ECE368: Probabilistic Reasoning

Lab 1: Classification with Multinomial and Gaussian Models

Name:	Jiani	Li	Student Number:
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You should hand in: 1) A scanned .pdf version of this sheet with your answers (file size should be under 2 MB); 2) one figure for Question 1.2.(c) and two figures for Question 2.1.(c) in the .pdf format; and 3) two Python files classifier.py and Idaqda.py that contain your code. All these files should be uploaded to Quercus.

1 Naïve Bayes Classifier for Spam Filtering

1. (a) Write down the estimators for p_d and q_d as functions of the training data $\{x_n, y_n\}, n = 1, 2, ..., N$ using the technique of "Laplace smoothing". (1 pt)

- (b) Complete function learn_distributions in python file classifier.py based on the expressions. (1 pt)
- 2. (a) Write down the MAP rule to decide whether y=1 or y=0 based on its feature vector \mathbf{x} for a new email $\{\mathbf{x},y\}$. The d-th entry of \mathbf{x} is denoted by x_d . Please incorporate p_d and q_d in your expression. Please assume that $\pi=0.5$. (1 pt)

- (b) Complete function classify_new_email in classifier.py, and test the classifier on the testing set. The number of Type 1 errors is _____, and the number of Type 2 errors is _____. (1 pt)
- (c) Write down the modified decision rule in the classifier such that these two types of error can be traded off. Please introduce a new parameter to achieve such a trade-off. (0.5 pt)

Write your code in file classifier.py to implement your modified decision rule. Test it on the testing set and plot a figure to show the trade-off between Type 1 error and Type 2 error. In the figure, the x-axis should be the number of Type 1 errors and the y-axis should be the number of Type 2 errors. Plot at least 10 points corresponding to different pairs of these two types of error in your figure. The two end points of the plot should be: 1) the point with zero Type 1 error; and 2) the point with zero Type 2 error. Please save the figure with name nbc.pdf. (1 pt)

(d) If we do not use Laplace smoothing and simply use maximum likelihood estimation in the training phase, what will go wrong? What kind of emails such a classifier would fail to classify? (0.5 pt)

off a word appears only in span and not in ham, and the word odso appears in test email, the probenat test email to ham would be o, and predet to be which is too organistic and might be wrong. Vice-versa.

2 Linear/Quadratic Discriminant Analysis for Height/Weight Data

1. (a) Write down the maximum likelihood estimates of the parameters μ_m , μ_f , Σ , Σ_m , and Σ_f as functions of the training data $\{\mathbf{x}_n, y_n\}, n = 1, 2, ..., N$. (1 pt)

Convertion:

Where $\mu = \frac{1}{404} \frac{1}{1} \frac{1$

1 (b) In the case of LDA, write down the decision boundary as a linear equation of x with parameters μ_m , μ_f , and Σ . Note that we assume $\pi = 0.5$. (0.5 pt)

In the case of QDA, write down the decision boundary as a quadratic equation of x with parameters μ_m , μ_f , Σ_m , and Σ_f . Note that we assume $\pi = 0.5$. (0.5 pt)

- (c) Complete function discrimAnalysis in Idaqda.py to visualize LDA and QDA models and the corresponding decision boundaries. Please name the figures as Ida.pdf, and qda.pdf. (1 pt)
- 2. The misclassification rates are D-118 for LDA, and V-109 for QDA. (1 pt)