CISC 102 (Fall 21) Homework #1: LaTeX (20 Points)

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Question 1

- A) $\{-2, -1, 0, 1, 2\}$
- B) $\{0, 1, 4, 9, 16\}$
- C) Ø

Question 2

- A) There are 18 elements of $A \times B \times C$:
- (1, 1, 1), (1, 1, 2), (1, 1, 3)
- (1, 3, 1), (1, 3, 2), (1, 3, 3)
- (2, 1, 1), (2, 1, 2), (2, 1, 3)
- (2, 3, 1), (2, 3, 2), (2, 3, 3)
- (3, 1, 1), (3, 1, 2), (3, 1, 3)
- (3, 3, 1), (3, 3, 2), (3, 3, 3)
- B) There are 4 elements of $(A \times B) \cap (B \times A)$:
- (1, 1), (1, 3),
- (3, 1), (3, 3)
- C) There are 3 elements of $(A \times A) \setminus (A \times B)$:
- (1, 2), (2, 2), (3, 3)

Question 3

- A) The set $\{x \in \mathbb{N} | x > 10\}$ is infinite.
- B) The set $\{x \in \mathbb{N} | x \le 10\}$ is finite: $|\{x \in \mathbb{N} | x \le 10\}| = 11$
- C) The set $\{4, \{4\}, \{4, \{4\}\}, \{\mathbb{N}\}\}\$ is finite: $|\{4, \{4\}, \{4, \{4\}\}, \{\mathbb{N}\}\}| = 4$

Question 4

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\forall x \{ x \in A \to x \in B \}
\forall x \{ x \in B \to x \in C \}
\therefore \forall x \{ x \in A \to x \in C \} \text{ *By def'n of transitivity}
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Question 5

- A) $\{\mathbb{Z}\}$ is finite: False, because \mathbb{Z} is the set of integers and there are infinite integers.
- B) $\{\{\mathbb{Z}\}\}\$ is finite: True, because $\{\{\mathbb{Z}\}\}\$ contains only one set, $\{\mathbb{Z}\}$, the set of integers itself.
- C) $\{x \in \mathbb{Q}|x^2\}$ is finite: True, as there are no rational numbers that satisfy the initial condition, the cardinality of the set would be 0, and therefore be finite.
- D) If A is a finite set then $|\mathcal{P}(A)| > |A|$: True, the power set will always have a greater cardinality than the set itself. $\forall n, n \in \mathbb{R} : n < 2^n$

Question 6

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\mathcal{P}(A) = \{\{\emptyset\}, \\ \{1\}, \{2\}, \{3\}, \{4\}, \\ \{1, 2\}, \{1, 3\}, \{1, 4\}, \{2, 3\}, \{2, 4\}, \{3, 4\}, \\ \{1, 2, 3\}, \{1, 2, 4\}, \{1, 3, 4\}, \{2, 3, 4\}, \\ \{1, 2, 3, 4\}\}
|\mathcal{P}(A)| = 2^4 = 16
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Question 7

- A) The number of students who speak Spanish and love dogs is 17.
- B) The number of students who love dogs and cannot cook is 29.
- C) The number of students who speak Spanish, are excellent cooks, and love dogs is 3.