

1. Generate $N = 500$, 2-D random data points and plot its corresponding Gaussian PDF.

$$f(x, y) = \frac{\exp\left\{\frac{-1}{2(1-\rho^2)}\left[\left(\frac{(x-\mu_x)}{\sigma_x}\right)^2 - 2\rho\left(\frac{(x-\mu_x)}{\sigma_x}\right)\left(\frac{(y-\mu_y)}{\sigma_y}\right) + \left(\frac{(y-\mu_y)}{\sigma_y}\right)^2\right]\right\}}{2\pi\sigma_x\sigma_y\sqrt{1-\rho^2}} \quad (1)$$

$$T = \rho\left(\frac{x-\mu_x}{\sigma_x}\right)\left(\frac{y-\mu_y}{\sigma_y}\right) + \left(\frac{y-\mu_y}{\sigma_y}\right)^2 \quad (2)$$

2. Generate $N = 500$, 2-dimensional data points that are distributed according to the Gaussian distribution $N(m, S)$, with mean $m = [0, 0]^T$ and covariance matrix

$$S_1 = \begin{bmatrix} \sigma_1^2 & \sigma_{12} \\ \sigma_{21} & \sigma_2^2 \end{bmatrix}$$

3. Considering iris dataset (Click here to download), D of size $N \times M$, with N : number of samples and M : number of features, design a Bayesian classifier to classify the test data. Divide the dataset into training and testing data into (a) 70:30 ratio (b) 80:20 ratio, calculating the accuracy and error rate.
4. Considering a loss function $L(y, a)$, pick the action with minimum expected loss (risk) for the following prior-probabilities

| | | y | | |
|---|------------|---------------------|----------------------------|------------------------------|
| | | None (ω_1) | Lung Cancer (ω_2) | Breast Cancer (ω_3) |
| a | Surgery | 100 | 20 | 10 |
| | No Surgery | 0 | 50 | 50 |