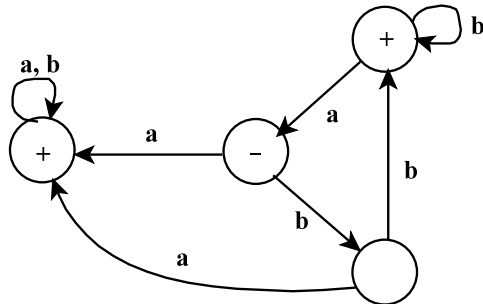
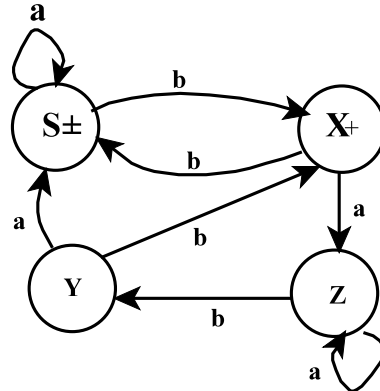


**Trent University**  
 Computing and Information Systems 3050H  
 Fall 2020  
**Assignment 3:** Due December 9, 2020

**1) Convert the following FA into a PDA.**



**2) Convert the following FA into a CFG.**



**3) Eliminate  $\Lambda$ -productions for the CFG:**

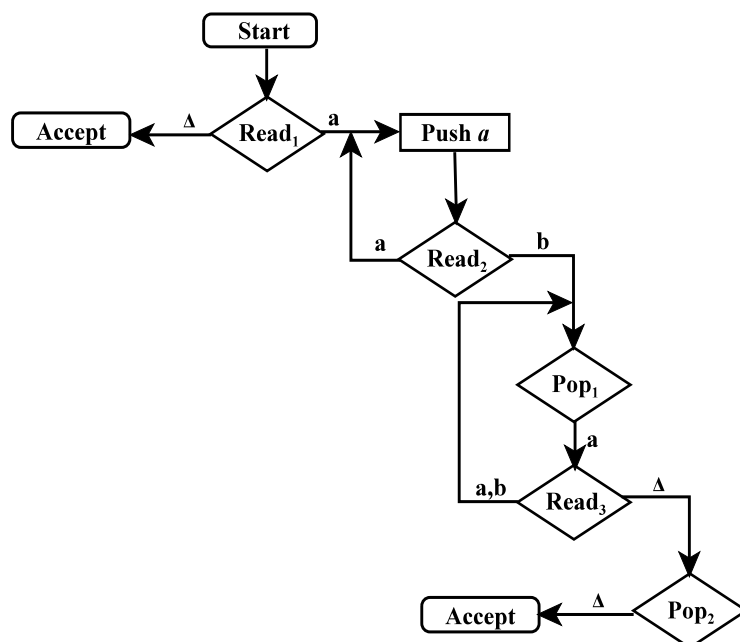
$S \rightarrow aXbX$   
 $X \rightarrow aY \mid bY \mid \Lambda$   
 $Y \rightarrow X \mid ZY \mid b$   
 $Z \rightarrow XY \mid c$

**4) Convert the following CFG into CNF.**

$S \rightarrow ABC$   
 $A \rightarrow aAS \mid a \mid \Lambda$   
 $B \rightarrow SbS \mid A \mid bb$   
 $C \rightarrow b$

**5) Consider the following non-deterministic PDA. Are the following words accepted by this PDA? For those that are rejected, indicate which state the PDA is in when the crash occurs.**

- (a) aaabbb
- (b) bbbaaa
- (c) aaabbbaa
- (d) aaaabaa
- (e) aaabaa



6) Use the algorithmic approach given in Module 5, Advanced CFLs to create a CFG for the language  $L = b(a^*b+a)^*$

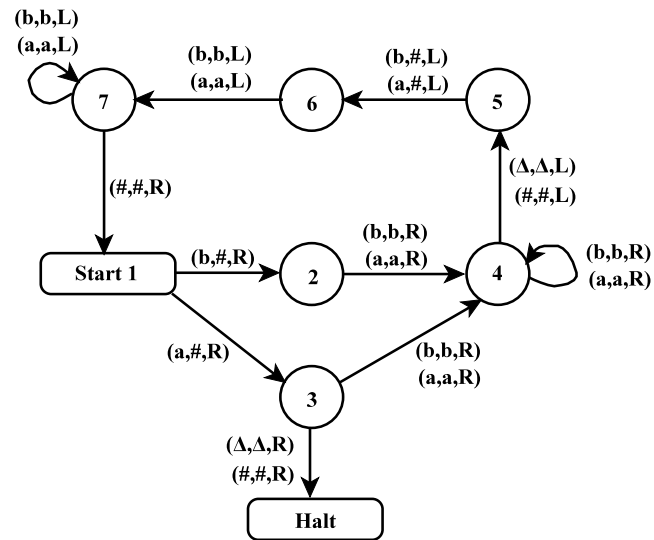
7) Consider the following Turing Machine: Show the execution traces using each of the following input strings (use the same format as shown in Module 6, Turing Machines):

(a) aaa

(b) aba

(c) ababb

(d) What does the machine do?



8) Build a Turing Machine over the alphabet  $\Sigma = \{a, b\}$  that accepts all words which start and end with the same letter. Note that this is a Regular Language. Show the execution traces with the following input strings:

(a) baa

(b) aba

(c) b

9) Build a TM over the alphabet  $E = \{a, b\}$  that accepts the language DoubleA where each word has twice as many a's as b's. You might find it easier if you use the Insert# routine.