

Statistics - 3
Additional Exercise - 13.11442

Solⁿ 1)

$$p = 0.3$$

\therefore this is a binomial distribution where $n=6, r=2$

$$\begin{aligned} P(X=2) &= {}^6C_2 \cdot (0.3)^2 (0.7)^4 \\ &= \frac{6 \times 5 \times \cancel{4 \times 3 \times 2 \times 1}}{2 \times 1 \times \cancel{4 \times 3 \times 2 \times 1}} (0.09) (0.2401) \\ &= 15 (0.09) (0.2401) \\ &= 0.3241 \end{aligned}$$

$$\text{and } \mu = np = 6(0.3) = 1.8$$

$$\begin{aligned} \sigma &= \sqrt{np(1-p)} = \sqrt{6(0.3)(0.7)} \\ &= \sqrt{1.26} = \underline{\underline{1.224}} \end{aligned}$$

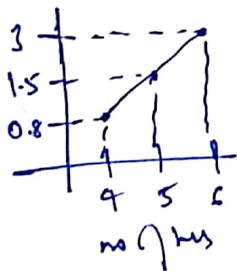
Solⁿ 2: $P_{\text{gamey}} = 0.75, n=8 \therefore P_{\text{gamey}}(X=5) = {}^8C_5 (0.75)^5 (0.25)^3$

$$\begin{aligned} &= \frac{8(7)(6)(5!)}{5! 3!} (0.2373) \\ &= 42 (0.2373) (0.0156) \\ &= \underline{\underline{0.1557}} \end{aligned}$$

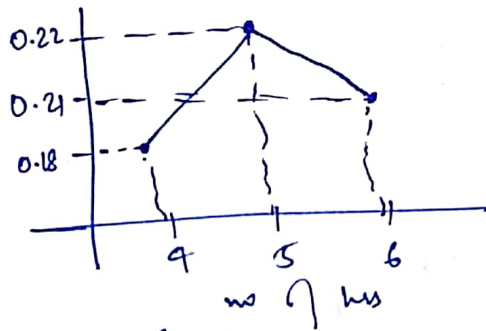
$$\begin{aligned} P_{\text{black}} &= 0.45, n=12, P_{\text{black}}(X=5) = {}^{12}C_5 (0.45)^5 (0.55)^7 \\ &= (79)(8)(0.018)(0.015) \\ &= \underline{\underline{0.2224}} \end{aligned}$$

$$\begin{aligned}
 P_{\text{gamer}} (X_1=4) &= 8C_4 (0.35)^4 (0.25)^4 \\
 &= 70 \times 0.3164 \times 0.0039 \\
 &= \underline{\underline{0.0865}}
 \end{aligned}$$

$$\begin{aligned}
 P_{\text{blanks}} (X_1=6) &= 12C_6 (0.45)^6 (0.55)^6 \\
 &= \underline{\underline{0.2123}}
 \end{aligned}$$



Gamer



Blanks

Sol 3 | 72 / hr

$$\lambda (\text{per min}) = \frac{72}{60} = 1.2$$

$$\lambda (\text{4 time / week}) = 1.2 \times 4 = 4.8$$

$$\textcircled{a} \quad 5 \text{ customers} \quad \frac{e^{-4.8} (4.8)^5}{5!} = \frac{20.967}{120} = 0.1747$$

⑥ not more than 3

$$\frac{e^{-4.8} (4.8)^0}{0!} = 0.0082$$

$$\begin{array}{l}
 \left. \begin{array}{l}
 \frac{e^{-4.8} (4.8)^1}{1!} = 0.0394 \\
 \frac{e^{-4.8} (4.8)^2}{2!} = 0.0947 \\
 \frac{e^{-4.8} (4.8)^3}{3!} = 0.1516
 \end{array} \right| \begin{array}{l}
 \frac{e^{-4.8} (4.8)^2}{2} = 0.0947 \\
 P(X_1 \leq 3) = \sum_{i=0}^3 X_i \\
 = \underline{\underline{0.2941}}
 \end{array}
 \end{array}$$

⑦ More than 3 customers

$$\frac{e^{-4.8} (4.8)^4}{4!} = 0.1820 \quad \left| \quad \frac{e^{-4.8} (4.8)^5}{5!} = 0.1747 \quad \left| \quad \frac{e^{-4.8} (4.8)^6}{6!} = 0.1397
 \right.$$

$$\therefore P(X_1 > 3) = \sum_{i=4}^6 X_i = \underline{\underline{0.4964}}$$

Sol 4 | 6 error/hr
77 × 60 words/hr | $\therefore 1 \text{ error} / \text{word} = \frac{6}{77 \times 60} = \frac{1}{770}$

$$\mu = \frac{455}{770} = 0.591$$

$$P(x_i = 2) = \frac{(e^{-(0.591)})(0.591)^2}{2!}$$

$$= 0.09671$$

$$\mu_2 = \frac{1000}{770} = 1.2987$$

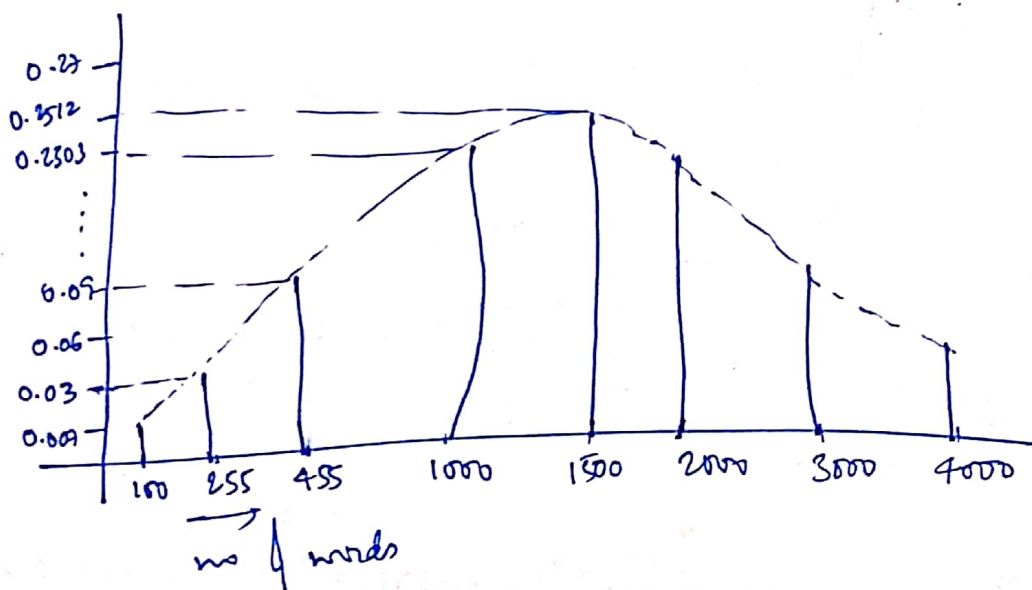
$$P(x_i = 7) = \frac{e^{-1.2987}(1.2987)^7}{7!}$$

$$= 0.2303$$

$$\mu = \frac{255}{770} = 0.3311$$

$$P(x_i = 2) = \frac{e^{-0.3311}(0.3311)^2}{2!}$$

$$= 0.03936$$



Sol 5 | $f(x) = 0.05$ for $0 \leq x \leq 20$

$$\int_0^{10} f(x) \cdot dx = \int_0^{10} 0.05 = (0.05x)_0^{10} = 0.5$$

