Data Mutation

- Primitive and compound data mutators
 - set! for names
 - set-car!, set-cdr! for pairs
- Stack example
 - · non-mutating
 - mutating
- · Queue example
 - non-mutating
 - mutating

Elements of a Data Abstraction

- · A data abstraction consists of:
 - · constructors -- makes a new structure
 - · selectors
 - · mutators -- changes an existing structure
 - · operations
 - contract

Primitive Data

(define x 10) creates a new binding for name;

special form

returns value bound to name

• To Mutate:

(set! x "foo") changes the binding for name;

special form (value is undefined)

Assignment -- set!

• Substitution model -- functional programming:

(define x 10) (+ x 5) ==> 15

- expression has same value

each time it evaluated (in $(+ \times 5) ==> 15$ same scope as binding)

· With mutation:

(define x 10)

(+ x 5) ==> 15- expression "value" depends

on when it is evaluated

(set! x 94)

 $(+ \times 5) ==> 99$

Compound Data

· constructor:

(cons x y) creates a new pair p

· selectors:

returns car part of pair p (car p) returns cdr part of pair p (cdr p)

• mutators:

($\mathtt{set-car!}\ \mathtt{p}\ \mathtt{new-x}$) changes car part of pair \mathtt{p} (set-cdr! p new-y) changes cdr part of pair p

; Pair, anytype -> undef -- side-effect only!

(define a (list 1 2)) (define b (list 1 2))

(set-car! a 10)

(define b a) a → (1 2)

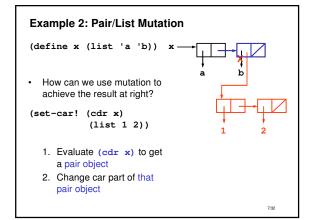
(set-car! a 10)

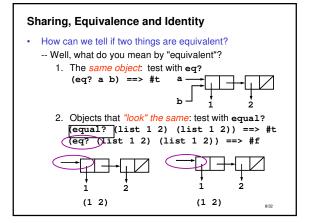
b ==> (10 2) Compare with:

b → (1 2)

b → (1 2)

Example 1: Pair/List Mutation (define a (list 1 2))

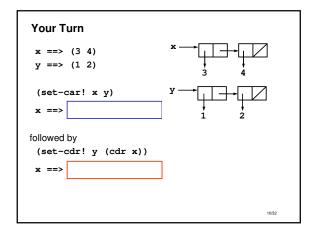




Sharing, Equivalence and Identity

- · How can we tell if two things are equivalent?
 - -- Well, what do you mean by "equivalent"?
 - The same object: test with eq? (eq? a b) ==> #t
 - 2. Objects that "look" the same: test with equal?
 (equal? (list 1 2) (list 1 2)) ==> #t
 (eq? (list 1 2) (list 1 2)) ==> #f
- If we change an object, is it the same object?
 - -- Yes, if we retain the same pointer to the object
- How tell if part of an object is shared with another?
 - -- If we mutate one, see if the other also changes

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End of part 1

- · Scheme provides built-in mutators
 - set! to change a binding
 - set-car! and set-cdr! to change a pair
- Mutation introduces substantial complexity
 - · Unexpected side effects
 - Substitution model is no longer sufficient to explain behavior

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Stack Data Abstraction · constructor: (make-stack) returns an empty stack · selectors: returns current top element from a stack s (top-stack s) operations: (insert-stack s elt) returns a new stack with the element added to the top of the stack (delete-stack s) returns a new stack with the top element removed from the stack returns #t if no elements, #f otherwise (empty-stack? s)

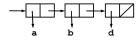
Stack Contract

- If s is a stack, created by (make-stack) and subsequent stack procedures, where i is the number of inserts and j is the number of deletes, then
- 1. If j>i then it is an error
- 2. If j=i then (empty-stack? s) is true, and (top-stack s) and (delete-stack s) are errors.
- 4. If j <= i then (top-stack (insert-stack s val)) = val for any val

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Stack Implementation Strategy

· implement a stack as a list



· we will insert and delete items off the front of the stack

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Stack Implementation

Limitations in our Stack

· Stack does not have identity

```
(define s (make-stack))
s ==> ()

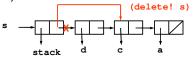
(insert s 'a) ==> (a)
s ==> ()

(set! s (insert s 'b))
s ==> (b)
```

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Alternative Stack Implementation - pg. 1

- Attach a type tag defensive programming
- Additional benefit:
 - Provides an object whose identity remains even as the object mutates



 Note: This is a change to the abstraction! User should know if the object mutates or not in order to use the abstraction correctly.

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Alternative Stack Implementation - pg. 2

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Alternative Stack Implementation - pg. 3 (define (insert-stack! s elt); Stack<A>, A -> Stack<A> (if (stack? s) (set-cdr! s (cons elt (cdr s))) (error "object not a stack:" s) stack) (define (delete-stack! s); Stack<A> -> Stack<A> (if (not (empty-stack? s)) (set-cdr! s (cddr s)) (error "stack underflow - delete")) stack) (define (top-stack s); Stack<A> -> A (if (not (empty-stack? s)) (cadr s) (error "stack underflow - top")))

```
Queue Data Abstraction (Non-Mutating)
· constructor:
                             returns an empty queue
  (make-queue)

    accessors:

                             returns the object at the front of the
  (front-queue q)
                             queue. If queue is empty signals error
 operations:
  (insert-queue q elt)
                            returns a new queue with elt at the
                             rear of the queue
                             returns a new queue with the item at the
  (delete-queue q)
                             front of the queue removed
  (empty-queue? q)
                             tests if the queue is empty
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```

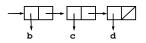
Queue Contract

- If q is a queue, created by (make-queue) and subsequent queue procedures, where i is the number of inserts, j is the number of deletes, and x_i is the ith item inserted into q, then
- 1. If j>i then it is an error
- 2. If j=i then (empty-queue? q) is true, and (front-queue q) and (delete-queue q) are errors.
- 3. If j < i then (front-queue q) = x_{j+1}

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Simple Queue Implementation - pg. 1

· Let the queue simply be a list of queue elements:



- The front of the queue is the first element in the list
- To insert an element at the tail of the queue, we need to "copy" the existing queue onto the front of the new element:



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Simple Queue Implementation – pg. 2

Simple Queue - Orders of Growth

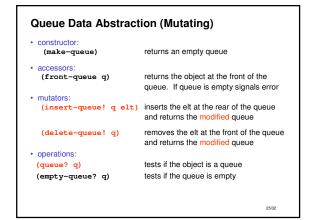
- · How efficient is the simple queue implementation?
 - For a queue of length n
 - Time required -- number of cons, car, cdr calls?
 - Space required -- number of new cons cells?
- front-queue, delete-queue:

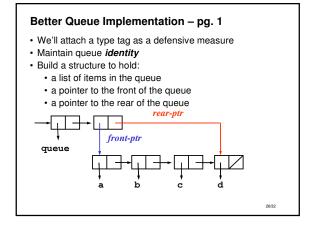
• Time: T(n) = O(1) that is, constant in time • Space: S(n) = O(1) that is, constant in space

• insert-queue:

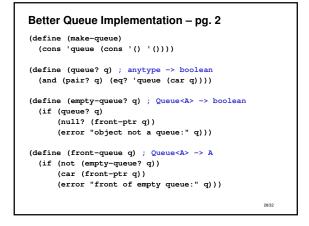
• Time: T(n) = O(n) that is, linear in time • Space: S(n) = O(n) that is, linear in space

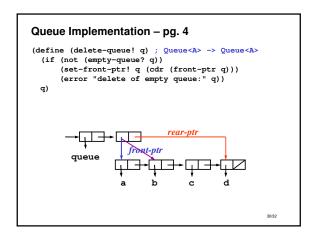
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```
Queue Helper Procedures
· Hidden inside the abstraction
(define (front-ptr q) (cadr q))
(define (rear-ptr q) (cddr q))
(define (set-front-ptr! q item)
  (set-car! (cdr q) item))
(define (set-rear-ptr! q item)
  (set-cdr! (cdr q) item))
    <del>-</del>-----
                       rear-ptr
               front-ptr
    queue
            b
                                               27/32
                           c
```





Mutating Queue - Orders of Growth

- How efficient is the mutating queue implementation?
 - For a queue of length n
 - Time required -- number of cons, car, cdr calls?
 - Space required -- number of new cons cells?
- front-queue, delete-queue!:
 - Time: T(n) = O(1) that is, constant in time • Space: S(n) = O(1) that is, constant in space
- · insert-queue!:
 - Time: T(n) = O(1) that is, constant in time • Space: S(n) = O(1) that is, constant in space

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Summary

• Built-in mutators which operate by side-effect

•set! (special form)

•set-car! ; Pair, anytype -> undef
•set-cdr! ; Pair, anytype -> undef

- Extend our notion of data abstraction to include mutators
- Mutation is a powerful idea
 - enables new and efficient data structures
 - can have surprising side effects
 - breaks our model of "functional" programming (substitution model)

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