summer work

Simplify each expression. No calculators.

1)
$$\frac{4}{3} + \frac{5}{6}$$

2)
$$\frac{2}{12} - \frac{1}{5}$$

3)
$$\frac{2}{12} - \frac{11}{8}$$

4)
$$\frac{1}{15} + \frac{3}{14}$$

Simplify each expression. No calculators!

$$5) \ \frac{\frac{8}{30}}{\frac{12}{5}}$$

6)
$$\frac{1}{8} \cdot \frac{36}{5}$$

7)
$$\frac{\frac{60}{80}}{\frac{10}{-8}}$$

8)
$$\frac{125}{56} \cdot \frac{16}{25}$$

$$9) \ \frac{-\frac{10}{16}}{\frac{36}{60}}$$

10)
$$\frac{12}{40} \cdot \frac{70}{30}$$

Factor each completely.

11)
$$x^2 + 2x$$

12)
$$3a^2 - 21a + 36$$

13)
$$14x^2 + 114x + 112$$

14)
$$6p^4 - 64p^3 + 128p^2$$

15)
$$6k^3 + 13k^2 + 6k$$

16)
$$6x^3 - 7x^2 - 24x$$

17)
$$80r^3 - 200r^2 + 32r - 80$$

18) $150x^3 + 210x^2 - 175x - 245$

19)
$$7m^3 + 56m^2 + 6m + 48$$

Simplify each and state the excluded values.

$$20) \ \frac{x^2 + 6x - 27}{3x^3 + 18x^2 - 81x}$$

21)
$$\frac{v^3 - 2v^2 - v + 2}{v^2 + 2v + 1}$$

Simplify each expression.

22)
$$\frac{x-6}{x-5} \cdot \frac{8x^3 - 40x^2}{x-6}$$

23)
$$\frac{n^2 + 3n + 2}{3n^2} \cdot \frac{1}{n+2}$$

24)
$$\frac{1}{n-5} \div \frac{4n^2}{n^2 - 3n - 10}$$

25)
$$\frac{1}{n+6} \div \frac{n+9}{n^2-2n-48}$$

$$26) \ \frac{3x}{x-4} - \frac{5}{x-1}$$

27)
$$\frac{5}{v+2} + \frac{2}{v-6}$$

28)
$$\frac{2}{x-7} + \frac{5x}{x+5}$$

$$29) \ \frac{2}{x+3} - \frac{2}{x+7}$$

Describe the end behavior of each function.

30)
$$f(x) = x^3 - 3x^2 + 1$$

- A) Rises to the left. Rises to the right
- B) Falls to the left. Rises to the right
- C) Rises to the left. Falls to the right
- D) Falls to the left. Falls to the right

32)
$$f(x) = -2x^2 + 4x$$

- A) Falls to the left. Falls to the right
- B) Rises to the left. Rises to the right
- C) Rises to the left. Falls to the right
- D) Falls to the left. Rises to the right

Simplify each expression.

31)
$$f(x) = x^4 - x^2 - x - 2$$

- A) Rises to the left. Falls to the right
- B) Falls to the left. Falls to the right
- C) Rises to the left. Rises to the right
- D) Falls to the left. Rises to the right

33)
$$f(x) = -x^5 + 3x^3 - 2$$

- A) Rises to the left. Rises to the right
- B) Falls to the left. Falls to the right
- C) Falls to the left. Rises to the right
- D) Rises to the left. Falls to the right

34)
$$(7p^3 - p^4 - 4p) + (6p - 3p^2 + 5p^4 + 4p^3) - (2p^3 + p^4 + p)$$

35)
$$(8n^4 + 7 - 3n^2) + (8n^4 + 5n^2 + 2n^3 - 7) - (4n^3 + 7 - n^2)$$

Find each product.

36)
$$(2x^2 + 6x - 7)(x - 1)$$

37)
$$(5v^2 + 2v - 5)(v^2 - 4v - 4)$$

Solve each system by substitution.

38)
$$y = -6$$
 $2x - y = 10$

39)
$$-8x - y = 19$$

 $y = -7x - 17$

40)
$$y = 2x - 4$$

 $6x + 4y = -16$

Solve each equation. No decimals, leave all answers as fractions with simplified radicals if needed.

41)
$$2(7b+6)-3b=89$$

42)
$$-158 = -4p - 6(8 + 3p)$$

43)
$$-(-3b+6)-2=2(-7+b)+3b$$

44)
$$-52 - 32v = -4(4 + 8v)$$

$$45) \ \frac{1}{2} = \frac{x-3}{6} + \frac{1}{3}$$

Solve each equation.

46)
$$|v+2|=2$$

47)
$$|4x| - 6 = 34$$

Solve each equation by factoring. No decimals, leave all answers as fractions with simplified radicals if needed.

48)
$$m^2 - 11m + 24 = 0$$

49)
$$n^2 + 4n = 0$$

Solve each equation by taking square roots. No decimals, leave all answers as fractions with simplified radicals if needed.

$$50) \ 10v^2 + 2 = -133$$

51)
$$6 - 6n^2 = -18$$

Solve each equation. Remember to check for extraneous solutions.

$$52) \ \frac{n-2}{n} + \frac{1}{n} = \frac{n-6}{3n}$$

$$53) \ \frac{3}{x^2 - 3x} = \frac{1}{x^2 - 3x} + \frac{1}{x}$$