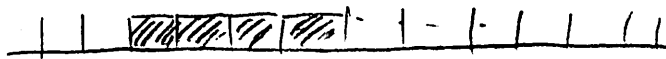


# Slotted Aloha



$N$  nodes  $\Pr(N \text{ nodes collide for a consecutive of } M \text{ slots})$

$$\prod_{i=1}^M \Pr(N \text{ nodes collide in } i\text{th slot})$$

$$= \prod_{i=1}^M [1 - \Pr(\text{no collision in slot } i)] = [1 - \underbrace{np(1-p)^{n-1}}_{\text{Prob of no collision}}]^M$$

$M \uparrow \Pr \downarrow$

Prob of no collision  
Max it?

Given  $N$  stations in a <sup>mult</sup> collision, what is the probability that no collision happens for retransmission for a particular station?

$$\begin{aligned} \text{Prob} &= \Pr(\text{no other station choose the same } k) \\ &= \left[ \frac{1}{2^m} \left(1 - \frac{1}{2^m}\right)^{N-1} \right] \times 2^m = \left(1 - \frac{1}{2^m}\right)^{N-1} \end{aligned}$$

if  $m$  is big, Prob is small.  
 $N$  is big, Prob is high

$$\text{bit time} = \frac{1}{10 \times 10^6} \times 1023 \times \textcircled{5/2} = \frac{5 \times 10^5}{10^7} = 0.05 \text{ s} = 50 \text{ ms}$$

$$\begin{array}{c} \gamma=3 \\ \hline 11010001 \quad 101^R \\ \hline D \quad R \end{array} = \begin{array}{c} 11010001000 = D \cdot 2^r \\ \hline 0000000101 \text{ XOR } \\ \hline 11010001101 \end{array} \rightarrow R$$

$$= (D \cdot 2^r) \text{ XOR } R$$

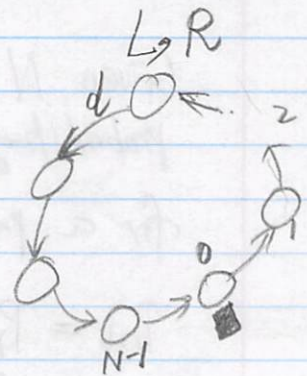
$$\begin{array}{c} (D \cdot 2^r) \text{ XOR } R \\ \hline \text{XOR } R \end{array} = NG$$

$$\text{XOR } R = NG \text{ XOR } R$$

$$D \cdot 2^r = NG \text{ XOR } R$$

$$R = (D \cdot 2^r) \% G$$

Token ring performance



throughput:

"1-node only":  $\frac{L}{\frac{L}{R} + N \cdot d} = R \cdot \frac{L}{R(\frac{L}{R} + N \cdot d)} = R \cdot \frac{L}{L + N \cdot d \cdot R}$

$$= R \cdot \frac{1}{1 + \frac{N \cdot d \cdot R}{L}} < R$$

"M-node" total:  $\frac{M \cdot L}{M \cdot \frac{L}{R} + N \cdot d} = R \cdot \frac{ML}{R(M \cdot \frac{L}{R} + N \cdot d)} = R \cdot \frac{ML}{ML + N \cdot d \cdot R}$

$$= R \cdot \frac{1}{1 + \frac{N \cdot d \cdot R}{ML}}$$

individual:  $\frac{L}{M \cdot \frac{L}{R} + N \cdot d} = \frac{R}{M} \cdot \frac{1}{1 + \frac{N \cdot d \cdot R}{ML}} < \frac{R}{M}$