

Problem Statement 1:

A company manufactures LED bulbs with a faulty rate of 30%. If I randomly select 6 chosen LEDs, what is the probability of having 2 faulty LEDs in my sample? Calculate the average value of this process. Also evaluate the standard deviation associated with it.

Solution:

$$p = \text{Success} = 0.3 ; q = \text{Failure} = 0.3$$

1. Calculate Mean

$$\mu = E(x) = n \cdot p$$

Where:

$$n = \text{No. of Trials} = 6$$

$$p = \text{Success ratio} = 0.3$$

$$\text{Mean} = 6 \cdot 0.3 = 1.8$$

1. Variance

$$\text{Var} = npq$$

Where:

$$n = \text{No. of Trials} = 6$$

$$p = \text{Success ratio} = 0.7$$

$$q = \text{Failure ratio} = 0.3$$

$$= 6 \cdot 0.7 \cdot 0.3$$

$$= 1.26$$

1. Standard Deviation

$$\sqrt{npq}$$

Where:

$$n = \text{No. of Trials} = 6$$

$$p = \text{Success ratio} = 0.7$$

$$q = \text{Failure ratio} = 0.3$$

$$\text{Standard Deviation} = \sqrt{6 \cdot 0.7 \cdot 0.3}$$

$$= 1.12$$

Problem Statement 2:

Gaurav and Barakha are both preparing for entrance exams. Gaurav attempts to solve 8 questions per day with a correction rate of 75%, while Barakha averages around 12 questions per day with a correction rate of 45%. What is the probability that each of them will solve 5 questions correctly? What happens in cases of 4 and 6 correct solutions? What do you infer from it? What are the two main governing factors affecting their ability to solve questions correctly? Give a pictorial representation of the same to validate your answer.

Gaurav:

$$n = 8$$

$$p = 0.75$$

$$q = 0.25$$

Barakha:

$$n = 12$$

$$p = 0.45$$

$$q = 0.55$$

problem of each solving 5 questions correctly

$$p = {}^8C_5 (0.75)^5 (0.25)^3$$

$$= {}^{12}C_5 (0.45)^5 (0.55)^7$$

$$= 0.212 \times 0.214$$

$$= 0.045$$

Problem of each solving 4 questions correctly

$$= 0.0896 \times 0.1624$$

$$= 0.0145$$

Problem of each solving 6 questions correctly

$$= 0.3115 \times 0.2124$$

$$= 0.0661$$

Probability is increasing with number of correct questions.

Problem Statement 3:

Customers arrive at a rate of 72 per hour to my shop. What is the probability of k customers arriving in 4 minutes? a) 5 customers, b) not more than 3 customers, c) more than 3 customers. Give a pictorial representation of the same to validate your answer.

In []:

Problem Statement 4:

I work as a data analyst in Aeon Learning Pvt. Ltd. After analyzing data, I make reports, where I have the efficiency of entering 77 words per minute with 6 errors per hour. What is the probability that I will commit 2 errors in a 455-word financial report?

What happens when the no. of words increases/decreases (in case of 1000 words, 255 words)? How is the λ affected? How does it influence the PMF? Give a pictorial representation of the same to validate your answer.

Given Data,

77 words per minute

6 errors per hour

possibility of 2 errors in a 455 words

no.of words per hour= 77×60

$$=4620$$

$$\mu = \text{errors in 455 words} = 6/4620 \times 455$$

$$=0.59$$

$$p(2) = (e)^{-0.59} (0.59)^{2/2!}$$

$$=0.0965$$

In case of 1000 words

$$\mu = 6/4620 \times 1000$$

$$=1.3$$

$$p(2) = (e)^{-1.3} (1.3)^{2/2!}$$

$$=0.23$$

In case of 255 words=0.04

Probability of error increase as the no of intervals increases.

In []: