



* Binary Search *

→ Linear Search → T.C = $O(n)$

* Binary Search :

→ Applied only on monotonic functions.

↳ value should be in increasing or decreasing functions.

Algo: start = 0; end = n-1; mid = $s + \frac{(e-s)}{2}$

write s ← {

1. find mid
2. compare with key. if found then return else --
3. compare greater or less than

 ↙ ↘

 (mid > key) (mid < key)

 ↙ ↘

 e = mid - 1 s = mid + 1

 go to step 1 go to step 2.

Q.

3 | 5 | 9 | 13 | 27

key = 13.

Ans. start = 0 ; e = n-1; mid = $s + \frac{(e-s)}{2} = 2$

(9 < 13)

ans = mid < key

$$\therefore s = \text{mid} + 1$$

$$\hookrightarrow \text{mid} = s + \frac{(e-s)}{2} = 3$$

$\therefore \text{arr}[\text{mid}] = \text{key}$
(9=13) } \rightarrow return the ans
that key is found.

Q. 3 | 7 | 11 | 13 | 19 | 27 key = 27

Ans $s=0$; $e=n-1=5$; $\text{mid} = s + \frac{(e-s)}{2} = 2$

$\rightarrow \text{arr}[\text{mid}] < \text{key}$.

$\therefore s = \text{mid} + 1$; $\text{mid} = s + \frac{(e-s)}{2} = 4$

$\rightarrow \text{arr}[\text{mid}] < \text{key}$
 $s = \text{mid} + 1$; $\text{mid} = 5$

$\rightarrow \text{arr}[\text{mid}] == \text{key} \rightarrow \text{cout} << \text{"found"} << \text{endl};$

T.C \Rightarrow

① n size

② $n/2$ size

$n/4$

$n/8$

$n/16$

\vdots

0

length=1

9

$$n + n/2 + n/4 + n/8 + n/16 + \dots + \frac{n}{2^k} =$$

$$O(\log_2(n))$$

$$\therefore \frac{n}{2^k} = 1$$

$$n = 2^k$$

$$k = \log_2(n)$$