

Competitive Coding Experiment 3

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KRC2-A

Q. Given 3 integers n, a, b return n^{th} magical number
since the answer may be very large return modulo $1e9+7$.

$n=1, a=2, b=3$ output:- 2

Magical number is no. divisible by either a or b .

Brute:- Run a loop till $\text{cnt} < k$ check if cnt is divisible by a or b , increment cnt .

T.C:- $O(N \times \min(a, b))$

Optimal:- we count number of optimal multiples a $a \leq x$
i.e. x/a .

then count multiples of b i.e. x/b

No. of multiples of both a and b $x/\text{lcm}(a, b)$

So, total number that are $\leq x$

$$\text{count}(x) = \frac{x}{a} + \frac{x}{b} - \frac{x}{\text{lcm}(a, b)}$$

Now we need smallest x such that $\text{count}(x) \geq r$

set $\text{low} = 1$, $\text{high} = r \times \min(a, b)$

$\text{mid} = \text{low} + \text{high} / 2$

for mid compute $\text{count} = \frac{\text{mid}}{a} + \frac{\text{mid}}{b} - \frac{\text{mid}}{\text{lcm}}$

if $\text{count} \leq r$:

mid could be ans
search left side.

else search right side

return ans;

Time Complexity:- $O(r \times \min(a, b))$