## Information theory

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## **Contents**

## 0.1 Preliminary definitions

**Definition 1** *Entropy*(H): The entropy of a random variable X with probability distribution  $p: X \to \mathbb{R}$  is defined as:

$$H(X) \equiv -\sum_{x \in X} p(x) \log p(x) = \mathbb{E}[-\log \circ p]$$

**Definition 2** Condtional entropy(H(X|Y)): The conditional entropy of a random variable X with respect to another variable Y is defined as:

$$\begin{split} H(X|Y) &\equiv -\sum_{y \in Y} p(y) H(X|Y = y) \\ &= \sum_{y \in Y} p(y) \sum_{x \in X} -p(x|y) \log p(x|y) \\ &= \sum_{y \in Y} \sum_{x \in X} -p(y) p(x|y) \log p(x|y) \\ &= \sum_{y \in Y} \sum_{x \in X} -p(y \land x) \log p(x|y) \end{split}$$

In this chapter we introduce a number of basic concepts including influences and noise stability.