CS1101S Midterms Cheatsheet AY19/20

by chrisgzf (adapted from https://github.com/ning-y/Cheatsheets/)

Recursive/Iterative: Check if there are deferred function reverse(xs) {
 operations function rev(original function reverse)

```
function fact_iter(n) {
    function mult_remaining(counter , product) {
       return counter === 1
           ? product
            : mult_remaining(counter - 1, product
            * counter);
    return mult remaining(n, 1);
function fib(n) {
    function f(n, k, x, y) {
       return (k > n)
           ?у
           : f(n, k + 1, y, x + y);
    return (n < 2) ? n : f(n, 2, 0, 1);
function gcd(a, b) {
    return b === 0
       ? a
        : gcd(b, a % b):
function cc(amount , kinds_of_coins) {
    return amount === 0
       ? 1
        : amount < 0 || kinds of coins === 0
           ? 0
            : cc(amount - first denomination(kinds
                of_coins), kinds_of_coins) +
             cc(amount , kinds_of_coins - 1);
```

Order of Growth

Big Theta: The function r has order of growth $\theta(g(n))$ if there are positive constants k_1 and k_2 and a number n_0 such that $k_1*g(n) \le \mathrm{r(n)} \le k_2*g(n)$ for any $n > n_0$.

Big O: The function r has order of growth O(g(n)) if there is a positive constant k such that $r(n) \leq k * g(n)$ function flatten_tree(xs) { function h(xs, prev) { return is_null(xs)}

Big Omega: The function r has order of growth $\Omega(g(n))$ if there is a positive constant k such that $k*g(n) \leq r(n)$ for any sufficiently large value of n

Order (small to big): 1, log n, n, n log n, n^2 , n^3 , 2^n , 3^n , n^n

Lists: A list is either null or a pair whose tail is a list.

A list of a certain type is either null or a pair whose head is of that type and whose tail is a list of that type

```
function rev(original, reversed) {
       return is_null(original)
           ? reversed
            : rev(tail(original),
                 pair(head(original), reversed));
    return rev(xs ,null);
function append iter(xs, ys){
    // iterative process
    function app(xs, ys, c) {
       return is null(xs)
       ? c(ys)
       : app(tail(xs), ys,
             x => c(pair(head(xs), x))
   return app(xs, ys, x => x);
function remove duplicates(1st) {
    return is null(1st)
       ? null
       : pair(head(lst), remove_duplicates(
           filter(x => !equal(x, head(lst)),
                   tail(lst)))):
```

Passing the deferred operation as a function in an extra argument is called "Continuation-Passing Style" (CPS).

Trees: A tree of certain data items is a list whose elements are such data items, or trees of such data items. function find(bst, name) {

Besides the base case, these operations consider two cases. One, when the element is itself a tree, and another when it is not.

function subsets(s) {
 return accumulate
 (x, s1) => ap

Binary Trees: A binary tree of a certain type is null or a list with three elements, whose first element is of that type and whose second and third elements are binary trees of that type. function choose(n, r) { if $(n < 0 \mid | r < 0)$ return 0; } else if (r === 0)

Binary Search Trees: A binary search tree of Strings is a binary tree of Strings where all entries in the left subtree are smaller than its value and all entries in the right subtree are larger than its value.

```
function insert(bst, item) {
    if (is_empty_tree(bst)) {
        return make_tree(item, make_empty_tree(),
          make_empty_tree());
   } else {
        if (item < entry(bst)) {</pre>
            // smaller than i.e. left branch
            return make_tree(entry(bst),
                       insert(left branch(bst),
                              item),
                       right_branch(bst));
       } else if (item > entry(bst)) {
            // bigger than entry i.e. right branch
            return make_tree(entry(bst),
                       left_branch(bst),
                       insert(right_branch(bst),
                              item));
        } else {
            // equal to entry.
            // BSTs should not contain duplicates
            return bst:
       }
   }
    return is_empty_tree(bst)
       ? false
        : name === entry(bst)
            ? true
            : name < entry(bst)
               ? find(left branch(bst), name)
                : find(right_branch(bst), name);
```

Permutations & Combinations

```
if (n < 0 | | r < 0) {
        return 0:
    } else if (r === 0) {
        return 1;
    } else {
        // Consider the 1st item, there are 2 choices:
        // To use, or not to use
        // Get remaining items with wishful thinking
        const to use = choose(n - 1, r - 1);
        const not to use = choose(n - 1, r);
        return to_use + not_to_use;
}
function combinations(xs, r) {
    if ( (r !== 0 && xs === null) || r < 0) {
        return null:
   } else if (r === 0) {
        return list(null);
   } else {
        const no choose = combinations(tail(xs), r):
        const yes_choose = combinations(tail(xs),
                                        r - 1):
        const yes_item = map(x => pair(head(xs), x),
                             yes_choose);
        return append(no_choose, yes_item);
function makeup_amount(x, coins) {
    if (x === 0) {
        return list(null):
   } else if (x < 0 || is_null(coins)) {</pre>
        return null:
   } else {
        // Combinations that do not use the head coin.
        const combi_A = makeup_amount(x, tail(coins));
        // Combinations that do not use the head coin
        // for the remaining amount.
        const combi_B = makeup_amount(x - head(coins),
                                      tail(coins));
        // Combinations that use the head coin.
        const combi_C = map(x => pair(head(coins), x),
                            combi B);
        return append(combi_A, combi_C);
}
```

Insertion sort takes elements from left to right, and *inserts* them into correct positions in the sorted portion of the list (or array) on the left. This is analagous to how most people would arrange playing cards.

Selection sort picks the smallest element from a list (or array) and puts them in order in a new list.

```
Time Complexity: \Omega(n^2) O(n^2)
function selection_sort(xs) {
    if (is_null(xs)) {
        return xs;
    } else {
        const x = smallest(xs);
        return pair(x,
            selection_sort(remove(x, xs)));
}
function smallest(xs) {
    function h(xs, min) {
        return xs === null
            ? min
            : head(xs) < min
                ? h(tail(xs), head(xs))
                : h(tail(xs), min);
    return h(xs, head(xs));
```

Quicksort is a divide-and-conquer algorithm. Partition takes a pivot, and positions all elements smaller than the pivot on one side, and those larger on the other. The two 'sides' are then partitioned again.

```
function take(xs, n) {
Time Complexity: \Omega(nlogn) O(n^2)
                                                          return n === 0
                                                             ? null
function partition(xs, p) {
                                                              : pair(head(xs),
    function h(xs, lte, gt) {
                                                                     take(tail(xs), n - 1));
        if (is_null(xs)) {
            return pair(lte, gt);
                                                     function drop(xs, n) {
                                                         return n === 0
        } else {
            const first = head(xs);
                                                             ? xs
                                                              : drop(tail(xs), n - 1);
            return first <= p
                ? h(tail(xs), pair(first, lte), gt) }
                : h(tail(xs), lte, pair(first, gt));
                                                     function merge(xs, ys) {
    }
                                                          if (is_null(xs)) {
    return h(xs, null, null);
                                                             return ys;
                                                         } else if (is_null(ys)) {
                                                             return xs;
                                                         } else {
function quicksort(xs) {
                                                              const x = head(xs):
                                                              const y = head(ys);
    if (is_null(xs) || is_null(tail(xs))) {
        return xs;
                                                             return (x < y)
                                                                 ? pair(x, merge(tail(xs), ys))
    } else {
        const pivot = head(xs);
                                                                  : pair(y, merge(xs, tail(ys)));
                                                        }
        const splits = partition(tail(xs), pivot);
        const smaller = quicksort(head(splits));
        const bigger = quicksort(tail(splits));
        return append(smaller, pair(pivot, bigger)); function merge_sort(xs) {
    }
                                                         if (is_null(xs) || is_null(tail(xs))) {
}
                                                         } else {
                                                              const mid = math_floor(length(xs) / 2);
                                                              return merge(merge_sort(take(xs, mid)),
                                                                          merge_sort(drop(xs, mid)));
```

Mergesort is a divide-and-conquer algorithm.

Time Complexity: $\Omega(nlogn)$ O(nlogn)