

Question 3.

a)

```
import math
```

```
def main(x, e, imax):
```

```
    i = 1
```

```
    print("iteration" + " " + "approximation")
```

```
    while (i <= imax):
```

```
        root = x - (f(x)/fp(x))
```

```
        print(i, end="")
```

```
        print(" "*12, end="")
```

```
        print('%0.6f' % root)
```

```
        if ((abs(1 - x/root)) < e):
```

```
            return root
```

```
        i = i+1
```

```
        x = root
```

```
    print("failed to converge in" + imax + "iterations")
```

```
def f (i):
```

```
    return ans
```

```
def fp (i):
```

```
    return ans
```

```
if __name__ == '__main__':
```

```
    main()
```

```
import math

def main(x,e,imax):
    i = 1
    print("iteration" + " " + "approximation")
    while (i <= imax):
        root = x - (f(x)/fp(x))
        print(i, end="")
        print(" "*12, end="")
        print('%0.6f' % root)

        if ((abs(1 - x/root)) < e):
            return root
        i = i+1
        x = root
    print("failed to converge in" + imax + "iterations")

def f (i):
    ans = (math.cos(i + (2 ** 0.5)) + (i**2)/2 + (2 ** 0.5)*i)
    return ans

def fp (i):
    ans = -(math.sin(i + 2**0.5)) + i + 2**0.5
    return ans

if __name__ == '__main__':
    main(1,0.000001,50)
```

iteration	approximation
1	0.332708
2	-0.127228
3	-0.458070
4	-0.700796
5	-0.880674
6	-1.014694
7	-1.114841
8	-1.189796
9	-1.245947
10	-1.288034
11	-1.319587
12	-1.343247
13	-1.360990
14	-1.374297
15	-1.384276
16	-1.391761
17	-1.397374
18	-1.401584
19	-1.404741
20	-1.407109
21	-1.408885
22	-1.410217
23	-1.411216
24	-1.411966
25	-1.412528
26	-1.412949
27	-1.413264
28	-1.413501
29	-1.413677
30	-1.413798
31	-1.413910
32	-1.413958
33	-1.413958

```

1 import math
2
3 def main(x,e,imax):
4     i = 1
5     print("iteration" + " " + "approximation")
6     while (i <= imax):
7         root = x - (f(x)/fp(x))
8         print(i, end=" ")
9         print(" %12, end=")
10        print('%6f' % root)
11
12        if ((abs(1 - x/root)) < e):
13            return root
14        i = i+1
15        x = root
16    print("failed to converge in" + imax + "iterations")
17
18 def f(i):
19     ans = (math.cos(i + (2 ** 0.5)) + (i**2)/2 + (2 ** 0.5)*i)
20     return ans
21
22 def fp(i):
23     ans = (-(math.sin(i + 2**0.5)) + i + 2**0.5)
24     return ans
25
26 if __name__ == '__main__':
27     main(1,0.000001,50)

```

```

CSC349a -- -zsh -- 100x36
punetgrewal@Puneets-MacBook CSC349a % python3 newton.py
iteration  approximation
1          0.332708
2         -0.127228
3         -0.458070
4         -0.700796
5         -0.880674
6         -1.014694
7         -1.114841
8         -1.189796
9         -1.245947
10        -1.288034
11        -1.319587
12        -1.343247
13        -1.360990
14        -1.374297
15        -1.384276
16        -1.391761
17        -1.397374
18        -1.401584
19        -1.404741
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21        -1.408885
22        -1.410217
23        -1.411216
24        -1.411966
25        -1.412528
26        -1.412949
27        -1.413264
28        -1.413501
29        -1.413677
30        -1.413798
31        -1.413910
32        -1.413958
33        -1.413958
punetgrewal@Puneets-MacBook CSC349a %

```

c)

def q3c(root):

```
root = round(root, 3)
ans1 = f(root)
print("f(xa)=" , ans1)
ans2 = fp(root)
print("fp(xa)=" ,ans2)
true_value = -(2**0.5)
```

```
relative_error = abs((true_value - root)/root)
print("error=" , relative_error)
```

```
f(xa)= -2.220446049250313e-16
fp(xa)= 1.6233681066069039e-12
error= 0.00015103421010977501
```

```
def q3c(root):
```

```
    root = round(root, 3)
    ans1 = f(root)
    print("f(xa)=" , ans1)
    ans2 = fp(root)
    print("fp(xa)=" ,ans2)
    true_value = -(2**0.5)

    relative_error = abs((true_value - root)/root)
    print("error=" , relative_error)
```

```
puneetgrewal@Puneets-MacBook CSC349a % python3 newton3b.py
f(xa)= -2.220446049250313e-16
fp(xa)= 1.6233681066069039e-12
error= 0.00015103421010977501
puneetgrewal@Puneets-MacBook CSC349a %
```

d)

Matplotlib wouldn't print my graph for some reason after much trouble shooting . I have included the file although. After trying to save the plot as a blurry png which I could barely see, I think the approximation is inaccurate as the graph was a big curve.