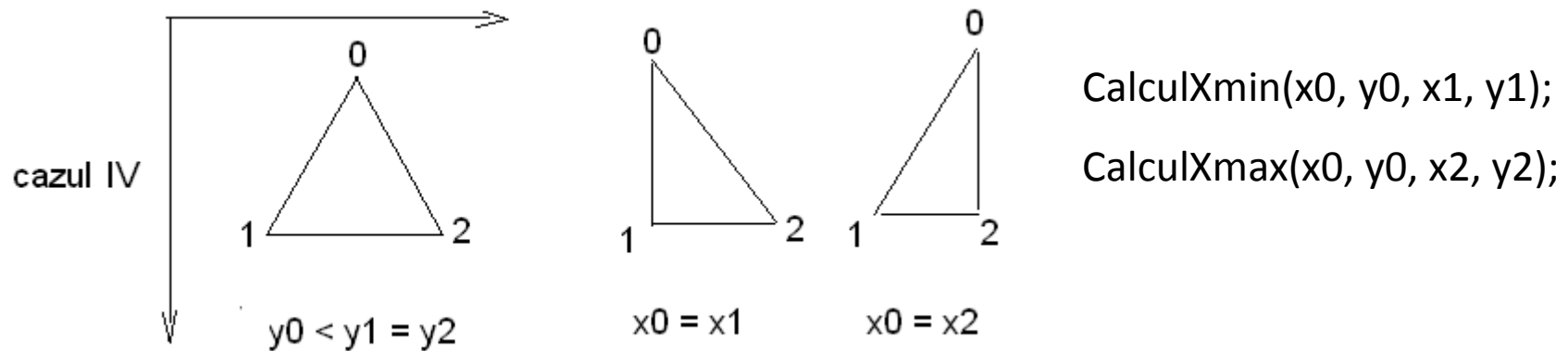


$x_0 = x_2$

CalculXmin(x_1, y_1, x_2, y_2);

CalculXmax(x_0, y_0, x_2, y_2);

Pasul 4: calculul extremitatilor segmentelor interioare (3)



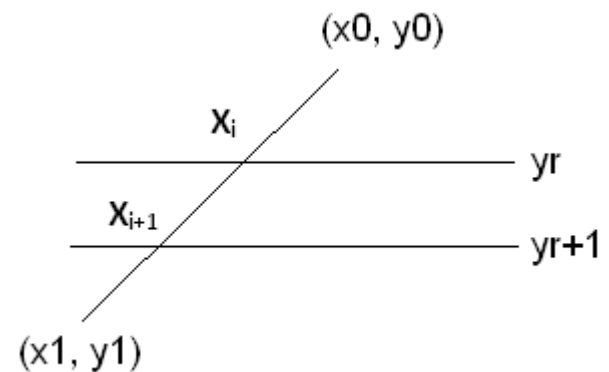
Calculul coordonatelor xmin, xmax

$m = (y_1 - y_0) / (x_1 - x_0)$ - panta laturii

$(y_{r+1} - y_r) / (x_{i+1} - x_i) = m \rightarrow x_{i+1} = x_i + (1/m)$

$dx = 1.0/m$ - constanta a laturii

$x_{i+1} = x_i + dx \rightarrow$ calcul incremental



Pasul 4: calculul extremitatilor segmentelor interioare (4)

```
int XMIN[H], XMAX[H];
```

```
void Calcul Xmin(int x0, int y0, int x1, int y1)
```

```
{ // y0 < y1
```

```
  int y;
```

```
  if( x0==x1)
```

```
    {for(y =y0; y<=y1;y++)
```

```
      XMIN[y] = x0;
```

```
    return;
```

```
  }
```

```
float dx = (float)(x1 - x0) / (y1 - y0);
```

```
XMIN[y0] = x0; XMIN[y1] = x1;
```

```
for(y = y0 +1; y<y1; y++)
```

```
  XMIN[y] = XMIN[y-1] + dx;
```

```
}
```

```
void CalculXmax(int x0, int y0, int x1, int y1)
```

```
{ - similara cu functia CalculXmin
```

```
- memoreaza punctele succesive de pe latură
```

```
in tabloul XMAX
```

```
}
```


Pasul 5: afisarea pixelilor suprafetei triunghiulare

5. Se afiseaza pixelii interiori triunghiului, intre xmin si xmax pe fiecare linie raster

```
ymax = y1; if (y2>y1 )ymax = y2;
```

```
for(int y= y0; y<= ymax; y++)
```

```
    for( int x = XMIN[y]; x <= XMAX[y]; x++)
```

```
        putpixel(x, y, culoare(x,y)); // afisare fragment rezultat din rasterizarea suprafetei
```

```
        // triunghiulare
```

Functia **culoare (int x, int y)** calculeaza culoarea fragmentului care se afiseaza in pixelul (x,y),

tinand cont de:

- sursele de lumina
- proprietatile de material ale suprafetei din care face parte triunghiul
- umbre (fragmentul poate fi in umbra)
- ceata

Functia **culoare (int x, int y)** este implementata in “fragment shader”